A Check of the Design of an

I-Beam Highway Bridge

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The Faculty of

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by

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THESIS

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Introduction

The purpose of this thesis is to check the design of a single span simply supported highway bridge.

This bridge as proposed will be constructed on the relocation of U.S. highway number 31, also to be known as the Muskegon East Belt Road, where it crosses Black Creek in Fruitport Township, Muskegon County, in the state of Michigan. Previous to the opening of this new highway it has been necessary for all thru traffic to travel over the already congested streets of Muskegon. Thus, by the construction of the East Belt Road this situation will be greatly alleviated.

The centerline of this highway makes a 56 degree angle with the abutment wall which runs parallel to the flow of the Black Creek. The span length from center to center of bearings is 57'-1" exact and the overall width of roadway from curb to curb is 42'-0" exact.

The drainage area tributary in this crossing is 56 square miles and the waterway area required based on Talbot's formula (using c = 0.1) is 260 square feet.

The existing bridge one mile downstream has a tributary drainage area of 57.5 square miles, provides 246 square feet and appears adequate. The proposed structure provides 238 square feet.

All of the above mentioned conditions concerning the site and the river were taken into account both in the analysis and the design of the bridge. Symbols

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A	Area
Ъ	breath or width
đ	depth of beam to center of steel
e	eccentricity of application of load
f	unit stress
I	moment of inertia
j	ratio of lever arm of resisting
	couple to depth, d
k	ratio of depth of neutral axis to
	depth, d
L	length in feet
1	length in inches
М	moment
n	ratio of modulus of elacticity of
	steel to the modulus of elacticity
	of concrete
R	reaction
v	unit shear
W	load per unit of length
Z	section modulus
ø	round
u	bond
Abbrevatio	ons
	M. M. Barra Charles Williamore Descriptions

M.S.H.D.	Michigan State Highway Department					
A.A.S.H.O.	American Association of State High-					
	way Officials					
A.I.S.C.	American Institute of Steel Construct- ion					

The specifications and maximum unit stresses used are those of the Michigan State Highway Department published in 1944 and from the specification for highway design published by the American Association of State Highway Officals in 1944.

fc'	3000 p si
fc	1200 psi
fs	18000 psi
j	. 867
k	•400
n	10
v	60 psi
v	90 psi
u	150 psi
u	300 psi (where special anchorage
	is provided)
Piles	20 ton per square foot supported
Loading	H 20 S 16-44
Shear	13500 psi power driven rivets
Shear	10000 psi unfinished bolts

Design of Railing

Substantial railings shall be provided along each side of the bridge for the protection of traffic. The top of railing shall not be less than 3'-O" above the top of curb and when on a sidewalk, not less then 3'-O" above the top of the sidewalk. Railings shall contain no opening of greater width than eight (8) inches. Ample provision shall be made for inequality in the rate of movement of the railing and the supporting superstructure, due to temperature or erection conditions.

(M.S.H.D. Spec. 25 p. 10)

Railings shall be designed to resist a horizontal force of not less than 150 pounds per lineal foot, applied at the top of the railing, and a vertical force of not less than 100 pounds per lineal foot. For railings adjacent to the roadway, the bottom rail shall be designed for a horizontal force of 300 pounds per lineal foot of rail.

(M.S.H.D. Spec 35 p. 14)

Railings:

Bolts 3/4" Ø in single shear capacity 4420 # (for 10,000 psi steel) Load 300 x 8.167/2 = 1225 # Strap shear capacity (1 3/4 - 13/16)5/8 x 10000 = 5860 # Design of Railing

Using 50 pounds per lineal foot as the dead weight of the railing

(M.S.H.D. Standard Design of Railing)



Load: $304 \times 8.167/2 = 1240\#$

Bolts control as they have minimum capacity 1 (max) $17/8" + 3/8" = 2\frac{1}{4}"$

f	(horizontal)	$\frac{1225 \times 2.25 \times 6}{.625 \times (1.75)}$	86 50 psi
f	(vertical)	1225 x 2.25 x 6 6 x 1.75 x (6.25)	4050 psi
f	(total)		12700 psi
f	(allowable)		18000 psi

