

ANALYSIS OF THE SUPERSTRUCTURE
OF HIGHWAY BRIDGE

Thesis for the Degree of B. S.
MICHIGAN STATE COLLEGE

Roy L. Colby Jr.
1941

**SUPPLEMENTARY
MATERIAL**
IN BACK OF BOOK



Analysis of the Superstructure
of Highway Bridge

A Thesis Submitted to

The Faculty of
MICHIGAN STATE COLLEGE
of
AGRICULTURE AND APPLIED SCIENCE

by

Roy Lynn Colby Jr.

Candidate for the Degree of
Bachelor of Science

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THESIS

Cap. 1

Analysis of the Super Structure of a
Bridge located in the west part of the busi-
ness section in Owosso, Michigan, on W 21.

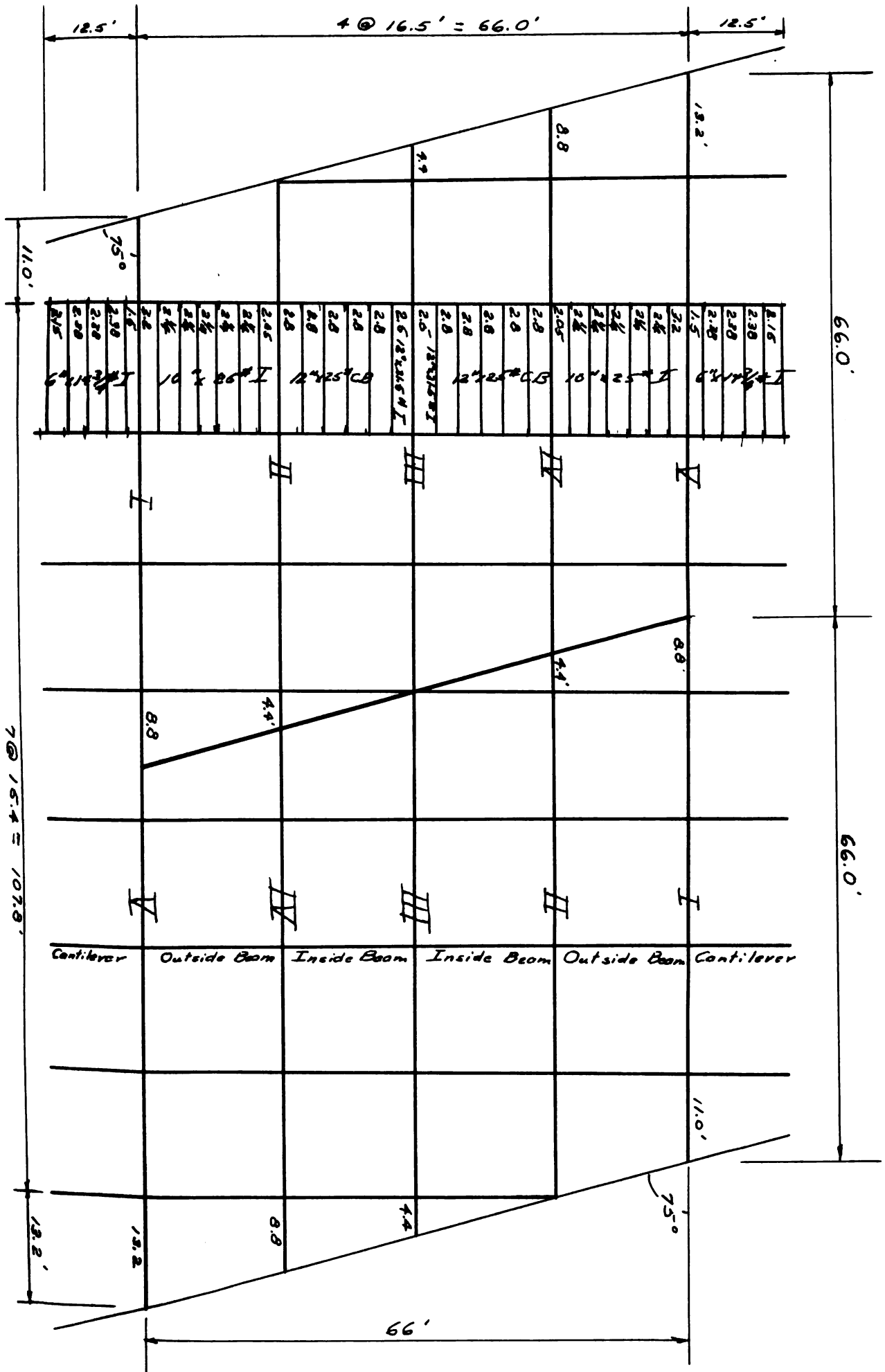
The bridge has two spans at 66 ft.
supported on masonry abutments and a mason-
ry pier at the center. It is on a skew of
75 degrees. There are 5 plate girder at
10.5 ft. center to center and built up beams
at 90 degrees with the girder. The beams
are connected on directly opposite sides
of the girders. The stringers, which are
I Beams, along with the girders support the
6 in. reinforced concrete deck. The clear
distance from curb to curb is 64 ft. There
is a 12 ft. sidewalk of 5 in. reinforced
concrete slab supported by a cantilever beam
on each side of the roadway. The bridge has
just recently been redecked and possible
other changes took place at that time.

Assumptions:

Girders-----	Freely supported
Beams-----	Continuous
Stringers-----	Freely supported
Concrete Slab-----	Continuous

The numbers in parenthesis used throughout the thesis correspond to the specification numbers in the book of specifications used for Design of Highway Bridges adopted by the Michigan State Highway Department in January, 1938.

The fiber stress in the specification is 18000 ψ /sq. in., but in checking old bridges the Michigan State Highway Department use 16000 in determining safe loading.



INDEX

	pages
Concrete Slab----	1 to 15
Stringers-----	16 to 21
Beams-----	22 to 43
Cantilever Beam-----	44 to 53
Girders-----	54 to 91

CONCRETE SLAB

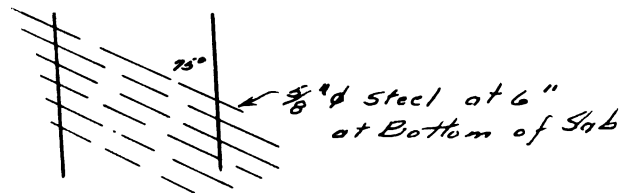
Sidewalk Concrete Slab

Concrete Slab between 6 in. ϕ 14.71 # I spaced at 2 ft. 4 in.
 Flange wd. 3.45 in.

$$\text{Clear Dis. } 3.38 - \frac{3.45}{12} = 2.09 \text{ ft.}$$

$$(55) \quad 2.09 + \frac{5}{12} = 2.5 \text{ ft.}$$

2.5 is less than 2.6; therefore span length
 is 2.38 ft.



$$\text{Dead Load } 150 \text{ #/ft}^3 \text{ concrete} \\
\frac{5}{12} 150 = 62.5 \text{ #/ft.}$$

$$(34) \text{ Live Load } 100 \text{ #/sq. ft.}$$

$$\text{Total lbs. per ft. } 100 + 62.5 = 162.5 \text{ #/ft.}$$

Total Bending Moment

$$M_{\text{max}} \text{ BM} = \frac{w l^2}{10} = \frac{162.5 \times 2.38^2}{10} = 92.3 \text{ ft. lbs.}$$

Total Shear

$$M_{\text{max}} V = \frac{w l}{2} = \frac{162.5 \times 2.38}{2} = 193.5 \text{ #}$$

Check d

$$d = \sqrt{\frac{M}{K b}} = \sqrt{\frac{92.3 \times 12}{173 \times 12}} = 0.73 \text{ in.}$$

supplied d at center of span
 $d = 5 - 1 = 4 \text{ in.}$
 supplied d at supports
 $d = 1 \frac{1}{2} \text{ in.}$

Steel-5/8 in. ϕ spaced at 6 in. on 75 degree angle
 $n = 0.0111$ steel ration needed

$$A_s = \frac{.6136}{\sin 75} = 0.635 \text{ sq. in.}$$

$$\text{at supports } n = \frac{.635}{1.5 \times 12} = .0353 \text{ supplied} \\
\text{needed } .0111$$

$$\text{at center of span } n = \frac{.635}{3.5 \times 12} = .0151 \text{ supplied}$$

Sidewalk Concrete Slab

Concrete Slab between 6 in. C 14.74 # I spaced at 2 ft. 4 1/2 in.

Shear

$$v = \frac{V}{7/8 b d} = \frac{193.5}{7/8 \cdot 12 \cdot 1.5} = \frac{12.26 \text{ #/sq. in.}}{\text{allowable } 50}$$

Bond

$$u = \frac{V}{7/8 o d} = \frac{193.5}{7/8 \cdot 4.07 \cdot 1.5} = \frac{36.2 \text{ #/sq. in.}}{\text{allowable } 125}$$

CONCRETE SLAB OF ROADWAY

25000 # Concrete

$$f_s = 18000 \text{ #/sq. in.}$$

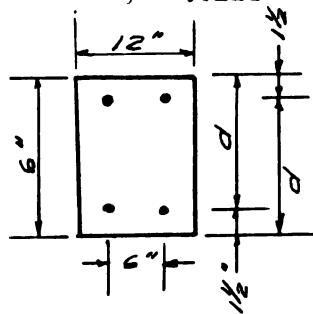
$$f_c = 1000 \text{ #/sq. in.}$$

$$n = 12$$

$$K = 173 \quad \text{used in formulae} \quad d = \sqrt{\frac{M}{K \cdot b}}$$

$$j = 0.871 \quad \text{say } 7/8$$

$$r = 0.0111 \quad \text{ratio of steel to concrete cross section}$$



Dis. d supplied equals $6 - 1.5 = 4.5$ in.

Steel-----5/8 in. Φ spaced at 6 in. on angle of 75 degrees
Top & Bottom

$$A_s = \frac{0.6136}{\sin 75} = 0.635 \text{ sq. in.}$$

$$r = \frac{A_s}{b \cdot d} = \frac{0.635}{4.5 \cdot 12} = 0.01174 \text{ supplied} \quad \text{needed } 0.011$$

Dead Load of Slab

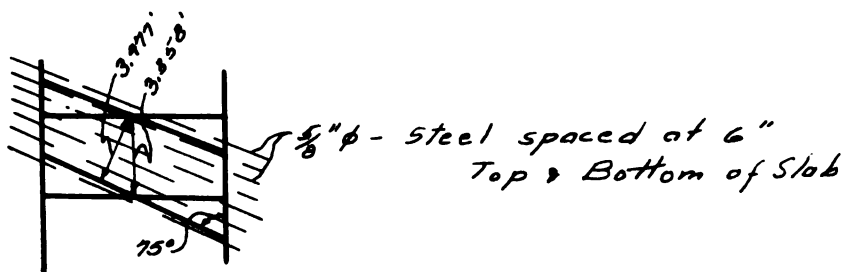
$$\begin{aligned} 6 \text{ in. Concrete} &= 150 \text{ #/ft}^3 \\ 6/12 \cdot 150 &= 75 \text{ #/ft.} \end{aligned}$$

$$\begin{aligned} \text{Wearing Surface} &= 25 \text{ #/ft}^2 \\ 25 \cdot 1 &= 25 \text{ #/ft.} \\ w &= 100 \text{ #/ft.} \end{aligned}$$

Concrete Slab between the Second Girder and the first 10 in. C25 # Stringer
 10 in. C 25 # IBM - flange wd. of 4.66 in.
 center to center dis. 2ft. - 0 1/2 in. or 2.04 ft.
 wd. of flange of girder 1.19 ft.

$$(35) \quad 1.25 + .5 = 1.75 \text{ ft.}$$

1.75 is less than 2.04 ft.; therefore Span Length is 1.75 ft.



(41) Effective Width

$$\begin{aligned} \text{eff. wd.} &= 0.7 s + 2 && \text{on 75 degree angle} \\ s &= \text{center to center of supports on 75 degree angle} \\ s &= \frac{2.04}{\sin 75} = 2.11 \text{ ft.} \end{aligned}$$

$$\text{eff. wd.} = 7 \cdot 2.11 + 2 = 3.477 \text{ ft.} \quad \text{on 75 degree angle}$$

$$\text{eff. wd.} = 3.477 \sin 75 = 3.358 \quad \text{on 90 degree angle}$$

Max Live Load Bending Moment H20 Loading
 wheel load = 16000 # 20 in. wd.

$$\text{Load on a ft. of slab} = \frac{16000}{3.358} = 4770 \text{ #}$$

$$\text{Continuity} = 0.8$$

$$\text{LLBM} = .8(2385 \cdot 975 - \frac{4770 \cdot 5}{2 \cdot 12}) = 8728 \text{ ft. lbs.}$$

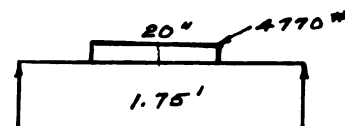
$$(37) \text{Impack} = \frac{L+20}{6L+20} = \frac{1.75+20}{6 \cdot 1.75+20} = 71.4 \%$$

$$\text{LLBM Imp.} = 872.8 \cdot 71.4\% = 1495 \text{ ft. lbs.}$$

Max. Dead Load Bending Moment $w = 100 \text{ #/ft.}$

$$\text{DLBM} = \frac{w l^2}{10} = \frac{100 \cdot 1.75^2}{10} = 30.7 \text{ ft. lbs.}$$

$$\text{Total BM} = 30.7 + 1495 = 15257 \text{ ft. lbs.}$$



Concrete Slab between the Second Girder and the first 10 in. C 25 # Stringer

Check d

$$d = \sqrt{\frac{M}{K b}} = \sqrt{\frac{15267.12}{173.12}} = 9.37 \text{ in. supplied 4.5}$$

H20 Live Load Shear H20 Loading

$$LLV = \frac{4770 (1.75 - \frac{20}{24})}{1.75} = 2500 \#$$

$$LLV + Imp. = 2500 (1.4) = 4280 \#$$

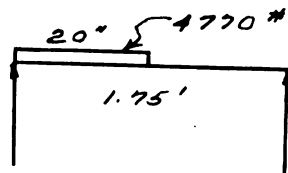
Dead Load Shear

$$DLV = \frac{w l}{2} = \frac{100 (1.75)}{2} = 87.5 \#$$

$$\text{Total Shear} = 4280 + 87.5 = 4367.5 \#$$

$$\text{Shear } v = \frac{V}{7/8 d b} = \frac{4367.5}{7/8 (4.5) 12} = 92.3 \#/\text{sq. in.} \quad \text{allowable } 75$$

$$\text{Bond } u = \frac{V}{7/8 o d} = \frac{4367.5}{7/8 (4.07) 4.5} = 272.3 \#/\text{sq. in.} \quad \text{allowable } 250$$



H15 Live Load Shear H20 Loading

Wheel Load = 12000 15 in. wd.
Eff. wd. = 3.358 ft.

$$\text{Load on } l \text{ ft. of slab} = \frac{12000}{3.358} = 3580 \#$$

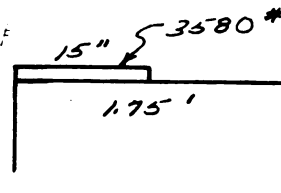
$$LLV = \frac{3580 (1.75 - \frac{15}{24})}{1.75} = 2300 \#$$

$$LLV + Imp. = 2300 (1.4) = 3942 \#$$

$$\text{Total Shear} = 3942 + 87.5 = 4029.5 \#$$

$$\text{Shear } v = \frac{V}{7/8 b d} = \frac{4029.5}{7/8 (12) 4.5} = 85.2 \#/\text{sq. in.} \quad \text{allowable } 75$$

$$\text{Bond } u = \frac{V}{7/8 o d} = \frac{4029.5}{7/8 (4.07) 4.5} = 251 \#/\text{sq. in.} \quad \text{allowable } 250$$

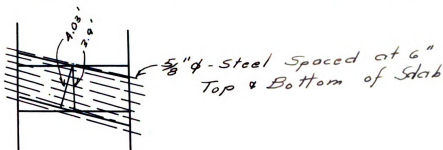


Concrete Slab between 12 in. @ 25# I Bm. spaced 2ft.-9in.
 12 in. @ 25 # I Bm.-Flange wd. of 6.5 in.
 center to center dis. 2.8 ft.

$$\text{Clear Dis. } 2.8 - \frac{6.5}{12} = 2.25 \text{ ft.}$$

$$(55) 2.25 + .5 = 2.75 \text{ ft.}$$

2.75 is ~~less~~ than 2.8; therefore Span Length is 2.75 ft.



(41) Effective Width

$$\text{eff. wd.} = 0.7 s + 2$$

s = center to center of supports on 75 degree angle

$$s = \frac{2.8}{\sin 75} = 2.9 \text{ ft.}$$

$$\text{eff. wd.} = .7 \cdot 2.9 + 2 = 4.03 \text{ ft. on 75 degree angle}$$

$$\text{eff. wd.} = 4.03 \sin 75 = 3.9 \text{ ft. on 90 degree angle}$$

Max. LLBM

H2O Loading

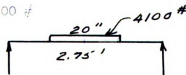
wheel load = 16000 #

20 in. wide

$$\text{Load on a ft. slab} = \frac{16000}{3.9} = 4100 \text{ #}$$

$$\text{Continuity} = 0.8$$

$$\text{LLBM} = .8 \left(2050 \cdot 1.375 - \frac{4100 \cdot 5}{12 \cdot 2} \right) = 1572.8 \text{ ft. lbs.}$$



$$(37) \text{ Impact} = \frac{L + 20}{6 L + 20} = \frac{2.9 + 20}{6 \cdot 2.9 + 20} = 61.2 \%$$

$$\text{LLBM} + \text{Imp.} = 1572.8 \cdot 1.612 = 2540 \text{ ft. lbs.}$$

Max. DLBM $w = 100 \text{ #/ft.}$

$$\text{DLBM} = \frac{w l^2}{10} = \frac{100 \cdot 2.75^2}{10} = 75.7 \text{ ft. lbs.}$$

$$\text{Total BM} = 2540 + 75.7 = 2615.7 \text{ ft. lbs.}$$

Concrete Slab between 12 in. @ 25" I Em. spaced 2 ft.-9 in.

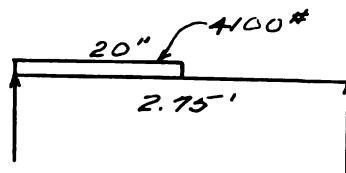
Check d

$$d = \sqrt{\frac{BM}{K b}} = \sqrt{\frac{2615.7 \text{ lb}}{173 \text{ lb}}} = 3.79 \text{ in. supplied 4.5 in.}$$

H20 Live Load Shear

H20 Loading

$$LLV = \frac{4100}{2.75} \left(2.75 - \frac{20}{2 \cdot 12} \right) = 2950 \text{ #}$$



$$LLV + Imp. = 2950 + 161.25 = 4600 \text{ #}$$

Dead Load Shear

$$DLV = \frac{wl}{2} = \frac{100 \cdot 2.75}{2} = 137.5 \text{ #}$$

$$\text{Total } V = 4600 + 137.5 = 4737.5 \text{ #}$$

$$\text{Shear } v = \frac{V}{7/8 b d} = \frac{4737.5}{7/8 \cdot 4.5 \cdot 12} = 100 \text{ #/sq. in. allowable 75}$$

$$\text{Bond } u = \frac{V}{7/8 o d} = \frac{4737.5}{7/8 \cdot 4.07 \cdot 4.5} = 395 \text{ #/sq. in. allowable 250}$$

H15 Live Load Shear

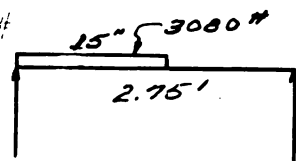
H15 Loading

$$\text{Wheel Load} = 12000 \text{ #} \quad 15 \text{ in. wd.}$$

$$\text{Eff. wd.} = 3.9 \text{ ft.}$$

$$\text{Load on a ft. of slab} = \frac{12000}{3.9} = 3080 \text{ #}$$

$$LLV = \frac{3080}{2.75} \left(2.75 - \frac{15}{2 \cdot 12} \right) = 3340 \text{ #}$$



$$LLV + Imp. = 3340 + 161.25 = 3840 \text{ #}$$

$$\text{Total } V = 3840 + 137.5 = 3977.5 \text{ #}$$

$$\text{Shear } v = \frac{V}{7/8 b d} = \frac{3977.5}{7/8 \cdot 4.5 \cdot 12} = 84 \text{ #/sq. in. allowable 75}$$

$$\text{Bond } u = \frac{V}{7/8 o d} = \frac{3977.5}{7/8 \cdot 4.07 \cdot 4.5} = 248 \text{ #/sq. in. allowable 250}$$

Concrete Slab between First Girder to First Stringer

10 in. @ 25 # I Flange wd. of 4.66 in.