Design of Railing



Rail: Lower rail only considered (max. case) For the first computation only the two side channels are considered to simplify the computations. Horizontal bending $8.167 - 2 \ge 15/8 = 7.90$? $M = \le 1/8 = 300 \ge (7.90)^2 \ge 12 = 28100$ in. lbs. 8 $A = 2 \ge 1.46 = 2.92$ sq. in. e = 2.06 Ig $= 2 \ge .25 = .50^{13}$ I = Ae + Ig $= 2.92 \ge (2.06) + .50 = 12.89$ in. $f = Mc/I = 28100 \ge 2.5 = 5450$ psi

18000 psi allowable

Since the stresses are so low we may neglect the top channel of the lower railing in the design. This top channel would increase the strength at the railing which is already "330% over designed. Posts



Posts

The posts are able to bear a far greater load then that to which they are subjected. The actual stressin the steel of the post is only 46% of the allowable stress.

The railing and posts are greatly over designed, however, a large post of this greater size is obviously to produce a more massive appearance and greater architectural beauty throughout.

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Design of Sidewalk and Curb



Curbs shall be designed to resist a force of not less than five hundred (500) pounds per lineal foot of curb applied at the top of the curb.

(M.S.H.D. Spec. 36 p. 14)

The specified roadway loading shall apply to all sidewalks constructed without guard rails between the sidewalk and roadway to prevent encroachment of roadway loads.

As this sidewalk is fully supported the use of this part of the bridge serves only as an additional safety measure for pedestrians and as a more or less decorative measure. The only steel actually required is temperature steel with the other being more or less superfulous. -

Design of Concrete Slab



Calculate bending moment by A.A.S.H.O. art. 3.2.2 p. 138 Main reinforcing perpendicular to center line of roadway.

Distribution of wheel loads

For span 2-7 ft.

E = 0.6s + 2.5

Bending moment for freely supported span

 $M = 0.25 \times P/E \times s \times (100 + I + 10\%)$ for

longitudional forces)

Bending moment for continuous span

 $M = 0.2 \times P/E \times S \times (100 + I + 10\%)$ for

lonitudional forces)

Where,

- E = width of slab over which wheel load is distributed P = maximum wheel load in pounds
- s = distance between flanges plus ½ width of girder flanges

 $I = \frac{L + 20}{6L + 20}$

Design of Concrete Slab

The forces due to traction or sudden braking of vehicles shall be considered as longitudinal forces having a magnitude of 10% of the gross live load that can be placed in one traffic line.This load shall be assumed as acting in the direction of traffic movement and applied at the top of pavement.

(M.S.H.D. Spec. 38 p. 15)

Design

E = 0,6 x 5 + 2.5 = 5.5 ft. M = 0.25 x 16000/5.5 x 5 x 1.31 = 4760 ft. lbs. d = $\sqrt{M/Rb}$ = $\sqrt{(4760 x 12)/(208 x 12)}$ = 4.78 in.

For slabs the distance from the surface of the concrete either top or bottom, to the center of the nearest bar shall be not less than one and one-half times the diameter of the bar nor less than one and one-half inches. Thickness required: 4.78 + 1.50 = 6.28 in. Actual: 7.00 in. As = M/fsjd = (4760 x 12)/(18000 x 7/8 x 5.5) = .663 sq. in. required 1.000 sq. in. actual

Steel at bottom of slab for lateral distribution.

Percent of main steel required

100/15 = 100/15 = 44.8% (A.A.S.H.O. art. 3.2.2 p. 140) As = .663 x .448 = .296 sq. in./ft. required .

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Design of Concrete Slab

Slabs designed for bending moment in accordence with the foregoing shall be considered satisfactory in bond and shear.

(A.A.S.H.O. art. 3.2.2 (d) p. 140)

Diaphragm Design

The forces due to wind and lateral wibrations shall consist of a horizontal moving load equal to 30 pounds per square foot on $1\frac{1}{2}$ times the area of the structure as seen in elevation, including the floor system and railing and on one-half the area of all trusses and girders in excess of two in the span.

(M.S.H.D. Spec. 38 p. 15)

(a) Size, Rivets shall be of the size specified but generally shall be 3/4 inch or 7/8 inch in diameter.