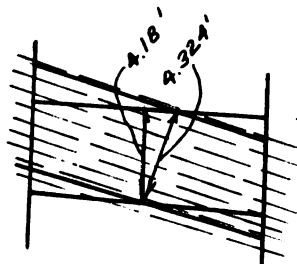
center to center dis. 3 ft. 2 1/2 in.

wd. of flange of girder 1.19 ft.

$$\text{Clear dis. } 3.21 - \frac{(1.19 + 4.66/12)}{2} = 2.42 \text{ ft.}$$

$$(55) \quad 2.42 + .5 = 2.92 \text{ ft.}$$

2.92 is less than 3.21; therefore Span Length is 2.92 ft.



8" @ Steel spaced at 6"
Top & Bottom of Slab

(41) Effective Width

$$\begin{aligned} \text{eff. wd.} &= 0.7 s + 2 && \text{on 75 degree angle} \\ s &= \text{center to center of supports on 75 degree angle} \\ s &= \frac{3.21}{\sin 75} = \frac{3.21}{.966} = 3.32 \text{ ft.} \end{aligned}$$

$$\begin{aligned} \text{eff. wd.} &= 7 \cdot 3.32 + 2 && \text{on 75 degree angle} \\ &= 4.324 \text{ ft.} \end{aligned}$$

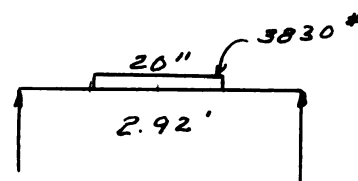
$$\text{eff. wd.} = 4.324 \sin 75 = 4.18 \text{ ft. on 90 degree angle}$$

Max. Live Load Bending Moment ~~H20~~ Loading
wheel load = 16000 # 20 in. wd.

$$\text{Load on a ft. slab} = \frac{16000}{4.18} = 3830 \text{ #}$$

$$\text{Continuity} = 0.8$$

$$\text{LLBM} = .8 (1215 \cdot 1.4 - \frac{3830 \cdot 5}{2 \cdot 12}) = 1600 \text{ ft. lbs.}$$



$$(57) \text{ Impact} = \frac{L + 20}{6 L + 20} = \frac{2.92 + 20}{6 \cdot 2.92 + 20} = 61 \%$$

$$\text{LLBM} + \text{Imp.} = 1600 \cdot 1.61 = 2575 \text{ #}$$

Max. Dead Load Bending Moment $w = 100 \text{ #/ft.}$

$$\text{DLBM} = \frac{w L^2}{10} = \frac{100 \cdot 2.92^2}{10} = 85.3 \text{ ft. lbs.}$$

$$\text{Total BM} \quad 2575 + 85.3 = 2660.3 \text{ ft. lbs.}$$

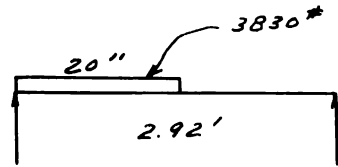
Concrete Slab between First Girder to First Stringer

Check d

$$d = \sqrt{\frac{M}{K b}} = \sqrt{\frac{2660.3 \text{ lb}}{173 \text{ lb}}} = 3.92 \text{ in.} \quad \text{supplied 4.5}$$

120 Live Load Shear H20 Loading

$$LLV = \frac{3830}{2.92} \left(2.92 - \frac{20}{2 \times 12} \right) = 2740 \text{ #}$$



$$LLV + Imp. = 2740 \times 161\% = 4410 \text{ #}$$

Dead Load Shear

$$DLV = \frac{w l}{2} = \frac{100 \times 2.92}{2} = 146 \text{ #}$$

$$\text{Total Shear} = 146 + 4410 = 4556 \text{ #}$$

$$\text{Shear } v = \frac{V}{7/8 b d} = \frac{4556}{7/8 \times 12 \times 4.5} = 96.5 \text{ #/sq. in.} \quad \text{allowable 75}$$

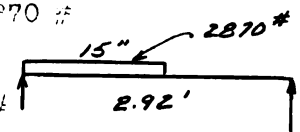
$$\text{Bond } u = \frac{V}{7/8 a c} = \frac{4556}{7/8 \times 4.07 \times 4.5} = 284.2 \text{ #/sq. in.} \quad \text{allowable 250}$$

H15 Live Load Shear H15 Loading

Wheel Load = 12000 # 15 in. wd.
Eff. wd. 4.18 ft.

$$\text{Load on 2 ft. of slab} = \frac{12000}{4.18} = 2870 \text{ #}$$

$$LLV = \frac{2870}{2.92} \left(2.92 - \frac{15}{2 \times 12} \right) = 2250 \text{ #}$$



$$LLV + Imp. = 2250 \times 161\% = 3625 \text{ #}$$

$$\text{Total Shear} = 3625 + 146 = 3771 \text{ #}$$

$$\text{Shear } v = \frac{V}{7/8 d b} = \frac{3771}{7/8 \times 4.5 \times 12} = 79.7 \text{ #/sq. in.}$$

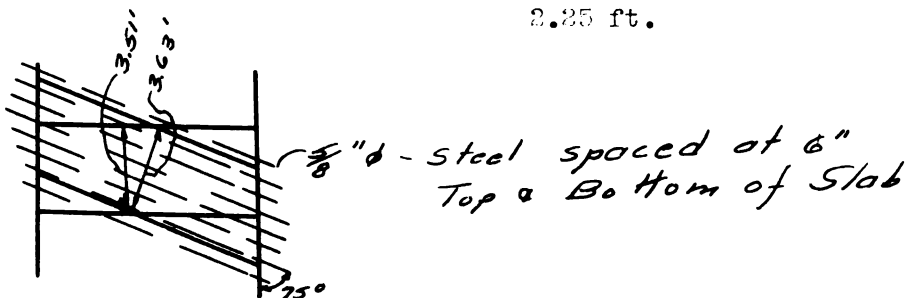
$$\text{Bond } u = \frac{V}{7/8 c d} = \frac{3771}{7/8 \times 4.07 \times 4.5} = 235 \text{ #/sq. in.} \quad \text{allowable 250}$$

Concrete Slab between 10 in. @ 25 I Beam spaced 2 ft. 3 in.
 10 in. @ 25 I Bm.-Flange wd. of 4.66 in.
 center to center dis. 2.25 ft.

$$\text{Clear Dis.} = 2.25 - \frac{4.66}{12} = 1.86 \text{ ft.}$$

(55) $1.86 + .5 = 2.36 \text{ ft.}$

2.36 is more than 2.25; therefore Span Length is
 2.25 ft.



(41) Effective Width

$$\begin{aligned} \text{eff. wd.} &= 0.7 s + 2 \quad \text{on 75 degree angle} \\ s &= \text{center to center of supports 75 degree angle} \\ s &= \frac{2.25}{\sin 75} = 2.33 \text{ ft.} \end{aligned}$$

$$\text{eff. wd.} = .7 \cdot 2.33 + 2 = 3.63 \text{ ft. on 75 degree angle}$$

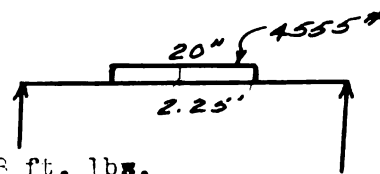
$$\text{eff. wd.} = 3.63 \sin 75 = 3.51 \text{ ft. on 90 degree angle}$$

Max. LLBM #20 Loading

$$\begin{aligned} \text{wheel load } 16000 & \quad 20 \text{ in. wide} \\ \text{Load on a ft. slab} & \quad \frac{16000}{3.51} = 4555 \text{ lb} \end{aligned}$$

$$\text{Continuity} = 0.8$$

$$\text{LLBM} = .8 (2277.5 \cdot 1.125 - \frac{4555 \cdot 5}{2 \cdot 12}) = 1288 \text{ ft. lbs.}$$



(37) Impact $= \frac{L + 20}{6 L + 20} = \frac{2.25 + 20}{6 \cdot 2.25 + 20} = 66.4\%$

$$\text{LLBM} + \text{Imp.} = 1288 \cdot 66.4\% = 2145 \text{ ft. lbs.}$$

Max. DLBM $w = 100 \text{ \#/ft.}$

$$\text{DLBM} = \frac{w l^2}{10} = \frac{100 \cdot 2.25^2}{10} = 50.75 \text{ ft. lbs.}$$

$$\text{Total BM} = 50.75 + 2145 = 2195.75 \text{ ft. lbs.}$$

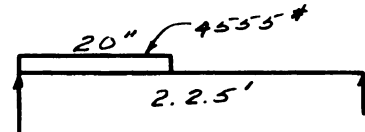
Concrete Slab between 10 in. @ 25 I Beam spaced 2 ft. 3 in.

Check d

$$d = \sqrt{\frac{BM}{K b}} = \sqrt{\frac{2195.75 \text{ lb}}{173 \text{ lb}}} = 3.58 \text{ in. supplied 4.5 in}$$

H20 Live Load Shear H20 Loading

$$LLV = \frac{4555}{2.25} (2.25 - \frac{20}{12}) = 3870 \#$$



$$LLV + Imp. = 3870 \times 166.4\% = 4780 \#$$

Dead Load Shear

$$DLV = \frac{w l}{2} = \frac{100 \times 2.25}{2} = 112.5 \#$$

$$\text{Total Shear} = 4780 + 112.5 = 4892.5 \#$$

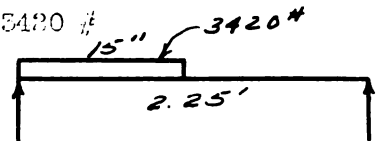
$$\text{Shear } v = \frac{V}{7/8 b d} = \frac{4892.5}{7/8 \times 4.5 \times 12} = 103.2 \text{ #/sq. in. allowable } 75$$

$$\text{Bond } u = \frac{V}{7/8 \times 4.07 \times 4.5} = 263 \text{ #/sq. in. allowable } 250$$

H15 Live Load Shear H15 Loading
Wheel Load = 12000 # 15 in. wd.
Eff. wd. = 3.51 ft.

$$\text{Load on a ft. of slab} = \frac{12000}{3.51} = 3420 \#$$

$$LLV = \frac{3420}{2.25} (2.25 - \frac{15}{12}) = 2470 \#$$



$$LLV + Imp. = 2470 \times 166.4\% = 4110 \#$$

$$\text{Total } V = 4110 + 112.5 = 4222.5 \#$$

$$\text{Shear } v = \frac{V}{7/8 b d} = \frac{4222.5}{7/8 \times 12 \times 4.5} = 89 \text{ #/sq. in. allowable } 75$$

$$\text{Bond } u = \frac{V}{7/8 \times 20 \times d} = \frac{4222.5}{7/8 \times 4.07 \times 4.5} = 263 \text{ #/sq. in. allowable } 250$$

Concrete Slab between Center Girder and first Stringer

12 in. $\times$ 31.5 I BM - Flange wd. of 5 in.

center to center dis. 2.5 ft.

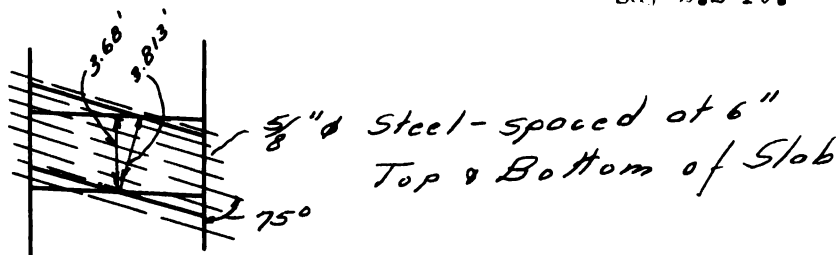
wd. of flange of girder 14 1/4 in. or 1.19 ft.

$$\text{Clear Dis. } 2.5 - \frac{(1.19 \times 5/12)}{2} = 1.695 \text{ ft.}$$

$$(55) \quad 1.695 + 0.8 = 2.195 \text{ ft.}$$

2.195 is less than 2.5 ; therefore Span Length is 2.195

say 2.2 ft.



(41) Effective Width

$$\text{eff. wd.} = 0.7 s + 2 \quad \text{on } 75 \text{ degree angle}$$

s = center to center of supports 75 degree angle

$$s = \frac{2.5}{\sin 75} = 2.59 \text{ ft.}$$

$$\text{eff. wd.} = 7 \times 2.59 + 2 = 3.813 \quad \text{on } 75 \text{ angle}$$

$$\text{eff. wd.} = 3.83 \sin 75 = 3.62 \quad \text{on } 90 \text{ degree angle}$$

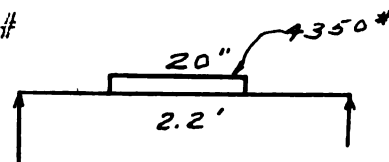
Max. LLBM HFO Loading

wheel load = 16000 # 20 in. wide

$$\text{Load on a ft. slab} = \frac{16000}{3.68} = 4350 \#$$

Continuity = 0.8

$$\text{LLBM} = .8 \left(2175 \times 1.1 + \frac{4350}{2} \times \frac{5}{12} \right) = 1190 \text{ ft. lbs.}$$



$$(37) \text{ Impact} = \frac{1+20}{6L+20} = \frac{2.2+20}{6 \times 2.2+20} = 66.9 \%$$

$$\text{LLBM} + \text{Imp} = 1190 \times 66.9 \% = 1987 \text{ ft. lbs.}$$

Max. DLBM $w = 100 \#/\text{ft.}$

$$\text{DLBM} = \frac{wl^2}{10} = \frac{100 \times 2.2^2}{10} = 48.5 \text{ ft. lbs.}$$

$$\text{Total BM } 1987 + 48.5 = 2035.5$$

Concrete Slab between Center Girder and first Stringer

Check d

$$d = \sqrt{\frac{B_u}{K b}} = \sqrt{\frac{2035.5 \text{ lb}}{173 \text{ lb/in}^2}} = 3.425 \text{ in. supplied } 4.5 \text{ in.}$$

H20 Live Load Shear H20 Loading

$$LLV = 4350 \left(\frac{2.2 - 20}{8 \text{ ft}} \right) = 2700 \text{ #}$$

$$LLV + Imp. = 2700 \text{ lb} \times 166.9\% = 4500 \text{ #}$$

Dead Load Shear

$$DLV = \frac{w l}{2} = \frac{100 \text{ lb/ft} \times 2.2 \text{ ft}}{2} = 110 \text{ #}$$

$$\text{Total Shear } 4500 + 110 = 4610 \text{ #}$$

$$\text{Shear } v = \frac{V}{7/8 b d} = \frac{4610}{7/8 \times 4.5 \text{ ft} \times 12 \text{ in}} = 97.5 \text{ #/sq. in. allowable } 75$$

$$\text{Bond } u = \frac{V}{7/8 o d} = \frac{4610}{7/8 \times 4.07 \text{ ft} \times 4.5 \text{ in}} = 289 \text{ #/sq. in. allowable } 250$$

H15 Live Load Shear H15 Loading

Wheel Load 12000 #

15 in. wd.

Eff. wd. 3.68 ft.

$$\text{Load on a ft. of slab} = \frac{12000}{3.68} = 3260 \text{ #}$$

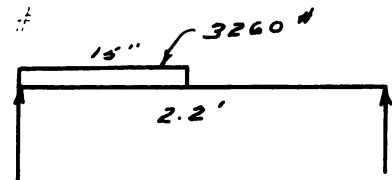
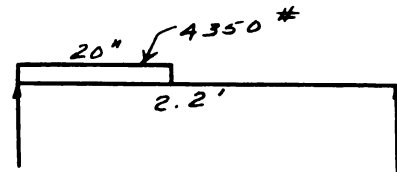
$$LLV = \frac{3260 \left(2.2 - \frac{15}{12} \right)}{2.3} = 2335 \text{ #}$$

$$LLV + Imp. = 2335 \text{ lb} \times 166.9\% = 3900 \text{ #}$$

$$\text{Total Shear } 3900 + 110 = 4010 \text{ #}$$

$$\text{Shear } v = \frac{V}{7/8 d b} = \frac{4010}{7/8 \times 4.5 \text{ ft} \times 12 \text{ in}} = 84.9 \text{ #/sq. in. allowable } 75$$

$$\text{Bond } u = \frac{V}{7/8 o d} = \frac{4010}{7/8 \times 4.07 \text{ ft} \times 4.5 \text{ in}} = 250 \text{ #/sq. in. allowable } 250$$

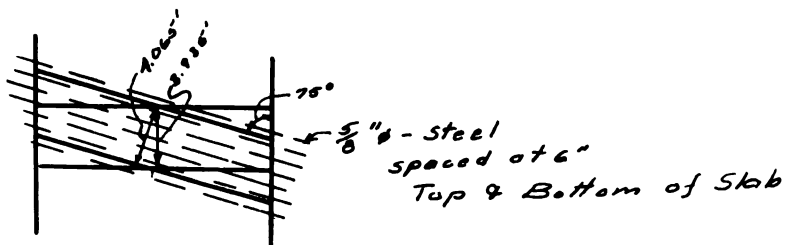


Concrete Slab between Second Girder and first 12 in. @ 25# 12
 12 in. @ 25# 12- Flange wd. 6.5 in.
 center to center dis. 2ft. 10in.
 wd. of flange of girder 1.19 ft.

$$\text{Clear dis.} = 2.75 - \frac{(1.19 + 6.5)}{2} = 1.985 \text{ ft.}$$

$$(35) \quad 1.985 + .5 = 2.485 \text{ ft.}$$

2.485 is less than 2.85; therefore Span Length is 2.485
 say 2.49 ft.



(41) Effective Width

$$\begin{aligned} \text{eff. wd.} &= 0.7 s + 2 \quad \text{on 75 degree angle} \\ s &= \text{center to center of supports on 75 degree angle} \\ s &= \frac{2.85}{\sin 75} = 2.95 \text{ ft.} \end{aligned}$$

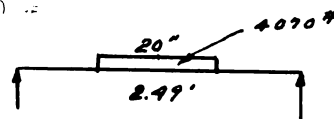
$$\begin{aligned} \text{eff. wd.} &= .7 \cdot 2.95 + 2 \quad \text{on 75 degree angle} \\ &= 4.065 \text{ ft.} \end{aligned}$$

$$\text{eff. wd.} = 4.065 \sin 75 = 3.935 \text{ ft. on 90 degree angle}$$

Max. Live Load Bending Moment 40 Loading
 wheel load = 16000 # 20 in. wd.

$$\begin{aligned} \text{Load on 3 ft. slab} &= \frac{16000}{3.935} = 4070 \# \\ \text{Continuity} &= 0.8 \end{aligned}$$

$$\text{LLBM} = .8 \left(\frac{2035 \cdot 1.245 - 4070 \cdot 5}{2 \cdot 12} \right) = 1340 \text{ ft. lbs.}$$



$$(37) \quad \text{Impact} = \frac{L + 20}{CL + 20} = \frac{2.49 + 20}{6 \cdot 2.49 + 20} = 64.5 \%$$

$$\text{LLEM} + \text{Imp.} = 1340 \cdot 64.5 \% = 867 \text{ ft. lbs.}$$

Max. Dead Load Bending Moment $w = 100 \#/\text{ft.}$

$$\text{DLBM} = \frac{w l^2}{10} = \frac{100 \cdot 2.49^2}{10} = 62 \text{ ft. lbs.}$$

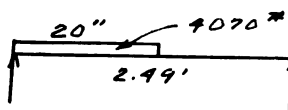
$$\text{Total BM} = 867 + 62 = 929 \text{ ft. lbs.}$$

Concrete Slab between Second Girder and first 12 in. @ 25# CB

Check d

$$d = \sqrt{\frac{B^2}{K b}} = \sqrt{\frac{2267 \cdot 12}{173 \cdot 12}} = 3.62 \text{ in.} \quad \text{supplied 4.5}$$

H20 Live Load Shear H20 Loading

$$LLV = \frac{4070}{2.49} \left(2.49 - \frac{20}{2 \cdot 12} \right) = 3720 \#$$


$$LLV + Imp. = 3720 \cdot 164.5 \% = 4480 \#$$

Dead Load Shear $W = 100 \text{ #/ft.}$

$$DLV = \frac{W l}{2} = \frac{100 \cdot 2.49}{2} = 124.5 \#$$

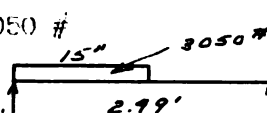
$$\text{Total } V = 4480 + 124.5 = 4604.5 \#$$

$$\text{Shear } v = \frac{V}{7/8 b d} = \frac{4604.5}{7/8 \cdot 4.5 \cdot 12} = 97.4 \text{ #/sq. in.} \quad \text{allowable 75}$$

$$\text{Bond } u = \frac{V}{7/8 \Sigma o d} = \frac{4604.5}{7/8 \cdot 4.07 \cdot 4.5} = 227 \text{ #/sq. in.}$$

H15 Live Load Shear H15 Loading

$$\begin{aligned} \text{Wheel Load} &= 12000 \# \quad 15 \text{ in. wd.} \\ \text{Eff. wd.} &= 3.935 \text{ ft.} \end{aligned}$$

$$\text{Load on a ft. of slab} = \frac{12000}{3.935} = 3050 \#$$


$$LLV = \frac{3050}{2.49} \left(2.49 - \frac{15}{2 \cdot 12} \right) = 2285 \#$$

$$LLV + Imp. = 2285 \cdot 164.5 \% = 3530 \#$$

$$\text{Total } V = 3530 + 124.5 = 3654.5 \#$$

$$\text{Shear } v = \frac{V}{7/8 d b} = \frac{3654.5}{7/8 \cdot 4.07 \cdot 12} = 77.2 \text{ #/sq. in.} \quad \text{allowable 75}$$

$$\text{Bond } u = \frac{V}{7/8 \Sigma o d} = \frac{3654.5}{7/8 \cdot 4.07 \cdot 4.5} = 228 \text{ #/sq. in.} \quad \text{allowable 250}$$

SPRINGERS

12 in. @ 25 # CB Stringers spaced at 2 ft. 9 1/2 in.