(b) Pitch of Rivets, The minimum distance between centers of rivets shall be three times the diameter of the rivet but preferably shall be not less than the following:

For 3/4 inch diameter rivets - $2\frac{1}{2}$ inches

(M.S.H.D. Spec. 92 p. 39 - 40)

Diaphragms shall be provided at the third points of all I-beams spans of forty feet or more.

(M.S.H.D. Spec. 124 p. 48)

(a) Design, Lateral, longitudinal and transverse bracing shall be composed of angles or other shapes and shall have riveted connections.

(M.S.H.D. Spec. 123 p. 48) The end connections angles of floorbeams and stringers shall be not less than 3/8 inch in finished thickness. (M.S.H.D. S pec. 120 p. 47)

Diaphregm Design Area of structure as seen in elevation 7.833 x 59.582 468 square feet 1.5 x 468 702 square feet .5 x 6 x 3 x 57 <u>512 square feet</u> Total effective area 1214 square feet Moving load 30 x 1214 = 36420 pounds Area required End diaphragm 36420/18000 = 2.02 square inches required Area furnished

4" x 4" x 3/8" furnishes 2.86 square inches

The intermediate diaphragms meet all the necessary specifications provided by the M.S.H.D. for depth of web, size of angles, pitch of rivets, depth of hitchangles, and number of stiffeners. Girder Design

Main trusses and girders shall be space a sufficient distance apart center to center to be secure against overturning by the assumed lateral and other forces.

(M.S.H.D. Spec. 76 p.36)

For the calculation of stresses, span lengths shall be assumed as follows:

Beams and girders, distance between centers of bearings.

(M.S.H.D. Spec. 77 p.36)

Rolled beams shall be proportioned by the moments of inertia of their net sections.

(M.S.H.D. Spec. 80 p.36)

For structures with concrete slab floors without separate wearing surface, a minimum allowance of 20 pounds per square foot of roadway shall be made, in addition to the weight of any monolithically placed concrete wearing surface, to provide for future wearing surface.

(M.S.H.D. Spec. 30 p.12)

When provision is made for three or more lanes of traffic, the design shall provide for the following percentages of the simultaneous maximum loading of all lanes;

For four or more traffic lanes-----80%

(M.S.H.D. Spec. 33 p.13-14)

Using H-20 s 16-14 loading from appendix A AASHO page 229

Girder Design Dead Load: Slab 4.98 x 7.5/12 x 1 x 150 467#/' span Girder (assumed 36 WF 230) 230#/ span Future wearing surface 20 x 4.98 100#/' span 797#/' span Total Dead Load Dead Load Moment $M = wl^2/8 = (797 \times 12 \times 57)/8 = 3885000$ in. lbs. Live Load Moment $M = 385400 \times 12 \times .80 = 3600000$ Impact 3600000 x .21 = 757000 Total live load moment 4357000 in lbs. Total moment 8242000 in. lbs. Z required 8242000/18000 = 456 in.³

Deck plate girders with compression flanges continuously stayed in a concrete slab may have a depth not less than 1/20 span.

(M.S.H.D. Spec. 79 p. 36)(57.08 x 12)/20 = 34.2 in.

It is therefore necessary to use a 36 inch beam. Z furnished by 36 WF 230 is 835.5 in. Girder Design

Check deflection



deflection @ midpoint $(x 1/2) = \frac{Pbx (1 - b - x)}{6EI1}$

 $\frac{16(16.85 \times 12)(28.54 \times 12)(467000-41000-117500)}{6 \times 30 \times 10 \times 14990 \times (57.08 \times 12)} = .186 \text{ in.}$

$$\frac{16(26.21 \times 12)(28.54 \times 12)(467000-99000-117500)}{6 \times 30 \times 10 \times 14990 \times (57.08 \times 12)} = .235 \text{ in.}$$

$4(12.21 \times 12)(28.54 \times 12)(467000-21500-117500)$	=	.038	in.
6 x 30 x 10 x 14990 x (57.08 x 12)		•••••	
Total L.L. Deflection		•459	in.
Impact (21%)		.096	in.
Total Deflection		•555	in.
Live load plus impact deflection 1/1000 span 1	lengt	h	

Allowable deflection $(57.08 \times 12)/1000 = .684$ inches

A 36 WF 230 beam is the smallest beam which does not exceed the allowable deflection.

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Retaining walls, abutments and structures built to retain fills shall be designed to resist pressures determined in accordance with the "Rankine" theory of pressure distribution in noncohesive granular material, provided that no structure shall be designed for an equivalent fluid pressure of less than 30 pounds per square foot.

Loading

Dead load (superstructure) Total concrete 104/2 x 27 x 150 210500 pounds Total steel 144100 x 불 **72050 poun**d**s** Total 282550 pounds Out to out of wings 86.875 Then $28 \ge 550 \times 1/86.875 = 3250 \#/!$ Live load One lane reaction 60400 # Total live load $60400 \times 4 \times .8 = 193000$ pounds Then 193000 x 1/86.875 = 2220 #/!Surcharge 0" Face to face of rail 45' 210 #/1 Then $(45 \times 4)0)/86.875 =$ Trial section: 21 0" Toe projection 21 4" Wall 21 8" Heel projection



	Overturning		Thrust	Moment
P)	342 x 10.25/2	=	1750 # x 3.42 =	6000 1 #
P)	138 x 10.25	=	1415 # x 5.12 =	72401#
		М	(OI) = M(OIII) =	13420 ' #
P)	70 x 10.25	=	717 # x 5.12 =	<u> </u>
			M(OII) =	16910 ' #

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	Stability			Weight		Moment
a)	7 x 2.5 x 150			2620 # x	3.50 =	9180 ' #
b)	7.75 x 2.33 x 150			2710 # x	3.17 =	860 0 1#
c)	7.75 x 2.67 x 100			2070 # x	5.66 =	117201#
d)	2.67 x 4.15 x 100			<u>1110 #</u> x	5.66 =	6270 '#
		W(I)	=	8 510 #	M(SI) =	35770 ' #
	Dead Load			<u>3250 #</u> x	3.17 =	<u>10600'#</u>
		W(IV)	=	11760 # x	M(SIV)=	46370 ' #
	Surcharge 2.67 x	2.1	-	56 1 # x	5.66 =	31701#
	-	W(II)	=	12321 #	M(II) =	495 40 ' #
		W(IV)	Ξ	1 1760 #	M(SIV) =	46370 ' #
	Live Load			<u>2220 #</u> x	3.17 =	70401#
		W(III)	2	139 80 #	M(SIII)=	= 53410'#

Case I

No 1	load	or	live	load	surchage
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M(I)	225301#	R(I)	=	22530/8510 = 2.65'	OK
M(OI)	<u>13240'#</u>				
M(SI)	357701#				

Case II

Superstructure dead load and live load surcharge

M(SI I)	49540 '#				
M(OII)	<u>16910'#</u>				
M(II)	326301#	R(II)	Ħ	32630/12321 = 2.65	OK

Case III

Superstruct	ure	dead	load	and	live	e load,	no	surcharg	çe
M(SIII)	5341	.01#							
M(OIII)	<u>1324</u>	10 '#							
M(III)	4017	'0 ' #	R(I]	[])	= 4	10 1 70/13	3 9 80)= 2.871	OK

Case IV

Superstructure dead load, no live load or surcharge R(IV) = 46370/11760 = 3.95 OK Note: Case IV assumes that theearth exerts no horizontal force against the abutment wall.

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Case III	<u>13980 x 7</u>	+	<u>13</u>	980 x '	7_x	.06 X	1.33
	3			10	0.68	3	
	32500 - 7	30	>	31770	#	OK	Front row
	32500 + 14	70	=	3 3970	#	OK	Back row

Case	IV	11760 1	<u>(7</u> +	11760 x 7	x 1.12 x 1	1.33	
		3		10.68			
		27400	- 11500	= 15900	# OK	Front row	
		27400	+ 23000	= 50400	# Over:	stressed 26%	
		Note: (Case IV,	back row f	s overstre	essed by 26%	
		ĩ	out this	does not d	consider th	ne horizontal	
		t	force exerted by the earth.(M.S.H.D. allows 33% overstress in this case.)				
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Reinforcement