Center to center of Beams 15.4 ft.

Dead Load

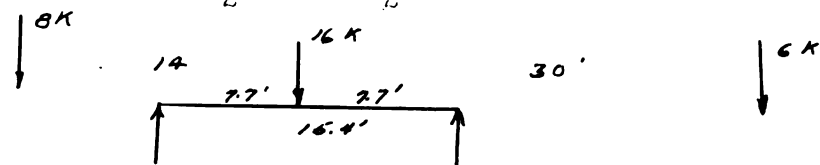
earing Surface	25 #/sq. ft.	
	25 x 2.8 =	70 #/ft.
Concrete	150 #/ft. ²	
	.5 x 2.8 x 150 =	210
Stringer		25
	total	305 #/ft.

Max. Dead Load Bending Moment

$$DLBM = \frac{wl^2}{8} = \frac{305 \times 15.4^2}{8} = 9040 \text{ ft. lbs.}$$

Max. Dead Load Shear

$$DLV = \frac{wl}{2} = \frac{305 \times 15.4}{2} = 2350 \text{ lbs.}$$



Max. Live Load Bending Moment H20 Loading

LLEM of one Traffic Line

$$\frac{32000 \times 15.4}{2 \times 2} = 123200 \text{ ft. lbs.}$$

$$(43) M' = C \frac{M}{N} = \text{LLEM for one stringer}$$

N = Width of Traffic Line (not to exceed 10 ft.)
 C = 1 (for concrete surface) Spacing of Stringers

$$N = \frac{10}{2.8} = 3.57$$

$$M' = \frac{1 \times 123200}{3.57} = 34500 \text{ ft. lbs.} \quad \text{LLEM for one stringer}$$

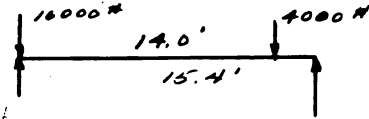
$$(37) \text{ Impact} = \frac{L+20}{6 \times L+20} = \frac{15.4+20}{6 \times 15.4+20} = 31.5 \%$$

$$LLBM + Imp. = 34500 \times 1.315 = 45400 \text{ ft. lbs.}$$

$$\text{Total BM} = 45400 + 9040 = 54440 \text{ ft. lbs.}$$

12 in. @ 25 # CB Stringers spaced at 2 ft. 9 1/2 in.

Max. Live Load Shear



$$LLV = 16000 + \frac{4000 \times 1.4}{15.4} = 16364 \#$$

$$LLV + Imp. = 16364 \times 1.31.5 \% = 21514 \#$$

$$Tot. V = 21514 + 2350 = 23864 \#$$

Check Section Modulus (I/c)

$$I/c \text{ of } 12 \text{ in. @ } 25 \# \text{ CB} = 30.3 \text{ in.}^3$$

$$I/c = M/f \quad f = 18000 \#/\text{sq. in.}$$

$$I/c = \frac{54440 \times 12}{18000} = 36.1 \text{ in.}^3$$

supplied 30.8

$$f = 24000 \#/\text{sq. in.}$$

$$I/c = \frac{54440 \times 12}{24000} = 27.0 \text{ in.}^3$$

supplied 30.8

Check Web of Stringer

$$\text{Back to back of Flange} = 11.88 \text{ in.}$$

$$\text{Thickness of Web} = .240 \text{ in.}$$

$$v = \frac{V}{A} = \frac{23864}{11.88 \times .24} = 8340 \#/\text{sq. in.}$$

allowable 12000

12 in. @ 31.5 # I Bm.

Not only has it a Section Modulus of 36.0 in.³, but is 2 ft. 9 1/2 in. from next stringer and 2 ft. 6 in. from Girder; therefore it is OK

10 in. @ 25 # I Stringers spaced at 2 ft. 3 in.

Center to center of Beams 15.4 ft.

Dead Load

Wearing Surface	25 #/sq. ft.	
	$25 \times 2.25 =$	56 #/ft.
Concrete	150 #/ft.^2	
	$.5 \times 2.25 \times 150 =$	168.75
Stringer	25 #/ft.	
		$\frac{25}{2}$
	total	249.75 #/ft.

Max. Dead Load Bending Moment

$$DLBM = \frac{w l^2}{8} = \frac{249.75 \times 15.4^2}{8} = 7400 \text{ ft. lbs.}$$

Max. Dead Load Shear

$$DLV = \frac{w l}{2} = \frac{249.75 \times 15.4}{2} = 1922 \text{ #}$$

Max. Live Load Bending Moment H20 Loading

$$LLBM \text{ of one Traffic Lane} = 123200 \text{ ft. lbs.}$$

$$(43) M' = \frac{C M}{N} = \text{LLBM for one stringer}$$

$$N = \frac{\text{Width of Traffic Lane (not to exceed 10 ft.)}}{\text{Spacing of Stringers}}$$

$$C = 1 \quad (\text{for concrete surface})$$

$$N = \frac{10}{2.25} = 4.45$$

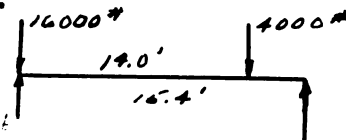
$$M' = \frac{1 \times 123200}{4.45} = 27750 \text{ ft. lbs.} \quad \text{LLBM for one Stringer}$$

$$LLBM + Imp. = 131.5 \times 27750 = 36500 \text{ ft. lbs.}$$

$$\text{Total BM} = 36500 + 7400 = 43900 \text{ ft. lbs.}$$

Max. Live Load Shear

$$LLV = 16000 + \frac{4000 \times 1.4}{15.4} = 16364 \text{ #}$$



$$LLV + Imp. = 16364 \times 131.5 \times 3 = 21514 \text{ ft. lbs.}$$

$$\text{Total V} = 21514 + 1922 = 23436 \text{ #}$$

10 in. @ 25 # I Stringers spaced at 2 ft. 6 in.

Check Section Modulus (I/c)

I/c of 10 in. @ 25 # 24 in.³

$$I/c = M/f$$

$$f = 18000 \text{ #/sq. in.}$$

$$I/c = \frac{43900 \cdot 12}{18000} = 29.5 \text{ in.}^3 \quad \text{supplied 24}$$

$$f = 24000 \text{ #/sq. in.}$$

$$I/c = \frac{43900 \cdot 12}{24000} = 22.0 \text{ in.}^3 \quad \text{supplied 24}$$

Check Web of Stringer

Back to back of Flange 10 in.

Thickness of Web 0.31 in.

$$v = \frac{V}{A} = \frac{23435}{10 \cdot 0.31} = 7530 \text{ #/sq. in.} \quad \text{allowable 12000}$$

6 in. @ 14.75 # I Stringer spaced at 2 ft. 4 1/2 in.

Center to center of Beams 15.4 ft.

Dead Load

Concrete	150 #/ft. ²		
	5/12 2.375	150	= 148.5 #/ft.
Stringer	14.75 #/ft.		<u>14.75</u>
		total	<u>163.25</u>

Max. Dead Load Bending Moment

$$DLBM = \frac{w l^2}{8} = \frac{163.25 \times 15.4^2}{8} = 4850 \text{ ft. lbs.}$$

Max. Dead Load Shear

$$DLV = \frac{w l}{2} = \frac{163.25 \times 15.4}{2} = 1258 \text{ #}$$

Max. Live Load Bending Moment

(34) Live Load 100 #/sq. ft.
 100 2.375 = 237.5 #/ft.

$$LLBM = \frac{w l^2}{8} = \frac{237.5 \times 15.4^2}{8} = 7050 \text{ ft. lbs.}$$

Max. Live Load Shear

$$LLV = \frac{w l}{2} = \frac{237.5 \times 15.4}{2} = 1830 \text{ #}$$

Total Bending Moment

$$4850 + 7050 = 11900 \text{ ft. lbs.}$$

Total Shear

$$1258 + 1830 = 3088 \text{ #}$$

Check Section Modulus (I/c)

$$I/c \text{ of 6 in. @ 14.75 # I} \quad 7.9 \text{ in}^3$$

$$I/c = M/f \quad f = 18000 \text{ #/sq. in.}$$

$$I/c = \frac{11900 \times 12}{18000} = 7.93 \text{ in}^3$$

supplied 7.9

$$f = 24000 \text{ #/sq. in.}$$

$$I/c = \frac{11900 \times 12}{24000} = 5.95 \text{ in}^3$$

supplied 7.9

6 in. @ 14.75 # I Stringer spaced at 2 ft. 4 1/2 in.

Check Web of Stringer

Back to back of Flange	6 in.
Thickness of Web	0.343 in.

$$v = \frac{V}{A} = \frac{8000}{6 \times 0.343} = 1500 \text{ #/sq. in.} \quad \text{allowable 12000}$$

ELAMS

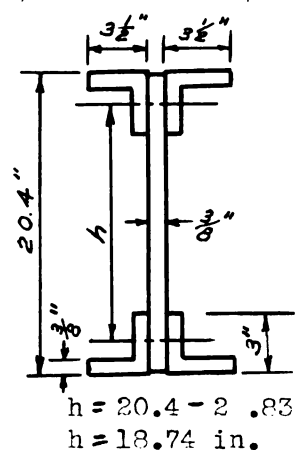
Dead Weight of Inside and Outside Beam #/ft.

$$\begin{array}{rcl}
 5/8 \text{ in. Web} & 20.4 \text{ in. wd.} & \\
 3/8 \times 1/12 \times 20.4/1.490 & = & 25.1 \text{ #/ft.} \\
 4\text{-Angles} & 3\frac{1}{2} \text{ by } 3 \text{ by } 3/8 \text{ in. @ } 7.9 \text{ #} & 31.6 \\
 4\text{-Stiffeners} & 5 \text{ by } 2\frac{1}{2} \text{ by } 3/8 \text{ in. @ } 6.6 \text{ #} & \\
 4 \times 6.6 \times 1.6/15.4 & = & 3.0 \\
 115 \text{ Rivets} & 12 \text{ #/100 Heads} & \\
 & 12 \times 20/15.4/100 & = 1.8 \\
 4\text{-Splice Plates} & 3/8" \text{ by } .75' \text{ by } 1.2' & \\
 4 \times .75 \times 1.2 \times 490 & = & 1.4 \\
 \hline
 6 \times 12 \times 15.4 & \text{tot. } 62.9 \text{ say } 63 \text{ #/ft.} &
 \end{array}$$

Cross Section of Beam

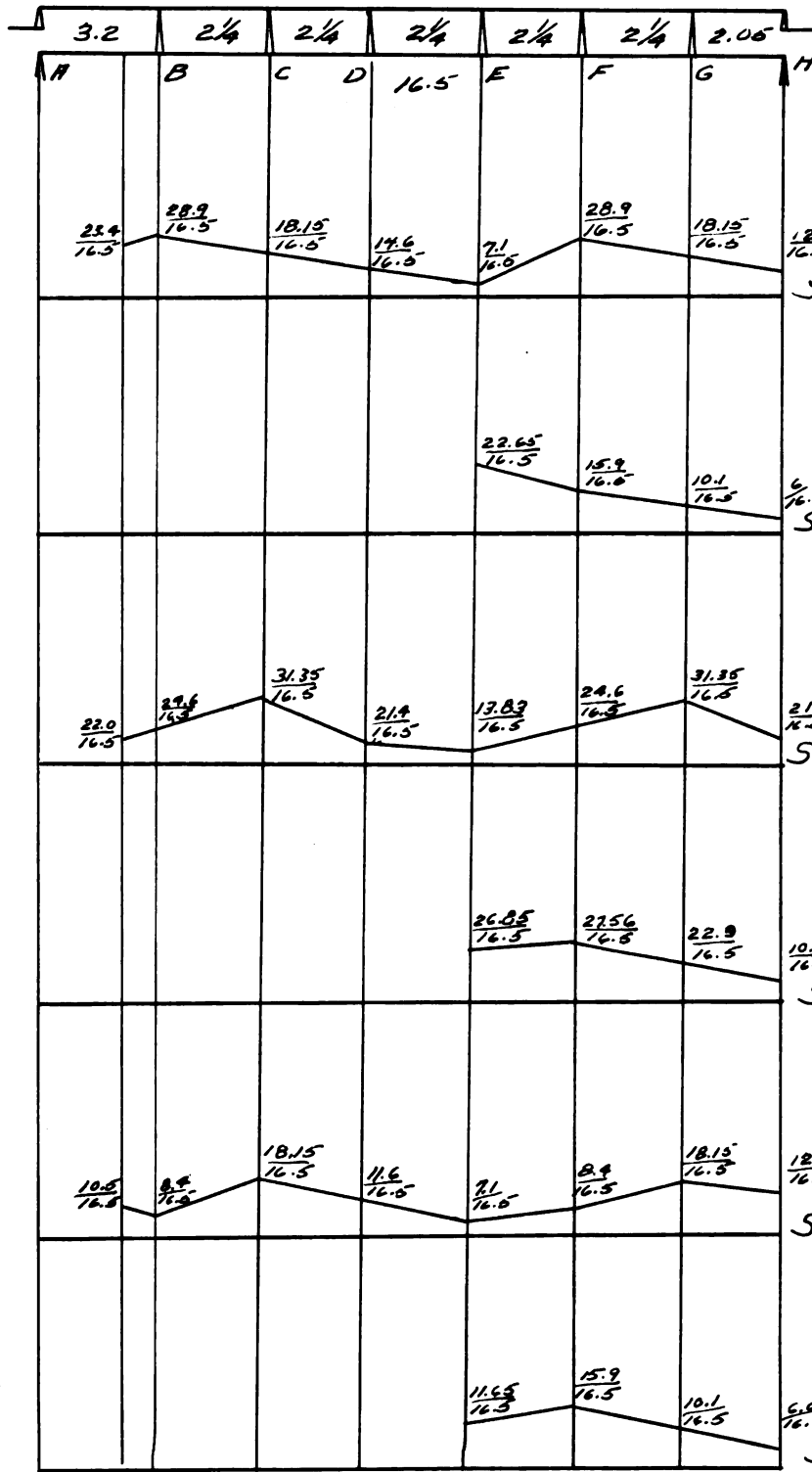
Gross Section of Flange Area
 2-angles $3\frac{1}{2}$ by 3 by $3/8$ 4.6 sq. in.

Net Section of Flange Area
 -4- $3/4$ Rivets $3/8 \times 7/8 \times 4$ $\frac{-1.3}{3.3 \text{ sq. in.}}$



Outside Beam
Influence Lines for Traffic Lanes
Live Load

Cutb
2.5'



Shear at AB, Load ①

Shear at AB, Load ②

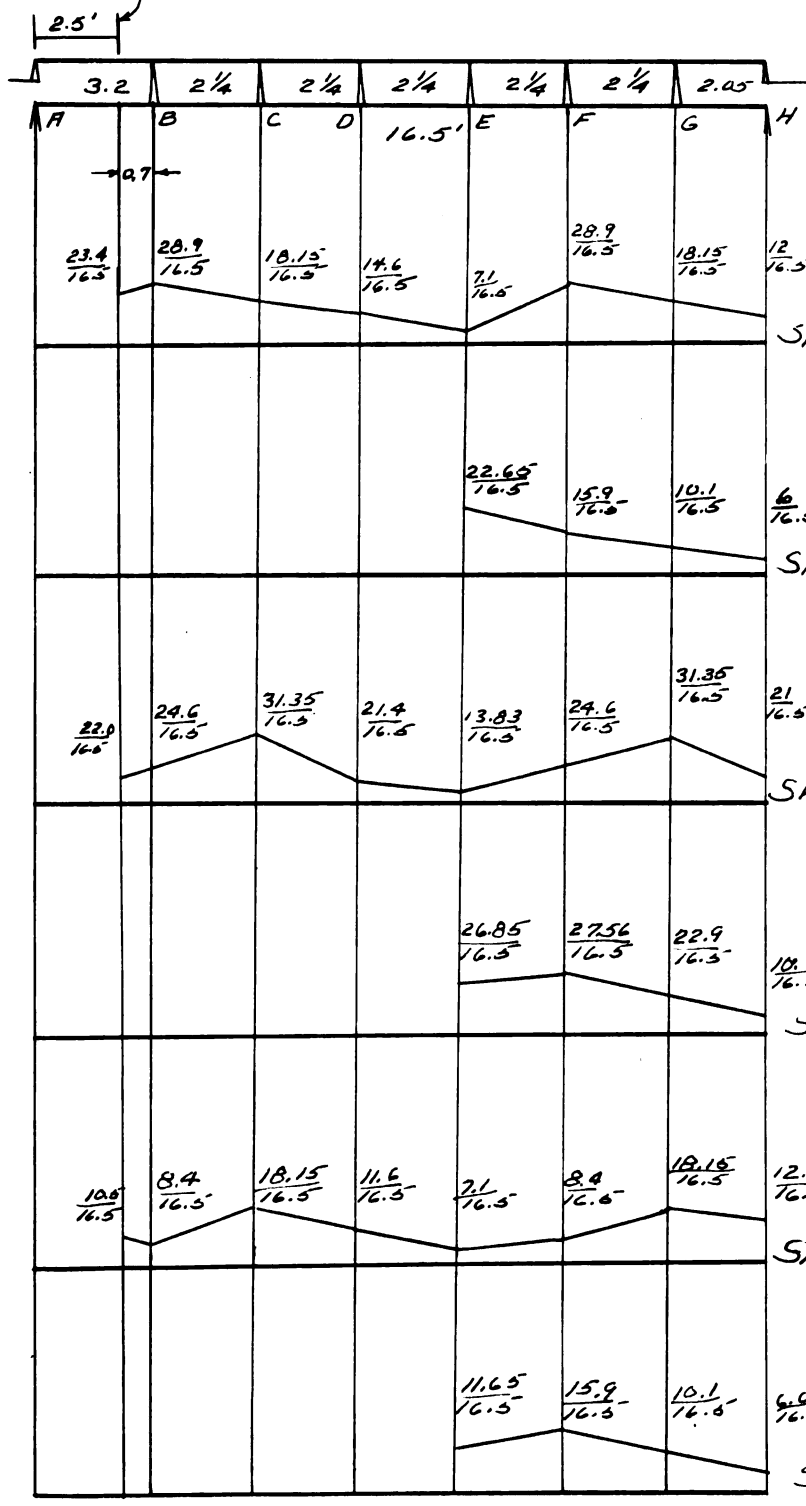
Shear at GH, Load ①

Shear at GH, Load ②

Shear at BC, Load ①

Shear at BC, Load ②

Outside Beam
Influence Line for Traffic Lanes
Live Load



Shear at AB, Load ①

Shear at AB, Load ②

Shear at GH, Load ①

Shear at GH, Load ②

Shear at BC, Load ①

Shear at BC, Load ②

Outside Beam

Dead Load

Dead Load Conc.

Panel Point B

Concrete 150 #/ft.³

$$.5 \frac{(3.2 + 2.35)}{2} 15.4 150 = 3150 \#$$

Wearing Surface 25 #/sq. ft.

$$25 \frac{(3.2 + 2.35)}{2} 15.4 = 1050$$

10 in. @ 25 # I stringer

$$25 15.4 =$$

$$\text{tot. } \frac{385}{4885 \#}$$

Panel Points C, D, E, F

Concrete 150 #/ft.³

$$.5 \frac{2\frac{1}{4}}{2} 15.4 150 = 1600 \#$$

Wearing Surface 25 #/sq. ft.

$$25 \frac{2\frac{1}{4}}{2} 15.4 = 868$$

10 in. @ 25 # I stringer

$$25 15.4 =$$

$$\text{tot. } \frac{385}{3853 \#}$$

Panel Point G

Concrete 150 #/ft.³

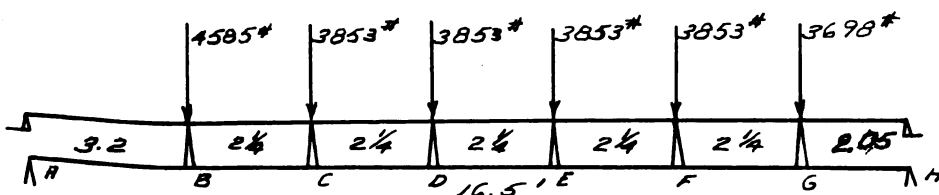
$$.5 \frac{(2\frac{1}{4} + 2.05)}{2} 15.4 150 = 2485 \#$$

Wearing surface 25 #/sq. ft.

$$25 \frac{(2\frac{1}{4} + 2.05)}{2} 15.4 = 888$$

Stinger

$$\text{tot. } \frac{385}{3888 \#}$$



Outside Beam

Max. Dead Load Bending Moment

DLBM at E

$$3698 \frac{14.45}{16.5} \cdot 0.55 + \frac{3255 \cdot 6.55}{16.5} (12.2 + 9.95 + 7.7 + 5.45) \\ + 4615 \frac{3.2 \cdot 6.55}{16.5} - 3698 \cdot 4.5 - 3255 \cdot 2.25 + \frac{63 \cdot 16.5^2}{8} = 56400 \text{ ft. lbs.}$$

DLBM at D

$$3698 \frac{14.45}{16.5} \cdot 8.8 + \frac{3255 \cdot 2.2}{16.5} (12.2 + 9.95 + 7.7 + 5.45) \\ + 4585 \frac{3.2 \cdot 2.2}{16.5} - 3698 \cdot 6.75 - 3255 \cdot 2.25 + \frac{63 \cdot 16.5^2}{8} \\ \text{Max.} = 59250 \text{ ft. lbs.}$$

Max. Dead Load Shear

DLV at AB

$$3255 \frac{2.05}{16.5} + \frac{3255}{16.5} (4.3 + 6.55 + 2.2 + 11.05) + 4585 \frac{13.3}{16.5} \\ + \frac{63 \cdot 16.5}{2} = 11040$$

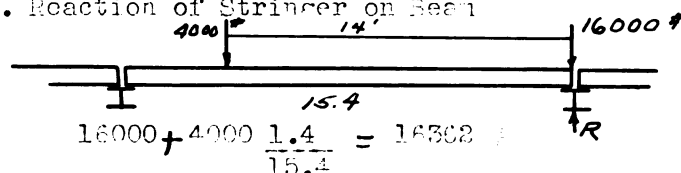
DLV at GE

$$3698 \frac{14.45}{16.5} + \frac{3255}{16.5} (12.2 + 9.95 + 7.7 + 5.45) + \frac{4585 \cdot 3.2}{16.5} \\ \text{Max.} + \frac{63 \cdot 16.5}{2} = 12920 \#$$

Max. Live Load Bending Moment H20 Loading

LLBM is Max. at D when load 1 is 1.5 ft. from curb and equals
122/15.5 for 1 load on each wheel

Max. Reaction of Stringer on Beam



$$(37) \text{ Impact} = \frac{L+30}{6L+30} \frac{16.5+30}{16.5+30} = 30.7 \%$$

Outside Beam

Max. Live Load Bending Moment (cont.)

BM at D (cont.)

$$LLM \text{ at D} + Imp. = 16362 \frac{122}{16.5} 130.7 \# = 158000 \text{ ft. lbs.}$$

$$DLM \text{ at D} = 59350 \text{ ft. lbs.}$$

$$\text{Total BM at D} = 59350 + 158000 = 217350 \text{ ft. lbs.}$$

BM at E

LLM is Max. at E when load 2 is at E and equals $126.4/16.5$ for $1\frac{1}{2}$ load on each wheel

$$LLM \text{ at E} + Imp. = 16362 \frac{126.4}{16.5} 130.7 \# = 155800 \text{ ft. lbs.}$$

$$DLM \text{ at E} = 56400 \text{ ft. lbs.}$$

$$(\text{Max.}) \text{ Total BM at E} = 56400 + 155800 = 212200 \text{ ft. lbs.} \quad \text{Freely supported}$$

$$\text{Continuity} = 0.7$$

$$\text{Total BM} = 212200 \times 0.7 = 148540 \text{ ft. lbs.} \quad \text{Continuous beam}$$

Max. Live Load Shear 120 Loading

LLV is max. at GH with load 1 at G and equals $51.35/16.5$ for $1\frac{1}{2}$ load on each wheel

$$LLV \text{ at GH} + Imps. = 16362 \frac{51.35}{16.5} 130.7 \# = 40500 \#$$

$$DLV \text{ is max. at GH} = 12900 \#$$

$$\text{Total V} = 12900 + 40500 = 53400 \#$$

Outside Beam

Max. Total Shear at the second Panel from End (between first and second stringer)

Dead Load Shear at FG

$$\frac{3698 \cdot 14.45}{16.5} + \frac{3953 (12.2 + 9.25 + 7.7 + 5.45)}{16.5} + \frac{4585 \cdot 3.2}{16.5} \\ + \frac{63 \cdot 16.5}{2} - 3698 - 63 \cdot 2.05 = 9093 \# \quad \text{Max.}$$

Dead Load Shear at BG

$$\frac{3698 \cdot 2.05}{16.5} + \frac{3953 (4.3 + 6.55 + 8.8 + 11.05)}{16.5} + \frac{4585 \cdot 13.3}{16.5} \\ + \frac{63 \cdot 16.5}{2} - 4585 - 63 \cdot 3.2 = 7053 \#$$

Live Load Shear is Max. at FG with load 1 at F and equals $24.6/16.5$ for 1st load at each wheel.

$$\text{Impact} = 130.7 \#$$

$$\text{Max. Reaction of Stringer on Beam} = 16362 \#$$

$$\text{LLV at FG} + \text{Imp.} = 16362 \frac{24.6}{16.5} + 130.7 \# = 31900 \#$$

$$\text{DLV at FG} = 9093 \#$$

$$\text{Total V at FG} = 9093 + 31900 = 40993 \#$$

Outside Beam

Check Cross Section of Beam

Gross Section of Flange 4.6 sq. in.

Net Section of Flange 3.3 sq. in.

Web 3/8 by 20.4 in.

h 18.74 in.

Tension Flange

$$A_s = \frac{P_u}{f F} - 1/8 \text{ of web}$$

$$f = 18000 \text{ \#/sq. in.}$$

$$3.3 = \frac{154140 \text{ lb} - 1/8 \cdot 20.4 \cdot 3/8}{18000 h}$$

$$h = 2.1 \text{ in. supplied } 18.74$$

$$f = 24000 \text{ \#/sq. in.}$$

$$3.3 = \frac{154140 \text{ lb} - 1/8 \cdot 20.4 \cdot 3/8}{24000 h}$$

$$h = 18.1 \text{ in. supplied } 18.74$$

Compression Flange

$$(47) \quad f = 18000 - 5 L^2/b^2 \\ = 18000 - 5 (3.2 \text{ in})^2 / 7.37^2 = 17864.5 \text{ \#/sq. in.}$$

$$A_s = \frac{154140 \text{ lb} - 1/8 \cdot 20.4 \cdot 3/8}{17864.5 \cdot 18.74}$$

$$A_s = 4.57 \text{ sq. in. supplied } 4.6$$

Web

$$v = 12000 \text{ \#/sq. in. allowable}$$

$$v = \frac{V}{A} = \frac{55480}{3/8 \cdot 20.4} = 6980 \text{ \#/sq. in.}$$

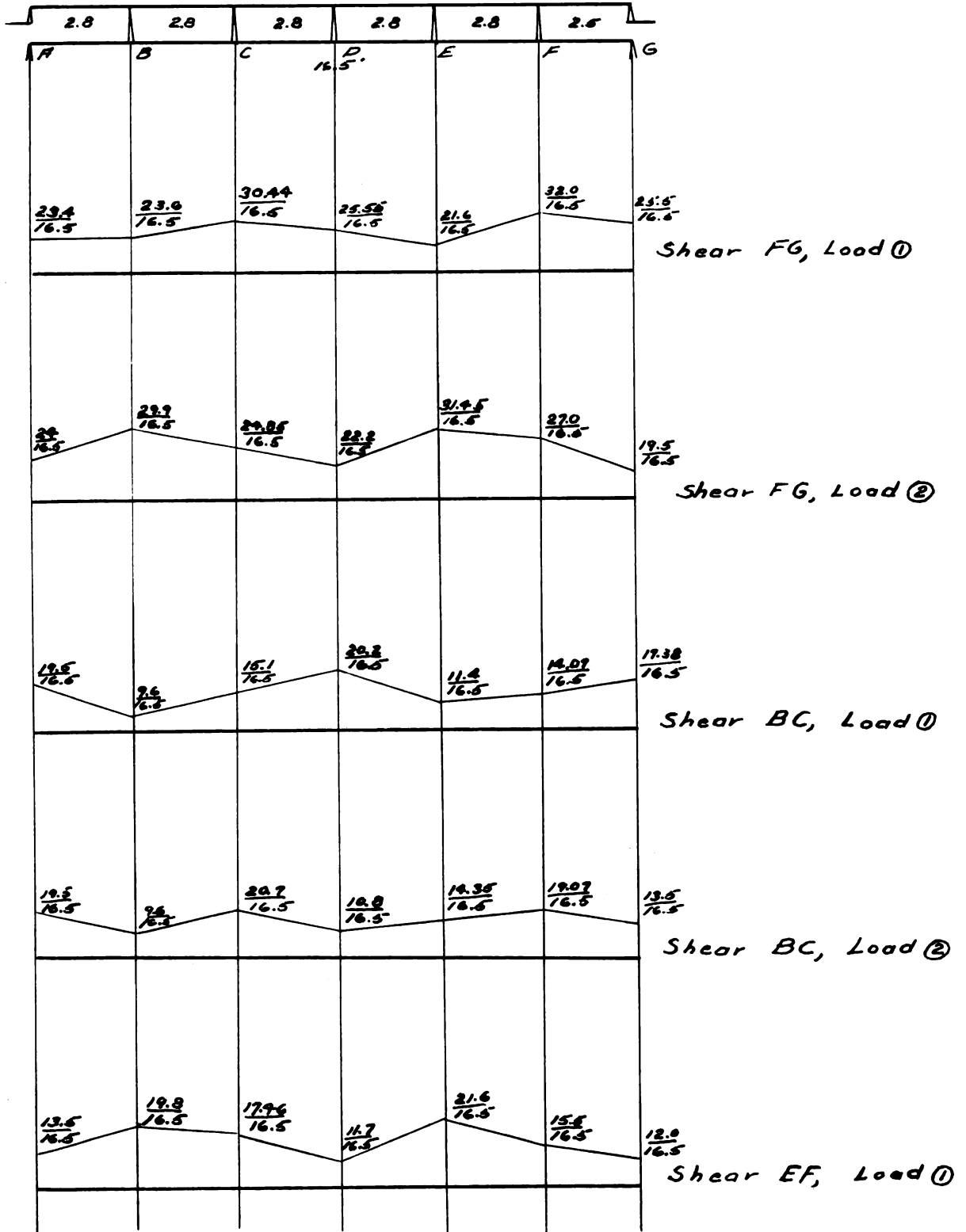


Inside Beam

Live Load

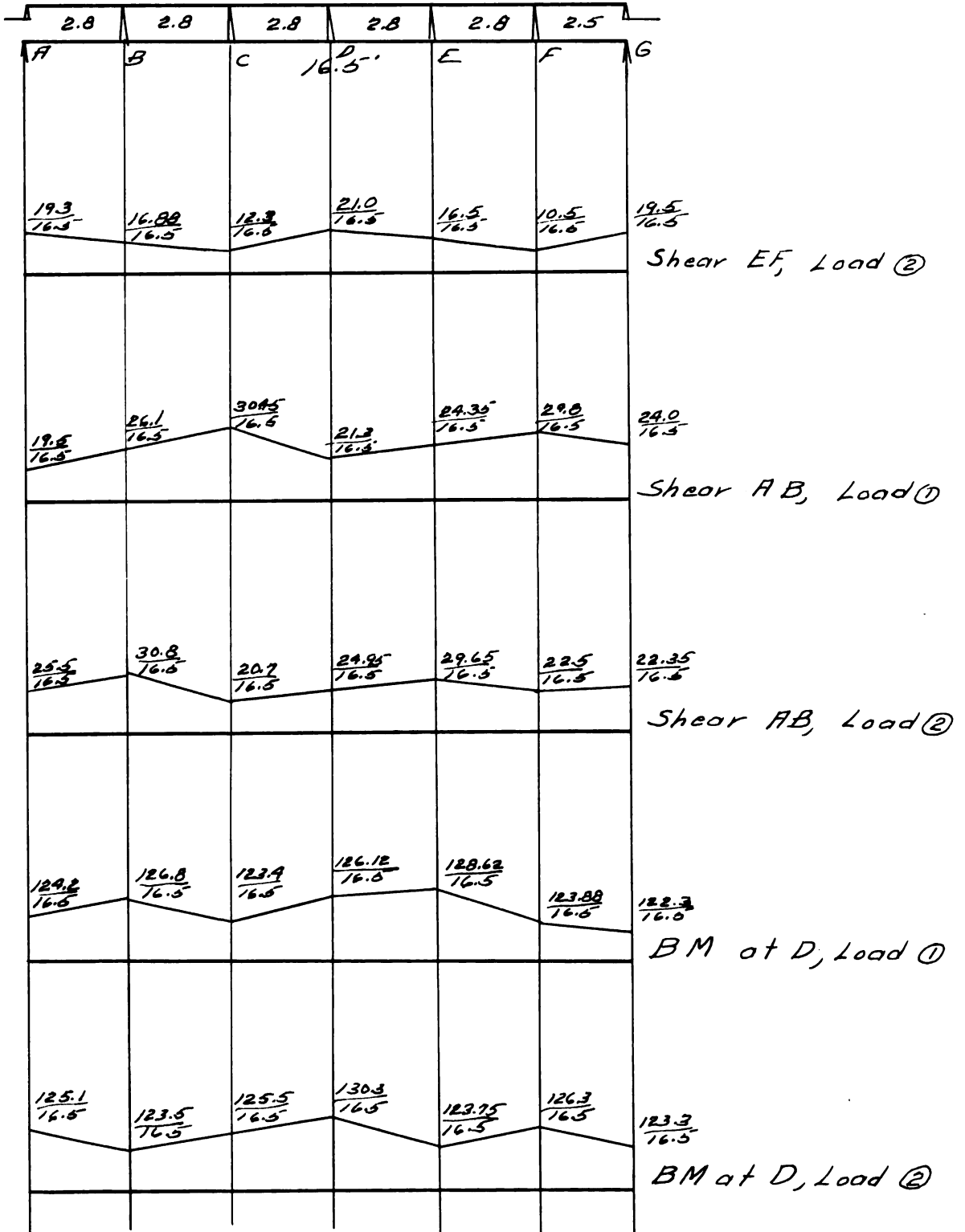
Influence Lines

for Traffic Lanes





Inside Beam
Live Load Influence
Lines for Lanes of Traffic



Inside Beam

Dead Load

Conc. Dead Load

Panel Points B, C, D, E

$$\text{Concrete } 150 \text{ #/ft.}^3 \\ 0.5 \times 2.8 \times 15.4 \times 150 = 3240 \text{ #}$$

$$12 \text{ in. @ } 25 \text{ # CB stringer} \\ 25 \times 15.4 = 385$$

$$\text{Wearing Surface } 25 \text{ #/sq. ft.} \\ 25 \times 2.8 \times 15.4 = 1072 \\ \text{total } 4703 \text{ #}$$

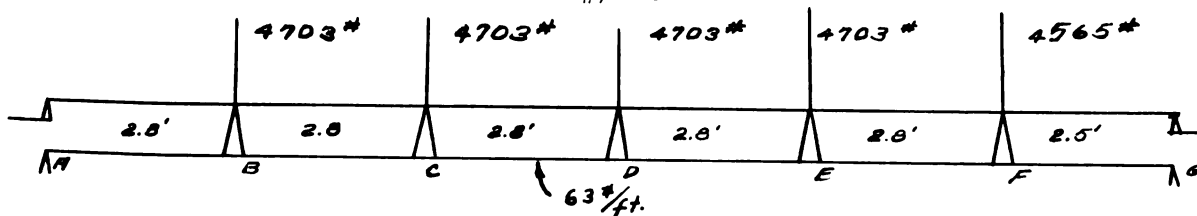
Panel Point F

$$\text{Concrete } 150 \text{ #/ft.}^3 \\ 0.5 \left(\frac{2.5 + 2.8}{2} \right) \times 15.4 \times 150 = 3060 \text{ #}$$

$$12 \text{ in. @ } 31.5 \text{ # I Em. stringer} \\ 15.4 \times 31.5 = 485$$

$$\text{Wearing surface } 25 \text{ #/sq. ft.} \\ 25 \times 15.4 \left(\frac{2.5 + 2.8}{2} \right) = 1020 \\ \text{total } 4565 \text{ #}$$

Uniform Dead Load 63 #/ft.



Max. Dead Load Bending Moment

DLBM at D

$$4565 \times \frac{14.0 \times 8.1}{16.5} + \frac{4703 \times 8.1}{16.5} (11.2 + 8.4 + 5.6 + 2.8) - 4703 \times 2.8 \\ - 4565 \times 5.6 + \frac{63 \times 16.5^2}{8} = 52100 \text{ ft. lbs.}$$

Max. Dead Load Shear

DLV at FG

$$\frac{4565 \times 14}{16.5} + \frac{4703}{16.5} (11.2 + 8.4 + 5.6 + 2.8) + \frac{63 \times 16.5}{2} = 12570 \text{ # Max.}$$

~~DLV at AB~~

$$\frac{4565 \times 2.5}{16.5} \quad \frac{4703}{16.5}$$

Inside Beam

Max. Dead Load Shear(cont.)

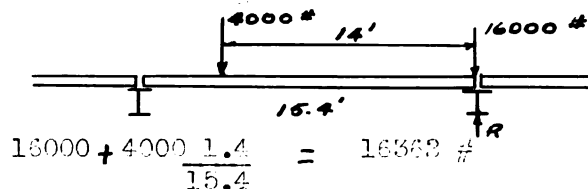
DLV at AB

$$\frac{4565 \cdot 2.5}{16.5} + \frac{4703}{16.5} (5.3 + 8.1 + 10.9 + 13.7) + \frac{63 \cdot 16.5}{2} = 11020 \text{ #}$$

Max. Live Load Bending Moment H20 Loading

LLBM is max. at D with Load 2 at D and equals $\frac{130.3}{16.5}$ for 1# load on each wheel

Max. Reaction of Stringer on Beam



$$(27) \text{ Impact} = \frac{L + 20}{6 L + 20} = \frac{16.5 + 20}{6 \cdot 16.5 + 20} = 30.7 \%$$

$$\text{LLBM} + \text{Imp.} = 16362 \frac{130.3}{16.5} 30.7 \% = 168570 \text{ ft. lbs.}$$

Max. DLBM = 54100 ft. lbs.

Total BM = 54100 + 168570 = 227670 ft. lbs. freely supported

Continuity at center of Beam .7

Total BM = 0.7 227670 = 159370 ft. lbs. Continuous Beam

Max. Live Load Shear H20 Loading

LLV is max. at FG with Load 1 at F and equals $\frac{32}{16.5}$ for 1# load on each wheel

LLV at FG

$$16362 \frac{32}{16.5} = 317000 \text{ #}$$

$$\text{LLV} + \text{Imp.} = 31700 30.7 \% 41400 \text{ #}$$

DLV at FG = 12370

$$\text{Total V} = 12370 + 41400 = 53770 \text{ #}$$

Inside Beam

Max. Total Shear at the second Panel from End (between first and second stringer)

Dead Load Shear at BC

$$\frac{4565 \cdot 2.5}{16.5} + \frac{4703 (5.3 + 8.1 + 10.9 + 13.7)}{16.5} + \frac{63 \cdot 16.5}{2}$$

$$- 4703 - 63 \cdot 2.9 = 6141 \#$$

Dead Load Shear at EF

$$\frac{4565 \cdot 14}{16.5} + \frac{4703 (11.2 + 8.4 + 5.6 + 2.8)}{16.5} + \frac{63 \cdot 16.5}{2}$$

$$- 4565 - 63 \cdot 2.5 = 8647 \# \quad \text{Max.}$$

Live Load Shear is Max. at EF with load 1 at E and equals $21.6/16.5$ for 1 # Load at each wheel.

$$\text{Impact} = 130.7 \%$$

$$\text{Max. Reaction of Stringer on Beam} = 16362 \#$$

$$\text{LLV at EF} + \text{Imp.} = 16362 \frac{21.6}{16.5} \cdot 130.7 \% = 27900 \#$$

$$\text{DLV at EF} = 8647 \#$$

$$\text{Total V at EF} = 27900 + 8647 = 36547 \#$$

Inside Beam

Check Cross Section of Beam

Gross Section of Flange 4.6 sq. in.
 Net Section of Flange 3.3 sq. in.
 Web 3/8 by 20.4 in.
 h 18.74 in.