As = $M/fsjd = 3625 \times 12$ = .132 sq. in. $18000 \times 7/8 \times 21$ use 3/4" Ø bars@ 1'-0" centers As = .44 sq. in. Eo = 2.4 in. $p = .44/12 \times 21 = .00175$ j - .944 k = .169fs = <u>3625 x 12</u> = 4440 psi .44 x .944 x 21 $fc - fsk/n(1-k) = 4440 \times .169$ = 91 psi 8.31 v = V/bjd= **8000 3**3 p**si** 2 12 x .944 x 21 u = V/Eojd = 8000 2 165 psi 2.4 x .944 x 21

(allowable)

300 psi

Heel: Case IV (bottom steel)



Shear

3020#

Moment = 7200 x 14 - 4180 × 16 - 34000 "# Use 3/4" Ø bars @ 2'-0" centers from every other toe bar As = .22 sq. in. Eo = 1.2" np = .0088 $k = \sqrt{2pn} + (pn)^2 - pn = .124$ j = .959 fs <u>34000</u> = 7680 psi OK .22 x .959 x 21 fc = 7680 x .124 2 110 psi OK 8.76 302**0** ▼ = . 12.5 psi OK = 12 x .959 x 21 u <u>3020</u>

 $u = \frac{3020}{1.2 \times .959 \times 21} = 125 \text{ psi}$ OK

Heel: Case II (top steel)

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26200"#

As $= \frac{26200}{18000 \times 7/8 \times 26} = .06$ " Use 3/4" \notin @ 2'-0" centers All unit stresses are OK by inspection. Wall:



Use 3/4" Ø @ 2'-0" centers



Wing Wall

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Overturning	Thrust	Moment
383 x 11.5 x 1/2	2200 # x 3.83 =	<u>84201#</u>
	M(0I) =	8 4 20 ' #
103 x 7.69 x 불	396 # x 2.56 •	<u>1013'#</u>
	M(OII) =	943 21#

	Stabilizing	Weight	Moment
a)	2.5 x 7 x 150	2620 # x 3.50	= 92001#
b)	1.5 x 7.75 x 150	1745 # x 2.75	= 4 800 '#
c)	7.75 x .83 x 150 $x\frac{1}{2}$	482 # x 3.78	= 1825'#
d)	7.75 x 2.67 x 100	2070 # x 5.6 7	= 11750'#
e)	7.75 x .83 x 100 x ½	321 # x 4.05	= 1300'#
f)	1.25 x 2.67 x 100 x ½	167 # x 6 .11	= 1020'#
g)	3.79 x 2 x 100	<u>758 #</u> x 1.00	= <u>7581#</u>
		W = 8163 # M(SI'I	[') =

306531#

Wing Wall Stability:

Case I'

No live load surcharge M(SI') 30653'# M(OI') <u>8420'#</u> M(I') 22233'# $R(I') = \frac{22233}{8163} = 2.72'$ OK

Case II'

With live load surcharge M(SII') 30653'# M(OII') <u>9432'#</u> M(II') 21221'# R(II') = <u>21221</u> = 2.58' OK

Case IV'

No earth thrust

$$R(IV') = \frac{30653}{8163} = 3.75'$$
 OK

Wing Wall Reinforcing Steel:

By a comparison of main wall and wing wall loads it is seen that the main wall is designed for a more severe condition of loading than would come on the wing. Further, it can also be seen that the same steel is used in the wall of the wing as that used in the wall of the main wall; therefore, the stresses in the wing wall are OK by inspection.

Conclusion

As the thesis progressed remarks were inserted in their related sections; however, it may be well to call attention to several items which are of standard design. Such items as the railing, posts, curb, concrete slab, and diaphragms are of Michigan State Highway Department standard; therefore, it will be noted that because they are designed for the most severe conditions they are overdesigned for this structure. The Highway Department through years of experience has found that the labor saving in design work far overshadows that saving in material if each item is to be designed separately.

As an overall conclusion it may be said that the entire structure is adequately designed and the above named sections are well overdesigned.

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