Tension Flange

$$A_s = \frac{M}{f h} - 1/8 \text{ of web}$$

$$f = 18000 \text{ #/sq. in.}$$

$$3.3 = \frac{159370 \cdot 12}{18000 h} - 1/8 \cdot 20.4 \cdot 3/8$$

$$h = 24.8 \text{ in. supplied } 18.74 \text{ in.}$$

$$f = 24000$$

$$3.3 = \frac{159370 \cdot 12}{24000 h} - 1/8 \cdot 20.4 \cdot 3/8$$

$$h = 18.7 \text{ in. supplied } 18.74$$

Compression Flange

$$(47) \quad f = 18000 - 5 \frac{L^2}{b^2} = 18000 - 5(2.8 \cdot 12)^2 / 7.37^2 = 17826.8 \text{ #/sq. in.}$$

$$A_s = \frac{159370 \cdot 12}{17826.8 \cdot 18.74} - 1/8 \cdot 20.4 \cdot 3/8$$

$$A_s = 4.74 \text{ sq. in. supplied } 4.6$$

Web

$$v = 12000 \text{ #/sq. in. allowable}$$

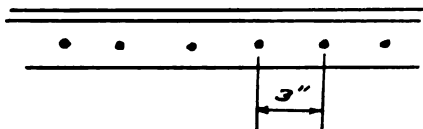
$$v = \frac{V}{A} = \frac{53770}{3/8 \cdot 20.4} = 7020 \text{ #/sq. in.}$$

Rivets in Beam from end to first Stiffener

Max. V of Each Beam

Inside Beam 53770 # Max.
Outside Beam 53420

Plan e Angle Rivets



Inside Beam

V was Max. at EG

Load on top of Flange

DL at F = 4565 #

Max. Reaction of Stringer 16362 # (H20)

LL + Imp = 16362 130.7 % = 21380 #

Total Load = 21380 + 4565 = 25945 #

Average Distance between stringers = $\frac{2.5 + 2.8}{2} = 2.65$ ft.

$w = \frac{25945}{2.65} = 9800$ #/ft.

Bearing of 3/4 Rivet on 3/8 Web Bearing = 27000 #/sq. in.
3/4 3/8 27000 = 7600 #

Double Shear shear = 13500 #/sq. in.
2 .443 13500 = 11960 #

$$FI = \frac{V}{h} \times \frac{A_f}{A_f + A_w/2} = \frac{53770}{15.74} \times \frac{4.6}{4.6 + 0.957} = 2375 \#$$

$$\text{Pitch} = \frac{R}{\sqrt{FI^2 + w^2}} = \frac{7600}{\sqrt{2375^2 + (9800/12)^2}} = 3.03 \text{ in.}$$

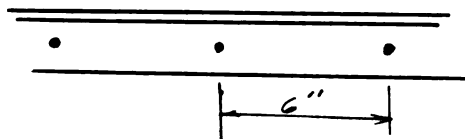
supplied 3 in.

Rivets in Beam (from Stiffener to Stiffener)

Max. V of Deck Beam (between first and second stringer)

Inside Beam	30547 #	
Outside Beam	40993	Max.

Flange Angle Rivets



Outside Beam

V was Max. at FG

Load on top of Flange

DL at F = 3883 #

Max. Reaction of Stringer = 16362 # (180)

LL + Imp. = 16362 130.7 % = 21380 #

Total Load = 21380 + 2883 = 25263 #

Average Dist. between stringers = 2.25 Ft.

$$w = \frac{25263}{2.25} = 11230 \text{ #/ft.}$$

Bearing of 3/4 Rivet on 3/8 Web	7600 #
Double Shear of 3/4 Rivet	11960

$$HI = \frac{V}{h} \times \frac{A_f}{A_f + A_w/8} = \frac{40993}{13.74} \times \frac{4.6}{4.6 + 0.957} = 1807 \text{ #}$$

$$\text{Pitch} = \sqrt{\frac{R^2}{HI^2 + w^2}} = \sqrt{\frac{7600^2}{1807^2 + (11230/13)^2}} = 3.74 \text{ in.}$$

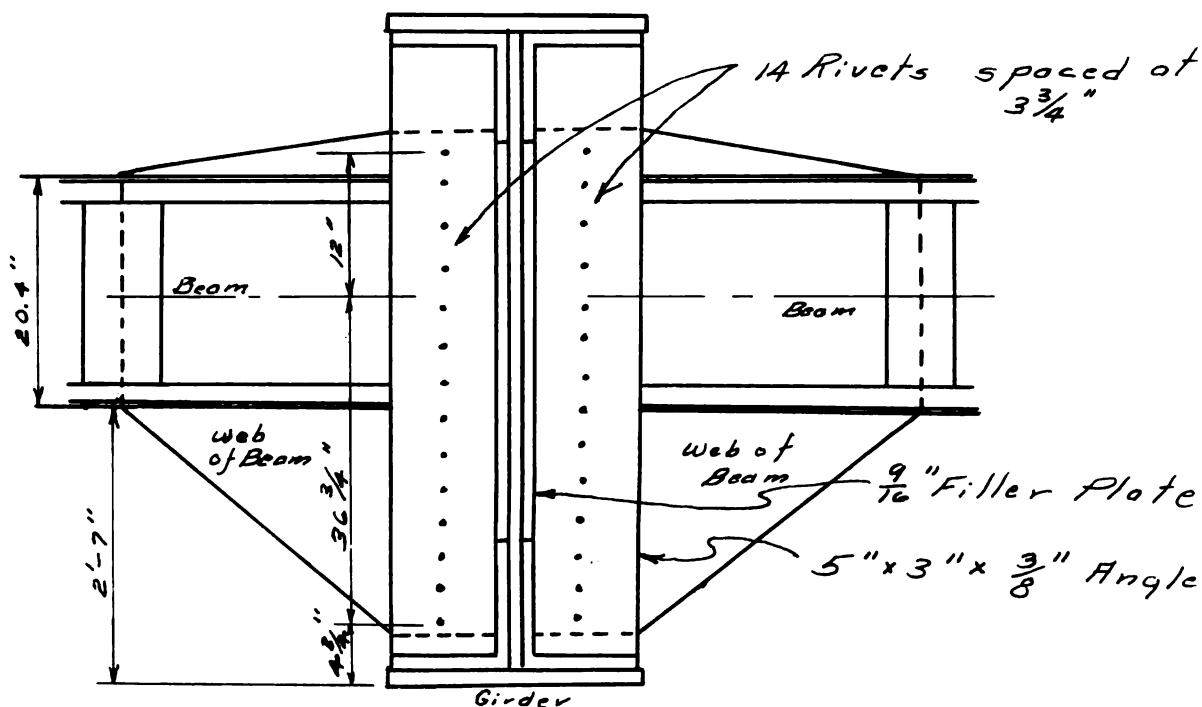
supplied 6 in.

Intermediate Stiffeners (Located 3.1 ft. from each end of Beam)

(127)(h) 60 3/8 = 22.5 in. which is greater than clear distance of 14.4 in.
No stiffeners needed.

Connection of Beam to Girder

Test Connection of Angles to Web of Beam



Inside Beam has greatest Bending Moment and also the greatest Shear next the Center Girder (Shear is the Reaction at the End of Beam)

BM = 227670 ft. lbs. bending moment at center of Freely Supported

Continuity at end of beam = $\frac{5}{6}$

BM = 227670 $\frac{5}{6}$ = 190550 ft. lbs. (at support)

V = 53770 #

Shear on each Rivet = $\frac{53770}{14}$ = 3840 #

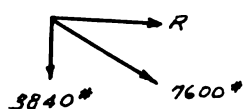
Bearing of $\frac{5}{4}$ Rivet on $\frac{3}{8}$ Web Bearing 27000 #/sq. in.
 $\frac{3}{8} \frac{3}{4}$ 27000 = 7600 #

Double Shear of $\frac{5}{4}$ Rivet shear = 13500 #/sq. in.
 2 .443 13500 = 11960 #

Connection of Beam to Girder

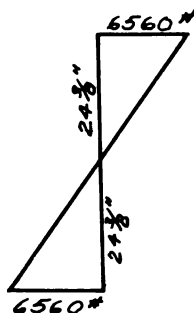
Web Connection of Angles to Web of Beam (cont.)

Reaction for bending moment



$$R = \sqrt{7600^2 - 3840^2} = 6560 \#$$

Bending Moment of Rivets



$$= \frac{2 \cdot 6560}{24 \frac{3}{8}} (1.375^2 + 5.375^2 + 9.375^2 + 13.125^2 + 16.875^2 + 20.625^2 + 24.375^2)$$

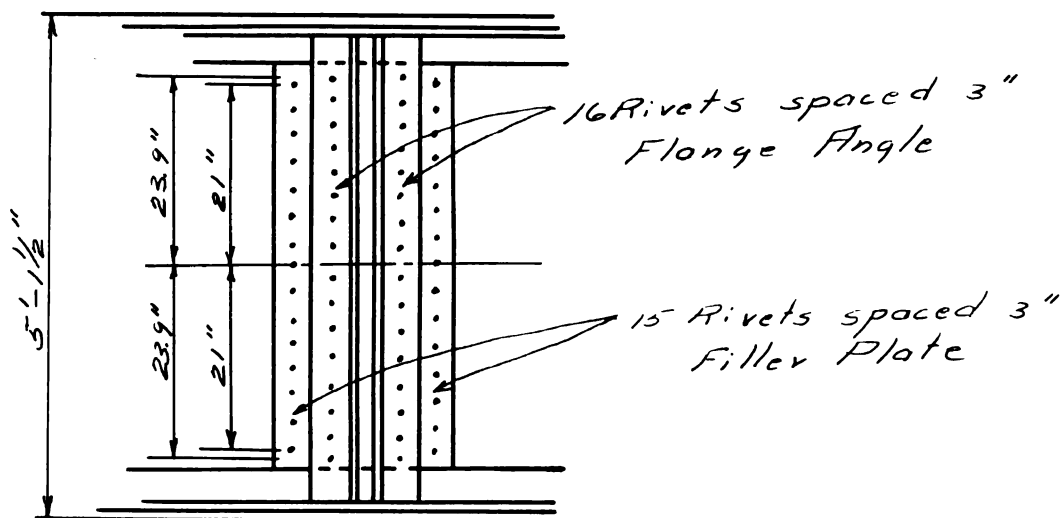
$$= 860000 \text{ in. lbs.}$$

or 71500 ft. lbs. supplied

130250 ft. lbs. needed

Connection of Beam to Girder

Fast Connection of Angles to Web of Girder



Rivets in Flange Angle

Bearing on $3/4$ Web and on $2-9/16$ Filler Plates
 bearing = 27000 #/sq. in.

$$27000 \left(\frac{3}{4} + 2 \frac{9}{16} \right) \frac{1}{2} = 55000 \#$$

Double Shear of $3/4$ Rivet $v = 13500$ #/sq. in.
 $2 \cdot 443 \cdot 13500 = 11960 \#$

$PK = 190250$ ft. lbs.

$V = 53770$ # One Beam

$V = 2 \cdot 53770 = 107540$ # Two Beams (one on each side of girder)
 Number of Rivets needed for Shear

$$= \frac{107540}{11960} = 9 \text{ Rivets}$$

Supplied 32 16 in each angle

(92)(c) Rivets in Tension fiber stress = $\frac{1}{2} 13500 = 6750$ #/sq. in.

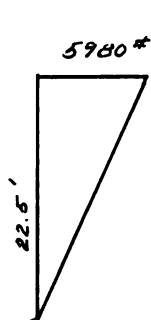
Rivets take the Tension while Compression is taken by
 angles bearing on web of Girder

Assumed neutral Axis Length of Angle

Fiber Stress per $3/4$ Rivet = $6750 \cdot 443 = 2990$ #
 2 rows of rivets = $2 \cdot 2990 = 5980$ #

Connection of Beam to Girder

Test Connection of Angles to Web of Girder (cont.)



RM of Rivets

$$\frac{2 \cdot 5980}{22.5} (22.5^2 + 19.5^2 + 16.5^2 + 13.5^2 + 10.5^2 + 7.5^2 + 4.5^2 + 1.5^2)$$

$$= 815000 \text{ in. lbs.}$$

or 67000 ft. lbs. Supplied

190250 ft. lbs. Needed

Test Connection of Filler Plate to Web of Girder

(99) Rivets in Filler (Same stress as those in Angle)

Bearing of 3/4 Rivet on 3/4 Web of Girder

$$\text{bearing} = 27000 \frac{\#}{\text{sq. in.}}$$

$$3/4 \cdot 3/4 \cdot 27000 = 11960 \frac{\#}{\text{in.}}$$

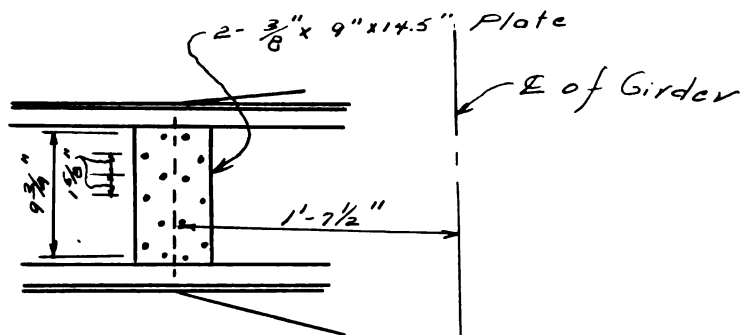
$$\text{Double Shear of } 3/4 \text{ Rivet} = 11960 \frac{\#}{\text{in.}}$$

$$V = 107540 \frac{\#}{\text{in.}}$$

$$\text{Number of Rivets} = \frac{107540}{11960} = 9 \text{ rivets needed}$$

supplied 30
15 on each end of filler

Beam Web Splice



(127)(f)

Web $3/8$ by 20.4 in.

Gross Section = 7.65 Sq. in.

Net Section

5- $3/4$ Rivets $5 \times 7/8 \times 3/8 = 1.65$ sq. in.Net Sec. = $7.65 - 1.65 = 6.0$ sq. in.Web Splice Plates 2- $3/8$ by 14.5 in.

Gross Section

 $2 \times 14.5 \times 3/8 = 10.88$ sq. in.

net Section

 $2 \times 4 \times 7/8 \times 3/8 = 2.62$ sq. in.Net Sec. = $10.88 - 2.62 = 8.26$ sq. in.

needed 6.0

Web will take Shear $v = 13000$ #/sq. in. $13000 \times 3/8 \times 20.4 = 91800$ #

Shear taken by one rivet

$$\frac{91800}{7} = 13114.3 \text{ #}$$

Bearing on one Rivet bearing = 27000 #/sq. in.

 $3/8 \times 3/4 \times 27000 = 7600$ #

Double Shear on one Rivet shear = 13500 #/sq. in.

 $2 \times .4418 \times 13500 = 11960$ #

13114.3 is greater than 7600; therefore there is nothing left to resist bending moment

The actual Max. V of Beams is 58770 #

Shear taken by one Rivet = $58770/7 = 7681.4$ #

Reaction to BM

$$R = \sqrt{7600^2 + 7681.4^2} = 1400 \text{ #}$$

BM due to Rivets

$$\frac{2 \times 1400}{47/8} \left[(15/8)^2 + (1/2)^2 + (47/8)^2 \right] = 21350 \text{ in. lbs.}$$

Beam Web Splice

Bending Moment possible of the web

$$1/8 \ 20.4 \ 3/8 \ 15000 \ 18.74 = 322500 \text{ in. lbs.}$$

BM the rivets will take is 21350 in. lbs.

Max. Bending Moment actually taken by web at this point

Max. Total BM at center 227670 ft. lbs. freely supported

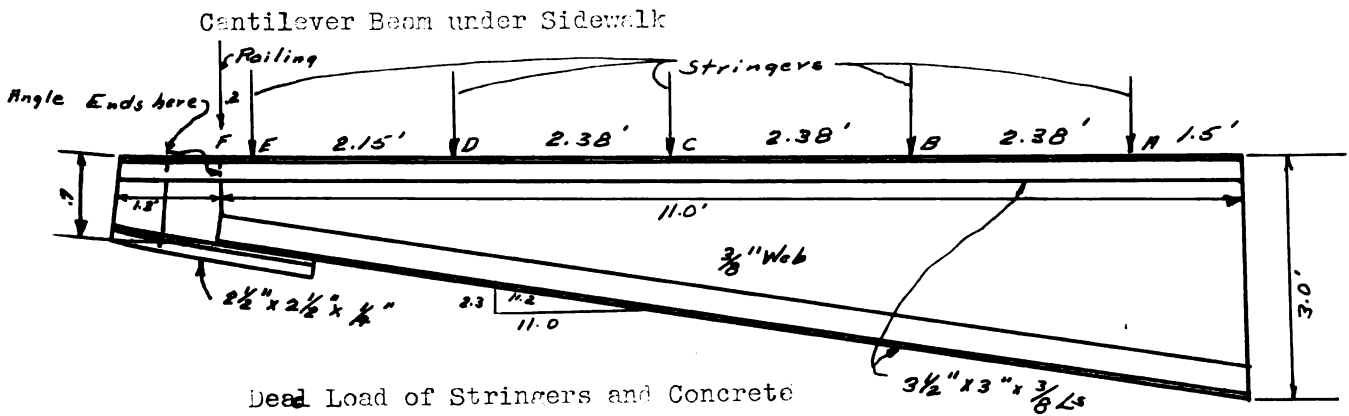
Continuity at end of Beam equals 5/6

$$5/6 \ 227670 \ 12 = 2275000 \text{ in. lbs.}$$

$$= \frac{1/8 \text{ web } 2275000}{\text{Gross Sec.}} = \frac{1/8 \ 20.4 \ 3/8}{4.6} \times 2275000$$

$$= 475000 \text{ in. lbs.}$$

BM the rivets will take
is 21350 in. lbs.



Dead Load of Stringers and Concrete

Panel Point A

$$\begin{aligned} & 5 \text{ in. concrete} \\ & \frac{5}{12} 150 \frac{(1 + 2.38)}{2} 15.4 = 1625 \# \\ & 6 \text{ in. @ 14.75 I} \\ & \frac{14.75}{12} 15.4 = \frac{227.5}{\text{tot. } 1952.5} \end{aligned}$$

Panel Points B and C

$$\begin{aligned} & 5 \text{ in. concrete} \\ & \frac{5}{12} 150 \frac{(2.38 + 2.38)}{2} 15.4 = 2290 \\ & 6 \text{ in. @ 14.75 I} = \frac{227.5}{\text{tot. } 2517.5} \end{aligned}$$

Panel Point D

$$\begin{aligned} & 5 \text{ in. concrete} \\ & \frac{5}{12} 150 \frac{(2.38 + 2.15)}{2} 15.4 = 2180 \\ & 6 \text{ in. @ 14.75 I} = \frac{227.5}{\text{tot. } 2407.5} \end{aligned}$$

Panel Point E

$$\begin{aligned} & 5 \text{ in. concrete} \\ & \frac{5}{12} 150 \frac{(2.15 + 0.2)}{2} 15.4 = 1134 \\ & 6 \text{ in. @ 14.75 I} = \frac{227.5}{\text{tot. } 1361.5} \end{aligned}$$

Railing Loading

Dead Load 15#/ft.

$$15 \times 15.4 = 231 \#$$

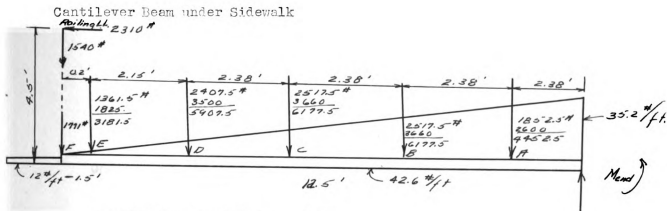
(25) Verticle Live Load 100 #/ft.

$$100 \times 15.4 = 1540 \#$$

Total Verticle Load $231 + 1540 = 1771 \#$

(25) Horizontal Live Load 150 #/ft.

$$150 \times 15.4 = 2310 \#$$



Bending Moment at End Max.

$$\begin{aligned}
 &4452.5 \cdot 1.5 + 6177.5 \cdot 3.88 + 6177.5 \cdot 6.26 + 5907.5 \cdot 8.64 + 3181.5 \cdot 10.8 \\
 &+ 1771 \cdot 11 + 1540 \cdot 11 + 2310 \cdot 4.5 + 42.6 \cdot 11 \cdot \frac{11}{2} + 12 \cdot 1.5 \cdot \frac{(1.5 + 11)}{2} \\
 &+ \frac{35.2}{2} \cdot 11 \cdot \frac{11}{3} = 189,727 \text{ ft. lbs.}
 \end{aligned}$$

Shear at End Max.

$$\begin{aligned}
 &4452.5 + 6177.5 + 6177.5 + 5907.5 + 3181.5 + 1540 + 1771 + 12 \cdot 1.5 + 42.6 \cdot 11 \\
 &+ \frac{35.2}{2} \cdot 11 = 29897.0 \#
 \end{aligned}$$

Bending Moment at A

$$\begin{aligned}
 &6177.5 \cdot 2.38 + 6177.5 \cdot 4.76 + 5907.5 \cdot 7.14 + 3181.5 \cdot 9.5 + 1771 \cdot 9.5 + 1540 \cdot 9 \\
 &+ 2310 \cdot 4.5 + 12 \cdot 1.5 \cdot \frac{(1.5 + 9.5)}{2} + 42.6 \cdot 9.5 \cdot \frac{9.5}{2} \\
 &+ \frac{9.5}{11} \cdot \frac{35.2}{2} \cdot \frac{9.5}{3} = 160,261.5 \text{ ft. lbs.}
 \end{aligned}$$

Shear at A

$$\begin{aligned}
 &4452.5 + 6177.5 + 6177.5 + 5907.5 + 3181.5 + 1771 + 1540 + 12 \cdot 1.5 \\
 &+ 42.6 \cdot 9.5 + \frac{35.2}{11} \cdot \frac{9.5}{2} \cdot \frac{9.5}{3} = 29774.5 \#
 \end{aligned}$$

Bending Moment at D

$$\begin{aligned}
 &3181.5 \cdot 2.15 + 1771 \cdot 2.35 + 1540 \cdot 2.35 + 2310 \cdot 4.5 + 12 \cdot 1.5 \cdot \frac{(1.5 + 2.35)}{2} \\
 &+ \frac{35.2}{11} \cdot \frac{2.35}{2} \cdot \frac{2.35}{3} + 42.6 \cdot 2.35 \cdot \frac{2.35}{2} = 27010.9 \text{ ft. lbs.}
 \end{aligned}$$

Shear at D

$$\begin{aligned}
 &5907.5 + 3181.5 + 1771 + 1540 + 12 \cdot 1.5 + 42.6 \cdot 2.35 \\
 &+ \frac{35.2}{11} \cdot \frac{2.35}{2} \cdot \frac{2.35}{3} = 12526.8 \#
 \end{aligned}$$

Cantilever Beam under Sidewalk

Bending Moment at F

$$2610 \cdot 4.5 + 12 \cdot 1.5 \cdot \frac{1.5}{2} = 10413.5 \text{ ft. lbs.}$$

Shear at F

$$1540 + 1771 + 12 \cdot 1.5 = 3389 \#$$

Check Cross Section at End of Cantilever Beam

$$M = 189727 \text{ ft. lbs} \quad V = 29887 \#$$

Gross Section

$$2\text{-angles @ } 2.3 \text{ sq. in.} \quad 4.6 \text{ sq. in.}$$

Net Section

$$-4 \text{ Rivets holes } 4 \cdot \frac{7}{8} \cdot \frac{3}{8} = \frac{-1.3 \text{ sq. in.}}{3.3 \text{ Net.}}$$

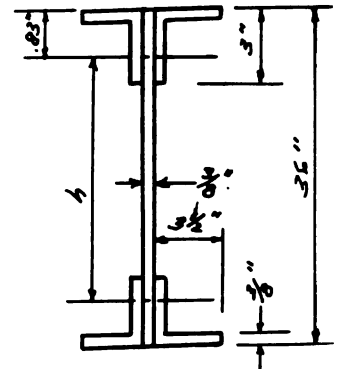
Tension Flange

$$f = 18000 \#/\text{sq. in.}$$

$$A = \frac{M}{f \cdot h} = \frac{1}{8} \text{ web}$$

$$3.3 = \frac{189727 \cdot 12}{18000 \cdot h} - \frac{1}{8} \cdot \frac{3}{8} \cdot 36$$

$$h = 35.4 \text{ in.} \quad \text{supplied } 34.34$$



Compression Flange

$$h = 36 - 2 \cdot .83 = 34.34 \text{ in.}$$

$$(47) \quad f = 18000 - 5 \frac{(L)^2}{(b)^2}$$

$$f = 18000 - 5 \frac{12^2}{(7/12)^2} = 15880 \#/\text{sq. in.}$$

$$A = \frac{189727 \cdot 12}{15880} - \frac{1}{8} \cdot \frac{3}{8} \cdot 36$$

$$A = 2.49 \text{ sq. in.} \quad \text{supplied } 4.6$$

Web

$$v = 12000 \#/\text{sq. in.} \quad \text{allowable}$$

$$v = \frac{V}{A} = \frac{29887}{3/8 \cdot 36} = 2220 \#/\text{sq. in.}$$

Cantilever Beam under Sidewalk

Check Cross Section at Panel Point A

$$BM = 160261.5 \text{ ft. lbs.} \quad V = 29774.5 \text{ #}$$

Gross Section 4.6 sq. in.

Net Section 3.3 sq. in.

Back to back of Flange angles

$$\text{dis.} = 3 - \frac{2.3 \times 1.5}{11} = 2.63 \text{ ft. or } 32.2 \text{ in.}$$

Tension Flange

$$f = 15000 \text{ #/sq. in.}$$

$$A = \frac{BM}{f h} = 1/8 \text{ web}$$

$$3.3 = \frac{160261.5 \times 12}{15000 h} = 1/8 \times 3/8 \times 32.2$$

$$h = 22.3 \text{ in.} \quad \text{supplied } 30.54$$

Compression Flange

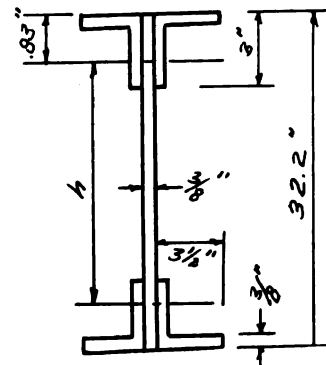
$$f = 15880 \text{ #/sq. in.}$$

$$A = \frac{160261.5 \times 12}{15880 \times 30.54} = 1/3 \times 3/8 \times 32.2$$

$$A = 2.47 \text{ sq. in.} \quad \text{supplied } 4.6$$

Web $v = 12000 \text{ #/sq. in.}$ allowable

$$v = \frac{V}{A} = \frac{29774.5}{3/8 \times 32.2} = 2360 \text{ #/sq. in.}$$



$$h = 32.2 - 2 \times 0.83 = 30.54 \text{ in.}$$

Cantilever Beam under Sidewalk

Check Cross Section at Panel Point D

$$BM = 27010.9 \text{ ft. lbs} \quad V = 12526.9 \text{ lb}$$

Cross Section 4.5 sq. in.

Net Section 3.3 sq. in.

Back to back of Flange angles

$$\text{dis. } 3 - \frac{2.3}{11} 8.64 = 1.2 \text{ ft. or } 14.4 \text{ in.}$$

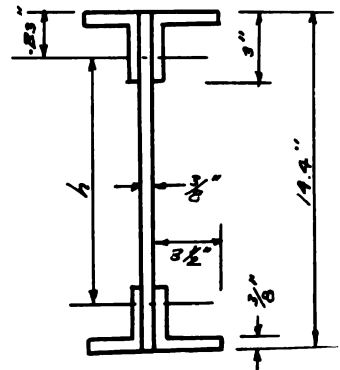
Tension Flange

$$f = 18000 \text{ #/sq. in.}$$

$$A = \frac{BM}{f h} - \frac{1}{8} \text{ web}$$

$$3.3 = \frac{27010.9 \times 12}{18000 h} - \frac{1}{8} 14.4 \times \frac{3}{8}$$

$$h = 14.4 \text{ in.} \quad \text{supplied } 12.54$$



$$h = 14.4 - 0.83 \times 2 = 12.54 \text{ in.}$$

Compression Flange

$$f = 15380 \text{ #/sq. in.}$$

$$A = \frac{27010.9 \times 12}{15380 \times 12.54} - \frac{1}{8} \times \frac{3}{8} \times 14.4$$

$$A = 0.951 \text{ sq. in.} \quad \text{supplied } 4.6$$

Web

$$v = 12000 \text{ #/in.} \quad \text{allowable}$$

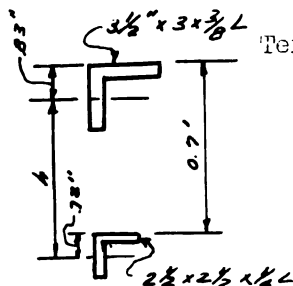
$$v = \frac{V}{A} = \frac{12526.8}{14.4 \times \frac{3}{8}} = 2320 \text{ #/sq. in.}$$

Cantilever Beam under Sidewalk

Check Cross Section at Panel Point F

$$BM = 10413.5 \text{ ft. lbs.}$$

$$V = 3329 \text{ #}$$



Tension Flange

$$f = 18000 \text{ #/sq. in.}$$

Gross Section angle-3/8 by 3¹/₂ by 3 @ 2.3 sq. in.

$$A = \frac{BM}{f h} = \frac{10413.5 \text{ lb}}{18000 \times 8.29}$$

$$A = .64 \text{ sq. in.} \quad \text{supplied } 2.3$$

$$h = 7.62 + .72 - .05$$

$$= 8.29"$$

Compression Flange

$$f = 18000 \text{ #/sq. in.}$$

Gross Section angle-2¹/₄ by 2¹/₄ by 1 @ 1.19 sq. in.

$$A = \frac{10413.5 \text{ lb}}{18000 \times 8.29} = 0.952 \text{ sq. in.}$$

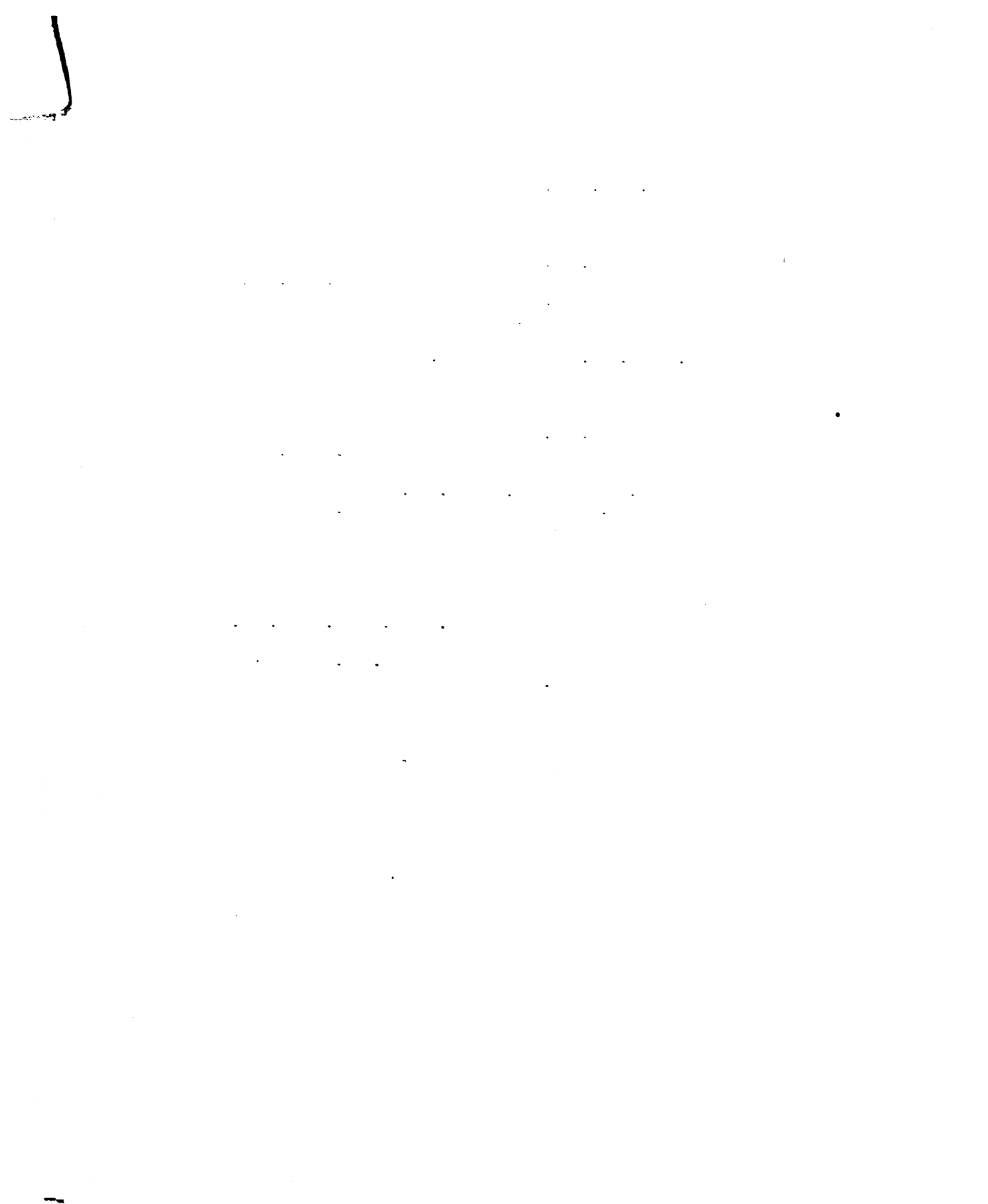
$$\text{supplied } 1.19$$

No web present here; therefore Flanges must take **shear**

$$\text{Total } A \text{ of Flanges} \quad 1.19 + 2.3 = 3.49 \text{ sq. in.}$$

$$v = \frac{V}{A} = \frac{3329}{3.49} = 953 \text{ #/sq. in.}$$

The Flanges have enough extra Area over what is
needed for Compression and Tension to take
care of this Shear.

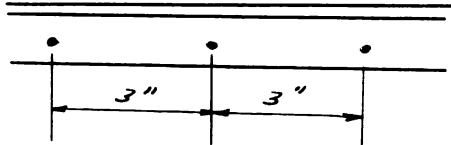


Rivets in Cantilver Beam (from the end to first stringer)

Shear at End = 39337 #

$h = 30.54$ in. at Panel Point A

Flange Angle Rivets



Load on top of Flange

$$DL + LLV = 4452.5 \text{ #}$$

$$\text{Average Distance between stringers} = \frac{2.32 + 1.5}{2} = 1.94 \text{ ft.}$$

$$w = \frac{4452.5}{1.94} = 2295 \text{ #/ft.}$$

Bearing of 3/4 Rivet on 3/8 Web 7600 #

Double Shear of 3/4 Rivet 11960

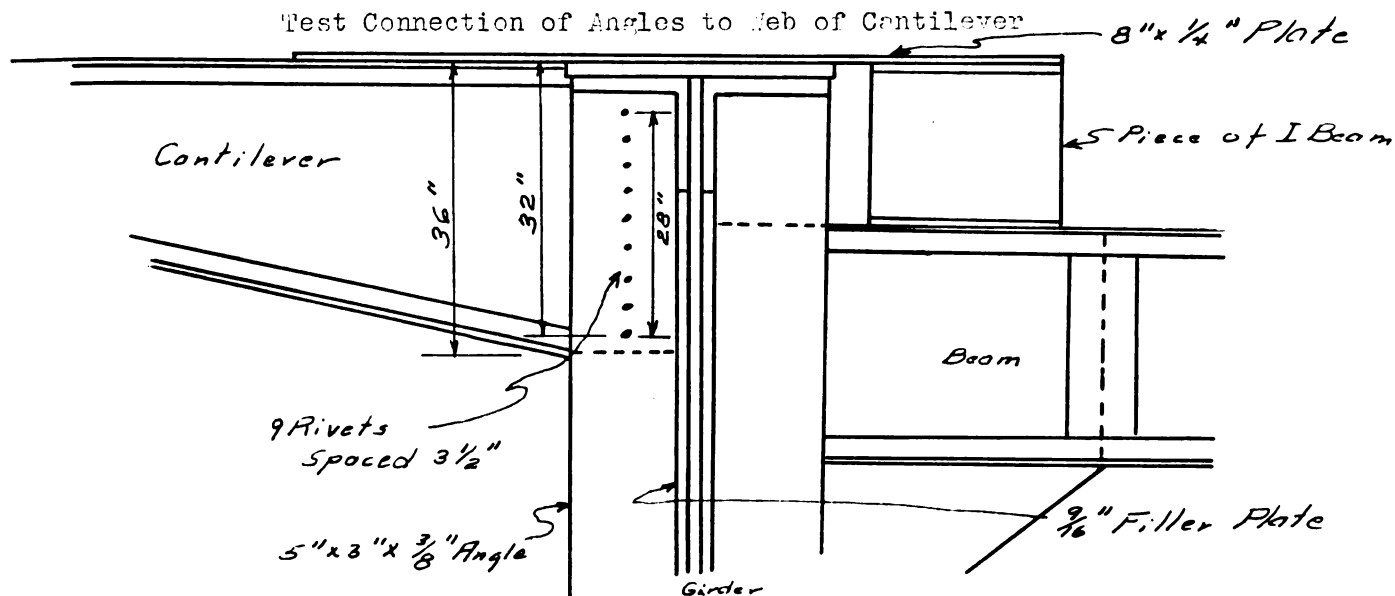
$$HI = \frac{V}{h} \times \frac{A_f}{A_f + A_{w/2}} = \frac{39337}{30.54} \times \frac{4.6}{4.6 + 1.51} = 735 \text{ #}$$

$$\text{Pitch} = \frac{R}{\sqrt{HI^2 + w^2}} = \frac{7600}{\sqrt{735^2 + (2295/12)^2}} = \begin{matrix} 8 \text{ in. supplied} \\ 3 \text{ in.} \end{matrix}$$

The Rivets in the rest of the
Flange are 6 in. (no need to test)

Connection of Cantilever to Girder

Test Connection of Angles to Web of Cantilever



Total V of Cantilever and Beam (V is the Reaction of Beams)

$$53420 + 2967 = 23307 \#$$

Bearing on 3/8 web by 3/4 Rivet

$$27000 \times \frac{3}{8} \times \frac{3}{4} = 7600 \#$$

Double Shear of 3/4 Rivet

$$2.443 \times 13500 = 11930 \#$$

Shear taken by each Rivet

$$\frac{29227}{9} = 3231 \#$$

BM at end of Cantilever = 189727 ft. lbs.

Reaction of Rivets for Bending Moment

$$R = \sqrt{7600^2 - 3320^2} = 6940 \#$$

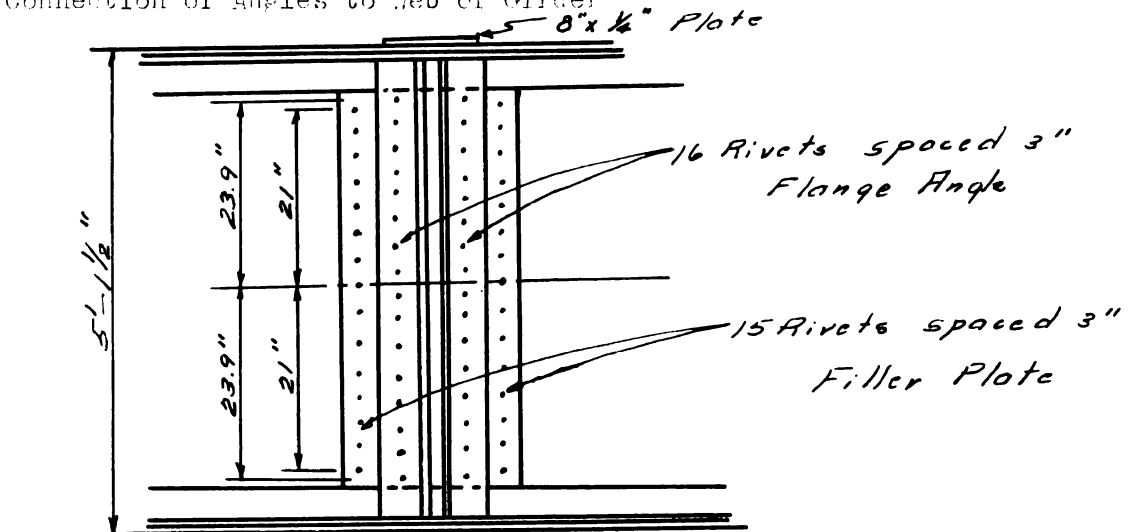
$$BM = \frac{2 \times 6940}{14} (14^2 + 10.5^2 + 7^2 + 3.5^2) = 359000 \text{ in. lbs. supplied}$$

or 29100 ft. lbs.
189727 needed

The difference in BM supplied and that needed is offset by having a 1/4 by 8 in. Plate on top of cantilever and attach to beam on other side of Girder.

Connection of Cantilever to Girder

Best Connection of Angles to Web of Girder



Total V of Cantilever and Beam (V is the Reaction of beams)
 $53420 + 29887 = 83307 \#$

Bearing on $3/4$ web and $2 \times 9/16$ bearing $27000 \#/\text{sq. in.}$
 $27000 (3/4 + 2 \times 9/16) = 56000 \#$

Double Shear of $3/4$ Rivet
 $2 \times .443 \times 13500 = 11960 \#$

Number of Rivets for Shear = $\frac{83307}{11960} = 7$ Rivets
 supplied 32
 16 in each angle
 or 30 in Filler Plate

Bending Moment at end of Cantilever = 189727 ft. lbs.

$1/4$ by 8 in. Plate takes Tension while the bearing of angle on web of girder takes the compression

Assumed Neutral Axis at neutral axis of the cantilever at the end.

BM = $8 \times 16000 \times 36 = 1152000 \text{ in. lbs.}$
 or 96000 ft. lbs. supplied
 189727 ft. lbs. needed

GIRDERS

Girders

Cross Section of Girders

2 angles-9/16 by 6 1/4 by 6 1/4 in.

13.4 sq. in.

1 CP-9/16 by 14 1/4 in.

9.02

total 21.42 sq. in.

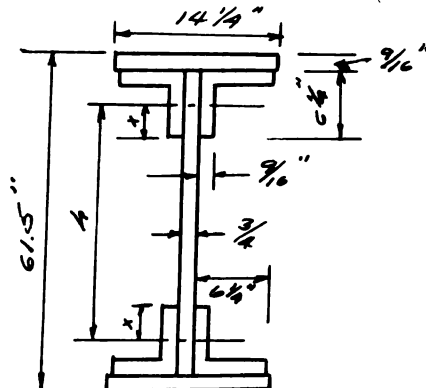
$$(33) \quad \begin{array}{l} 4 \text{ Holes } 4 \ 9/16 \ 7/8 = 1.97 \text{ sq. in.} \quad \text{angles} \\ 2 \text{ Holes } 2 \ 7/8 \ 9/16 = 1.0 \text{ sq. in.} \quad \text{CP} \end{array}$$

$$(33) \quad x = 1 - \frac{S^2}{4 h c}$$

$$x = 1 - \frac{6^2}{4 \ 21 \frac{1}{4} \ 7/8} = -2.164 \quad \text{or } 0 \text{ to be deducted}$$

$$\text{Net Section } 21.42 - 1.97 - 1.0 = 18.45 \text{ sq. in.}$$

Find h (h dist. from center of gravity of the flanges)



$$21.45 x = \frac{2 \ 25 \ 9 \ 25}{4 \ 16 \ 8} + \frac{2 \ 128 \ 9 \ 121}{56 \ 16 \ 32} + \frac{57 \ 9 \ 309}{4 \ 16 \ 32}$$

$$x = 5.14 \text{ in.}$$

$$h = 61.5 - 2 (6.89 - 5.24) = 48.34 \text{ in.}$$

Compression of extreme fiber of rolled sections and built up girder

$$(46) \quad = 18000 - 5 (L/b)^2$$

$$= 18000 - \frac{5 (15.4 \ 18)^2}{(14 \ 25)^2} = 17187.5 \text{ #/sq. in.}$$

Weight of the Girder #/ft.

$$\begin{array}{rcl} 2\text{-CP } 9/16 \text{ in. by } 14\frac{1}{2} \text{ in. } 60 \text{ ft. long @ } 27.3 \text{ \#} & & \\ 27.3 \times 60/66 & = & 24.9 \text{ \#/ft.} \end{array}$$

$$3/4" \text{ Web } 5 \text{ ft. lin. @ } 153 \text{ \#} \quad 153$$

$$4 \text{ angles } 6\frac{1}{2} \text{ by } 6\frac{1}{2} \text{ by } 9/16 \text{ in. @ } 22.2 \text{ \#} \quad 91.2$$

Concrete over Girder (girder II, III, IV)

$$\begin{array}{rcl} \left(\frac{2.2 + 2.01}{2} \right) \cdot 0.5 \cdot 150 + 1.5 \left(\frac{23/4 + 27/8}{2} \right) 150 & = & 205.9 \\ & & \text{total } 474.9 \text{ \#/ft.} \end{array}$$

$$\begin{array}{rcl} 8\text{-Int. Stiffeners } 3/8 \text{ by } 3 \text{ by } 5 \text{ in. @ } 9.8 \text{ \#} & & \\ 5 \times 8 \times 9.8 & = & 196 \text{ \#} \end{array}$$

$$1000 \text{ Rivets @ } 12 \text{ \#/100 heads } \quad 12 \times 20 = 240$$

$$\begin{array}{rcl} 12\text{-End Stiffeners } 3/8 \text{ by } 3 \text{ by } 5 \text{ in. @ } 9.8 \text{ \#} & & \\ 12 \times 5 \times 9.8 & = & 294 \end{array}$$

$$\begin{array}{rcl} \text{Sway Bracing } 2\text{-} 2\frac{1}{2} \text{ by } 3 \text{ by } \frac{1}{2} \text{ in. angles} & & \\ @ 4.5 \quad 22.5 \times 2 \times 4.5 & = & 202.5 \end{array}$$

$$\begin{array}{rcl} 20\text{-Filler Plates } 9/16 \text{ by } 5/1 \text{ in. @ } 5.74 \text{ \#} & & \\ 4 \times 20 \times 5.74 & = & 459 \end{array}$$

$$\begin{array}{rcl} 2\text{-CP Splice } 5/8 \text{ by } 14\frac{1}{2} \text{ in. @ } 30.3 \text{ \#} & & \\ 4.9 \times 30.3 \times 2 & = & 298 \\ & & \text{total } 1682.5 \text{ \#} \end{array}$$

$$w = 474.9 + \frac{1682.5}{66} = 501 \text{ say } 510 \text{ \#/ft.}$$

Girder I

Dead Load

Cons. Dead Load

Max. Reaction of Beam between Girder I and II 11840 #
 Max. reaction of Canilever Beam 29887

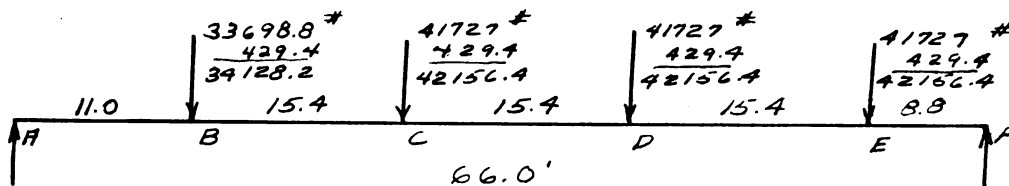
Panel Point -O one beam and one canilever 41727 #
 " " -D one beam and one ca illever 41757
 " " -E one beam and one canilever 41827
 " " -B $\frac{11840 + 12.1}{15.4} \frac{11840}{2} = 10870$ Beam

$$\frac{29887.0}{2} + \frac{29887.0 (11 - 11.4.4)}{15.4 \cdot 2} = 23128.8 \text{ canilever}$$

$$\text{total DL at B } 23128.8 + 10870 = 34098.8 \#$$

wt. of connection of beam and canilever to girder = 429.4 #

Uniform Dead Load same as Girder V 640.9 #/ft say 641



Max. Dead Load Bending Moment
 DLBM at C

$$\frac{42156.4 \cdot 26.4}{66} (2.8 + 24.2 + 39.6) + \frac{34128.2 \cdot 55 \cdot 26.4}{66} - \frac{42128.2 \cdot 15.4}{66} = 1451 \text{ KF Max.}$$

DLBM at D

$$+ \frac{641 \cdot 66^2}{8} = \frac{35}{1485} \text{ KF Total}$$

$$\frac{42156.4 \cdot 24.2}{66} (26.4 + 41.8 + 57.2) + \frac{34128.2 \cdot 11 \cdot 24.2}{66} - \frac{42156.4 \cdot 15.4}{66}$$

$$= 1480.4 \text{ KF}$$

Max. Dead Load Shear
 DLV at EF

$$+ \frac{641 \cdot 66}{8} = \frac{35}{1485.4} \text{ KF Total}$$

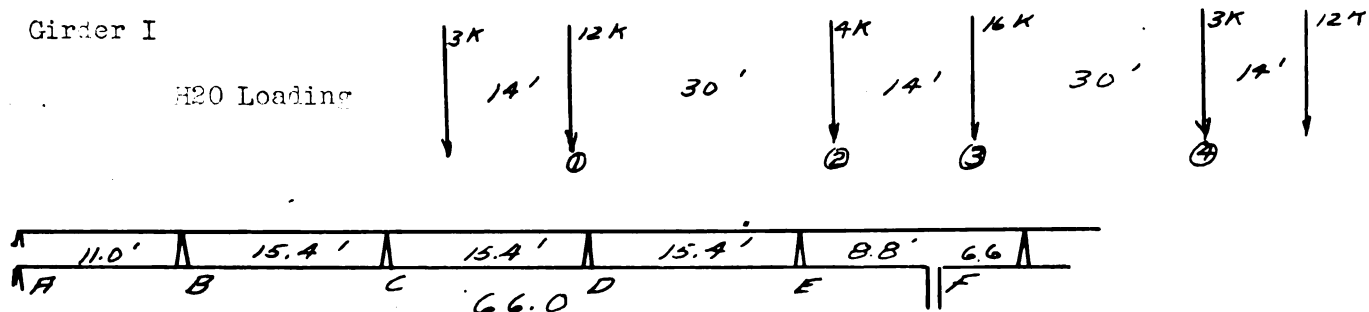
$$\frac{34128.2 \cdot 11}{66} + \frac{42156.4 (26.4 + 41.8 + 57.2)}{66} + \frac{641 \cdot 66}{2} = 107030 \# \text{ Max.}$$

DLV at AB

$$\frac{42156.4 (8.8 + 24.2 + 39.6)}{66} + \frac{34128.2 \cdot 55}{66} + \frac{641 \cdot 66}{2} = 95850 \#$$

Girder I

H20 Loading



Max. Live Load Bending Moment one wheel of a train of trucks

LLBM at C

Load 1 at C

$$16 \frac{2.2 \cdot 8.8 \cdot 26.4}{15.4 \cdot 66} + 4 \frac{9.6 \cdot 26.4}{66} + \frac{12 \cdot 39.6 \cdot 26.4}{66} + \frac{3 \cdot 53.6 \cdot 26.4}{66} - 3 \cdot 14 = 236 \text{ KF}$$

Load 2 at C

$$3 \frac{2.2 \cdot 8.8 \cdot 26.4}{15.4 \cdot 66} + 16 \frac{24.2 \cdot 26.4}{66} + \frac{4 \cdot 39.6 \cdot 26.4}{66} = 220 \text{ KF}$$

Load 3 at C

$$12 \frac{2.2 \cdot 8.8 \cdot 26.4}{15.4 \cdot 66} + 3 \frac{9.6 \cdot 26.4}{66} + \frac{16 \cdot 39.6 \cdot 26.4}{66} + \frac{4 \cdot 53.6 \cdot 26.4}{66} - 4 \cdot 14 = 301 \text{ KF}$$

LLBM at D

Load 1 at D

$$3 \frac{27.8 \cdot 24.2}{66} + \frac{12 \cdot 41.8 \cdot 24.2}{66} + 4 \frac{0.8 \cdot 57.2 \cdot 24.2}{15.4 \cdot 66} - \frac{0.8 \cdot 4 \cdot 15.4}{15.4} = 215.2 \text{ KF}$$

Load 2 at D

$$\frac{16 \cdot 10.2 \cdot 41.8}{66} + \frac{4 \cdot 24.2 \cdot 41.8}{66} + \frac{12 \cdot 54.2 \cdot 41.8}{66} - 12 \cdot 30 = 217 \text{ KF}$$

Load 3 at D

$$4 \frac{27.8 \cdot 24.2}{66} + 16 \frac{41.8 \cdot 24.2}{66} + \frac{3 \cdot 0.8 \cdot 57.2 \cdot 24.2}{15.4 \cdot 66} - \frac{3 \cdot 0.8 \cdot 15.4}{15.4} = 222 \text{ KF}$$

Max. Live Load Shear one wheel of train of trucks

LLV at AB

Load 2 at B

$$\frac{12 \cdot 3.6 \cdot 9.3}{15.4 \cdot 66} + \frac{3 \cdot 11}{66} + \frac{16 \cdot 41}{66} + \frac{4 \cdot 55}{66} = 14.13 \text{ K}$$

Load 3 at B

$$\frac{12 \cdot 11 \cdot 3 \cdot 25}{66} + \frac{16 \cdot 55}{66} = 16.45 \text{ K}$$

Girder I

Max. Live Load Shear -cont.

LLV at EB

Load 1 at E

$$\frac{12 \ 13.2}{66} + \frac{3 \ 43.2}{66} + \frac{12 \ 57.2}{66} = 14.75 \text{ K}$$

Load 2 at E

$$\frac{16 \ 14 \ 57.2}{15.4 \ 66} + \frac{4 \ 57.2}{66} + \frac{12 \ 37.2}{66} + \frac{3 \ 13.2}{66} = 10.23 \text{ K}$$

Load 3 at E

$$\frac{16 \ 57.2}{66} + \frac{4 \ 43.2}{66} + \frac{12 \ 13.2}{66} = 18.89 \text{ K Max.}$$

Bending Moment and Shear Totals

Max. LLBM (1 wheel) 371 KF
 Max. LLV (1 wheel) 18.89 K

Impact* 20.6%

Max. Reaction at Girder I is same as Girder V

$$\frac{27}{16.5}$$

$$\text{Total LLBM } \frac{371 \ 27}{16.5} \ 120.6 \% = 593 \text{ KF}$$

$$\text{Total LLV } \frac{18.89 \ 27}{16.5} \ 120.6 \% = 37.5 \text{ K}$$

Max. DLBM 1486 K
 Max. DLV 107030 #

$$\begin{aligned} \text{Total Max. BM} & 1486 + 593 = 2079 \text{ KF} \\ \text{Total Max. V} & 107030 + 37500 = 144530 \# \end{aligned}$$

Girder I

Dead Load Shear at BC

$$\frac{42155.4}{66} (8.8 + 24.2 + 59.6) + \frac{34128.2}{66} \frac{55}{2} + \frac{641}{2} \frac{66}{2} \\ - \frac{54128.2}{11} \frac{641}{66} = 54570.8 \#$$

Dead Load Shear at CD

$$\frac{34128.2}{66} \frac{11}{66} + \frac{42155.4}{66} (26.4 + 41.8 + 57.2) + \frac{641}{2} \frac{66}{2} \\ - \frac{42155.4}{2.8} \frac{641}{66} = 59232.8 \# \quad \text{Max.}$$

Live Load Shear at BC 120 Loading 1 wheel of train of trucks

Load 2 at C

$$3 \frac{2.2}{15.4} \frac{8.8}{66} + \frac{16}{66} \frac{25.6}{66} + \frac{4}{66} \frac{39.6}{66} = 8.68 \text{ K}$$

Load 3 at C

$$12 \frac{2.2}{15.4} \frac{8.8}{66} + \frac{3}{66} \frac{9.6}{66} + \frac{16}{66} \frac{39.6}{66} + \frac{4}{66} \frac{53.6}{66} - \frac{4}{15.4} \frac{14}{66} = 9.86 \text{ K}$$

Live Load Shear at DE

Load 2 at D

$$12 \frac{11.8}{66} + \frac{4}{66} \frac{41.8}{66} + \frac{16}{66} \frac{55.8}{66} + \frac{16}{15.4} \frac{14}{66} = 3.69 \text{ K}$$

Load 3 at D

$$\frac{4}{66} \frac{27.8}{66} + \frac{16}{66} \frac{41.8}{66} + \frac{3}{15.4} \frac{57.8}{66} - \frac{3}{15.4} \frac{8}{66} = 13.3 \text{ K} \quad \text{Max.}$$

Total Shear at DE

Max. Reaction at Girder I of 1/2 load on each wheel across Girder
(Reaction same as Girder II) 27/16.5

Impact = 20.6 %

$$\text{Total LLV} = \frac{13.3}{16.5} \frac{27}{16.5} 120.6 \% = 26.3 \text{ K}$$

KLV at DE = 59232.8 #

$$\text{Total V at DE} = 26300 + 59232.8 = 85532.8 \#$$

Girder I

Check Girder Cross Section

Gross Section of Flange 21.42 sq. in.

Net " " " 18.45

Web 3/4 in. by 60 3/8 in.

h equals 58.34 in.

Tension Flange

$$f = 18000$$

$$A = \frac{RM}{h f} = 1/8 \text{ of web}$$

$$18.45 = \frac{2079000 \cdot 12}{h \cdot 18000} = 1/8 \cdot 3/4 \cdot 603/8$$

$$h = 57.3 \text{ in. supplied } 58.34 \text{ in.}$$

Compression Flange

$$f = 17157.5 \text{ \#/sq. in.}$$

$$A = \frac{2079000 \cdot 12}{18000 \cdot 58.34} = 1/8 \cdot 3/4 \cdot 603/8$$

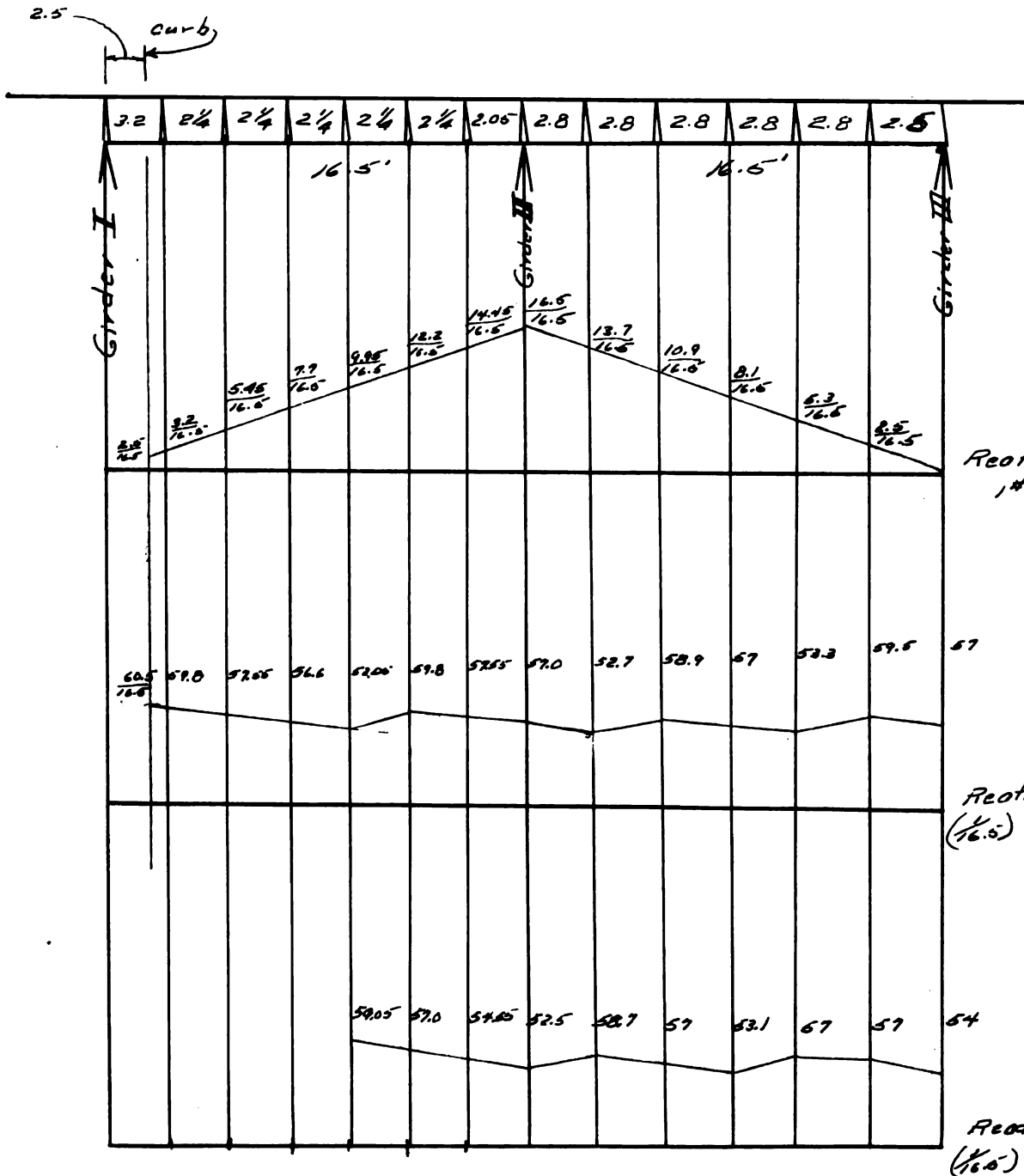
$$A = 18.12 \text{ sq. in. supplied } 21.42$$

Web

$$v = 12000 \text{ allowable}$$

$$v = \frac{V}{A} = \frac{144530}{3/4 \cdot 603/8} = 3190 \text{ \# per sq. in.}$$

Max. Reaction at Girder II
& Girder IV
Influence Lines
for Traffic Lanes



Dead Load

Conc. Dead Load

Max. Reaction of Beam between Girder	Land II	12320
" " " " " "	II and III	11020
Panel Points B,C,D, and E	-----	tot. 23940

wt. of connections of two beams to girder

4-3/8 by 3 by 5 angles 4 5 9.8 = 1 67

2- back plates 9/16 2 4 1 490 9 = 134

16 13

2- triangles of web of beam 3/8 (lower side)

2 3 15 2.3 490 = 44

8 12 12 2

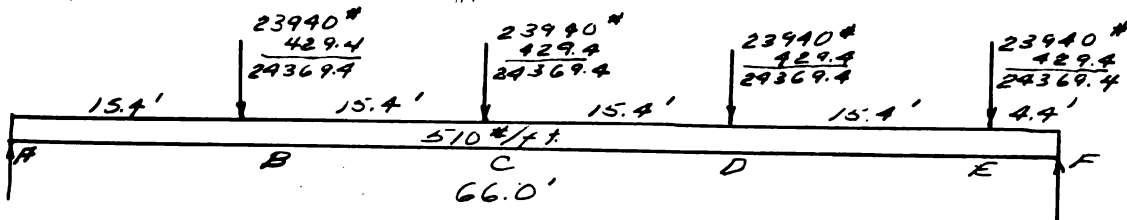
2- triangles of web of beam 3/8 (upper side)

2 3 15 2.3 490 = 5.77

8 12 12 2

tot. 429.4 #

Uniform Load 510 #/ft.



Max. Dead Load Bending Moment

DLBM at C

$$\frac{24369.4}{66} \cdot 50.8 (4.4 + 19.8 + 35.2 + 50.6) - \frac{24369.4}{66} \cdot 15.4 + \frac{510 \cdot 66^2}{8} = 902.9 \text{ LF}$$

Max. Dead Shear

DLV at AB

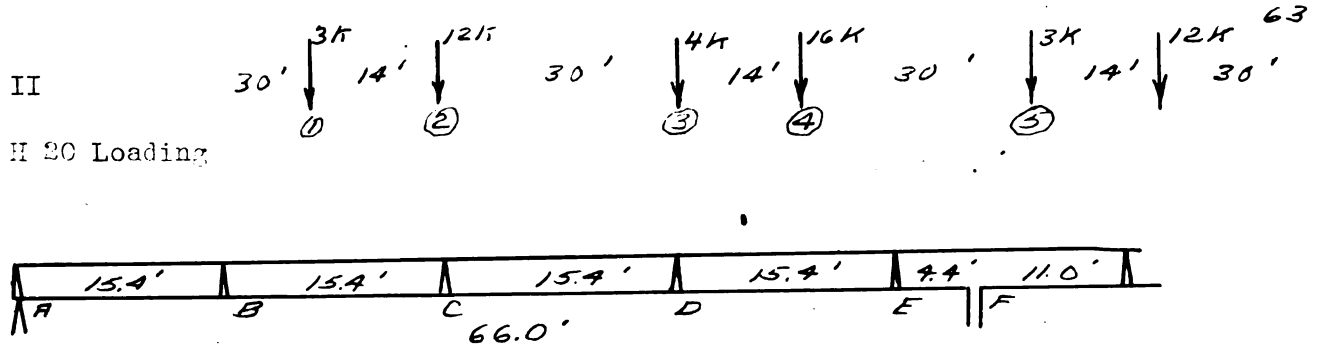
$$\frac{24369.4}{66} (4.4 + 19.8 + 35.2 + 50.6) + \frac{510 \cdot 66}{2} = 57445.7 \text{ #}$$

DLV at EF

$$\frac{24369.4}{66} (15.4 + 30.8 + 46.2 + 61.6) + \frac{510 \cdot 66}{2} = 73630 \text{ #}$$

Girder II

H 20 Loading



Max. Live Load Bending Moment

one wheel of a train of trucks

LLBM at C

Load 2 at C

$$\begin{aligned} & 3 \frac{16.2 \cdot 35.2}{66} + 12 \frac{30.8 \cdot 35.2}{66} + 4 \frac{60.8 \cdot 35.2}{66} + 16 \frac{2.2 \cdot 61.6 \cdot 35.2}{15.4 \cdot 66} \\ & - 4 \cdot 30 - 16 \frac{2.2 \cdot 30.8}{15.4} = 238.5 \text{ KF} \end{aligned}$$

Load 3 at C

$$\begin{aligned} & 12 \frac{0.8 \cdot 35.2}{66} + 4 \frac{30.8 \cdot 35.2}{66} + 16 \frac{44.8 \cdot 35.2}{66} + 3 \frac{2.2 \cdot 61.6 \cdot 35.2}{15.4 \cdot 66} \\ & - 16 \cdot 14 - 3 \frac{2.2 \cdot 30.8}{15.4} = 230.8 \text{ KF} \end{aligned}$$

Load 4 at C

$$\begin{aligned} & 4 \frac{16.2 \cdot 35.2}{66} + 16 \frac{30.8 \cdot 35.2}{66} + 3 \frac{60.8 \cdot 35.2}{66} + 12 \frac{2.2 \cdot 61.6 \cdot 35.2}{15.4 \cdot 66} \\ & - 3 \cdot 30 - 12 \frac{2.2 \cdot 30.8}{15.4} = 304.5 \text{ KF Max.} \end{aligned}$$

Load 5 at C

$$\begin{aligned} & 16 \frac{0.8 \cdot 35.2}{66} + 3 \frac{30.8 \cdot 35.2}{66} + 12 \frac{44.8 \cdot 35.2}{66} + 3 \frac{2.2 \cdot 61.6 \cdot 35.2}{15.4 \cdot 66} \\ & - 12 \cdot 14 - 3 \frac{2.2 \cdot 30.8}{15.4} = 175.3 \text{ KF} \end{aligned}$$

Max. Live Load Shear

LLV at AB

Load 2 at B

$$3 \frac{1.4 \cdot 50.6}{15.4 \cdot 66} + 12 \frac{30.6}{66} + 4 \frac{20.6}{66} + 16 \frac{6.6}{66} = 12.24 \text{ K}$$

Load 3 at B

$$4 \frac{50.6}{66} + 16 \frac{36.6}{66} + 3 \frac{6.6}{66} + 12 \frac{3.6 \cdot 4.4}{66} = 12.43 \text{ K}$$

Girder II

Max. Liv. Load Shear -cont.

LLV at AB

Load 4 at B

$$4 \frac{1.4 \cdot 50.6}{15.4 \cdot 66} + \frac{16 \cdot 50.6}{66} + \frac{3 \cdot 30.6}{66} + \frac{12 \cdot 6.6}{66} = 14.68 \text{ K}$$

LLV at EF

Load 3 at E

$$3 \frac{17.6}{66} + \frac{12 \cdot 31.6}{66} + \frac{4 \cdot 61.6}{66} + \frac{16 \cdot 1.4 \cdot 61.6}{15.4 \cdot 66} = 11.62 \text{ K}$$

Load 4 at E

$$\frac{16 \cdot 61.6}{66} + \frac{4 \cdot 47.6}{66} + \frac{12 \cdot 17.6}{66} + \frac{3 \cdot 3.6}{66} = 21.2 \text{ K Max.}$$

Bending Moment and Shear Totals

Max. LLBM	(1 wheel) H20	304.5	KF
Max. LLV	(1 wheel) H20	21.2	K

(37) Impact 20.6 %

(33) 4 Lanes 80%

Max. Reaction at Girder II of 1- Load each wheel across Girder $\frac{60.5}{16.5}$

Total LLBM 304.5 120.6% 80% $\frac{60.5}{16.5} = 1075 \text{ KF}$

Total LLV 21.2 120.6% 80% $\frac{60.5}{16.5} = 75 \text{ K}$

Max. DLBM	777.7	902.9	KF
Max. DLV		73630	K

Total Max. BM 1075 + 902.9 = 1977.9 KF

Total Max. V at EF 75000 + 73630 = 148630 K

Girder II

Dead Load Shear at DE

$$\frac{24369.4}{66} (15.4 + 30.8 + 46.2 + 61.6) + \frac{510 \cdot 66}{2} - 24369.4 - 4.4 \cdot 510 = 47016.6 \# \quad \text{Max.}$$

Dead Load Shear at EC

$$\frac{24369.4}{66} (4.4 + 19.8 + 35.2 + 50.6) + \frac{510 \cdot 66}{2} - 24369.4 - 15.4 \cdot 510 = 25222.3 \#$$

Live Load Shear at DE H20 Loading 1 wheel of train of trucks

Load 3 at D

$$3 \frac{2.2}{66} + 12 \frac{16.2}{66} + 4 \frac{46.2}{66} + 16 \frac{61.6}{66} - \frac{16 \cdot 14}{15.4} = 6.25 \text{ K}$$

Load 4 at D

$$12 \frac{2.2}{66} + 4 \frac{22.2}{66} + 16 \frac{46.2}{66} + 3.8 \frac{61.6}{66} - \frac{3 \cdot 3}{15.4} = 13.544 \text{ K} \quad \text{Max.}$$

Live Load Shear at EC H20 Loading 1 wheel of train of trucks

Load 3 at C

$$3 \frac{2.2 \cdot 4.4}{15.4 \cdot 66} + 16 \frac{21.2}{66} + 4 \frac{35.2}{66} + 12 \frac{55.2}{66} - 12 = 7.3 \text{ K}$$

Load 4 at C

$$12 \frac{2.2 \cdot 4.4}{15.4 \cdot 66} + 3 \frac{5.2}{66} + 16 \frac{35.2}{66} + 4 \frac{49.2}{66} - \frac{4 \cdot 14}{15.4} = 8.23 \text{ K}$$

Total Shear at DE

Max. Reaction at Girder II of 1st load on each wheel across Girder
60.5/16.5

Impact 20.6 %

4 Lanes 80 %

$$\text{Total LLV} = 13.544 \frac{60.5}{16.5} 120.6 \% 80 \% = 48 \text{ K}$$

$$\text{DLV at DE} = 47016.6 \#$$

$$\text{Total V at DE} = 48000 + 47016.6 = 95016.6 \#$$

Check Girder Cross Section

Gross Section of Flange 21.42 sq. in.
 let " " " 18.45
 Web $3/4$ in. by 60 $3/8$ in.
 h equals 58.34 in.

Tension Flange

$$f = 18000$$

$$A = \frac{M}{h f} = 1/4 \text{ of web}$$

$$18.45 = \frac{1977900 \cdot 12}{18000 h} = 1/4 \cdot 3/4 \cdot 603/8$$

$$h = 58.6 \text{ in. supplied } 58.34 \text{ in.}$$

Compression Flange

$$f = 17187.5 \text{ #/in.}^2$$

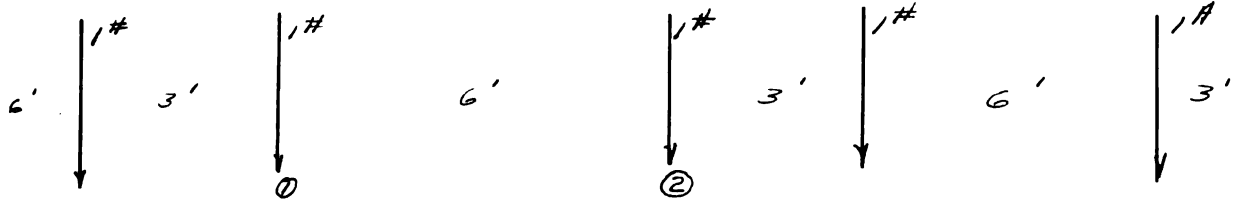
$$A = \frac{1977900 \cdot 12}{17187.5 \cdot 58.34} = 1/4 \cdot 3/4 \cdot 603/8$$

$$A = 18.04 \text{ sq. in. supplied } 21.42$$

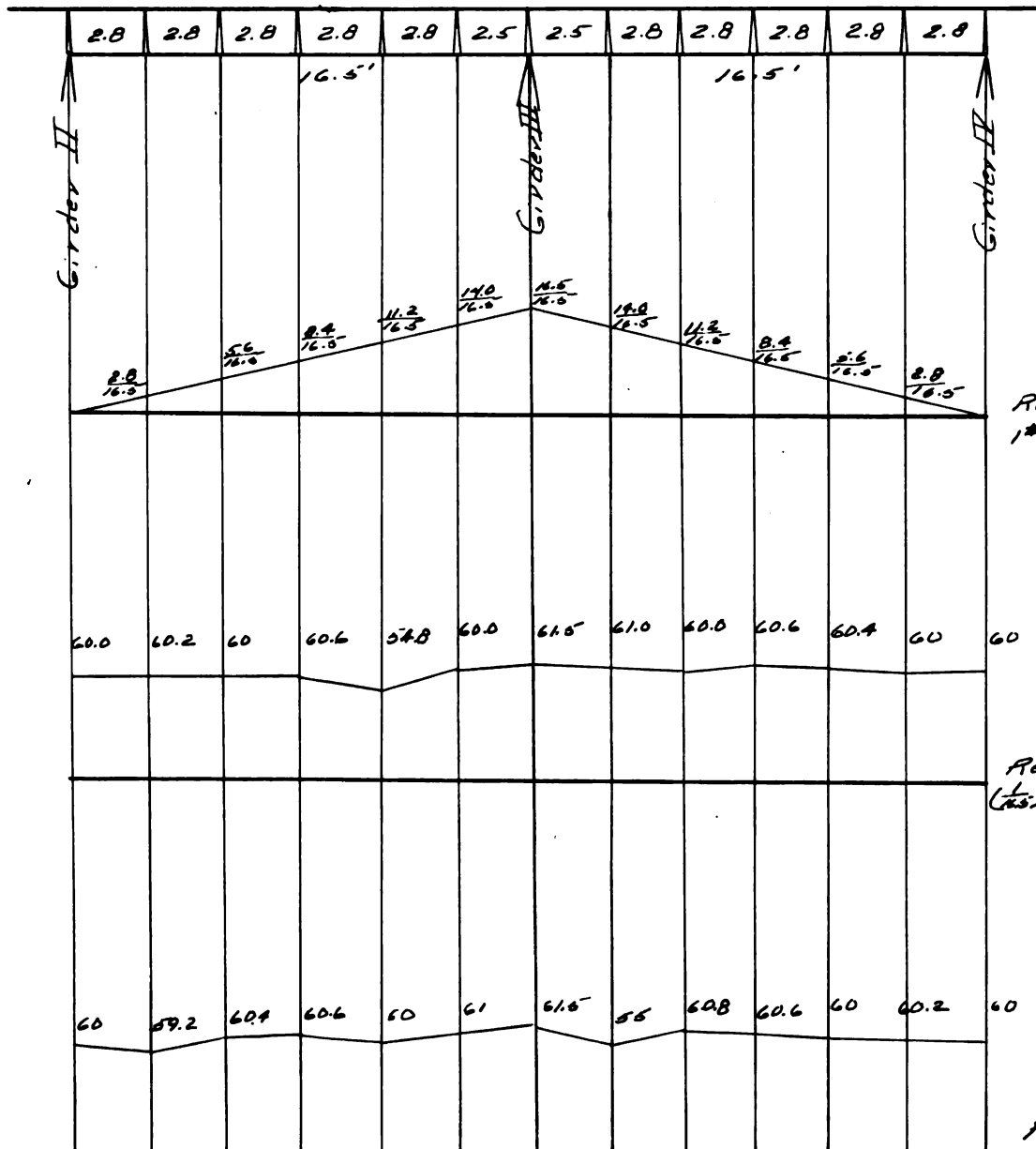
Web

$$v = 12000 \text{ allowable}$$

$$v = \frac{V}{A} = \frac{148630}{603/8 \cdot 3/4} = 3790 \text{ #/in.}^2$$



Max. Reaction at Girder III
Influence Lines for Traffic Lanes.



Reaction at III
1# Load Influence
Lines

Reaction at III
(1/16) Load

Reaction at III
(1/16) Load

Dead Load

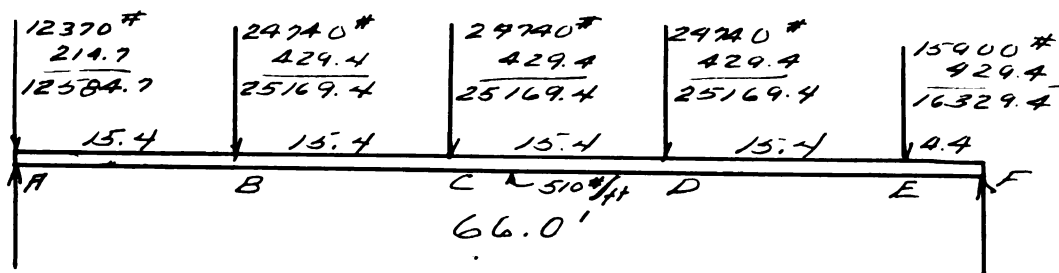
Cons. Dead Load

Reactions of Beam between Girder III and II, and Girder III and IV
 $12370 \frac{L}{ft}$

Point-A	one beam	$12370 \frac{L}{ft}$
" -B	two beam	24740
" -C	" "	24740
" -D	" "	24740
" -E	$24740 + \frac{4.4}{15.4} 24740 = 15900$	

wt. of connection of two beams to girder $429.4 \frac{L}{ft}$

Uniform Load $510 \frac{L}{ft}$



Max. Dead Load Bending Moment

DLEM at C

$$\frac{16329.4 \times 4.4 \times 30.8}{66} + \frac{25169.4 \times 30.8}{66} (19.8 + 35.2 + 50.6) - 25169.4 \times 15.4 + \frac{510 \times 66^2}{8} = 913.9 \text{ KF}$$

Max. Dead Load Shear

DLV. at AB

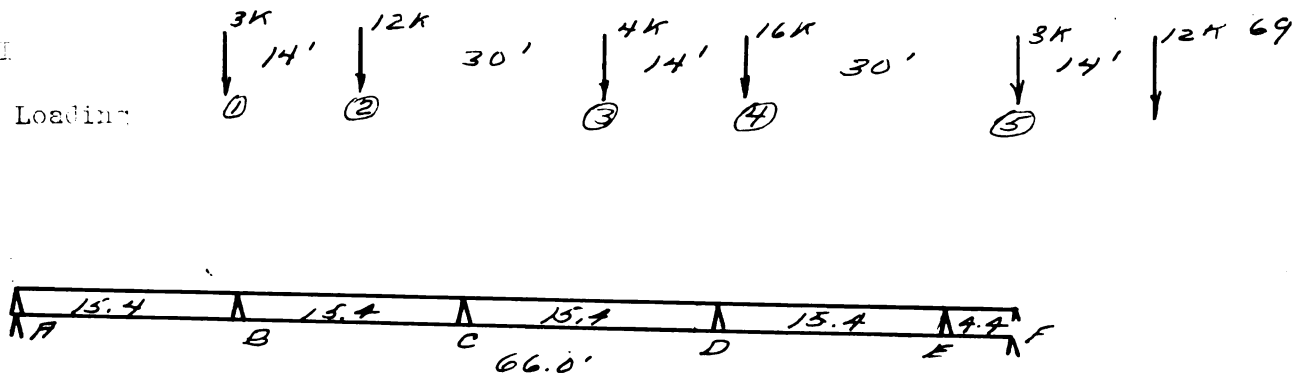
$$\frac{16329.4 \times 4.4}{66} + \frac{25169.4}{66} (19.8 + 35.2 + 50.6) + \frac{510 \times 66}{11} = 59.13 \text{ K}$$

DLV. at EF

$$\frac{25169.4}{66} (15.4 + 30.8 + 46.2) + \frac{16329.4 \times 61.6}{66} + 510 \times 66 = 67.07 \text{ K}$$

Ex. 111

120 Loading



Max. Live Load Bending Moment

one wheel of a train of trucks

LLM at C

Load 2 at C

$$4 \frac{52.2 \cdot 30.8}{66} + 12 \frac{35.2 \cdot 30.8}{66} + 3 \frac{49.2 \cdot 30.8}{66} - 3 \cdot 14 = 232 \text{ K}$$

Load 3 at C

$$16 \frac{21.2 \cdot 30.8}{66} + 4 \frac{35.2 \cdot 30.8}{66} + 12 \frac{65.2 \cdot 30.8}{66} - 12 \cdot 30 = 229 \text{ K}$$

Load 4 at C

$$3 \frac{5.2 \cdot 30.8}{66} + 16 \frac{35.2 \cdot 30.8}{66} + 4 \frac{49.2 \cdot 30.8}{66} + 4 \cdot 14 = 306 \text{ LF Max.}$$

Max. Live Load Shear

one wheel of a train of trucks

LLV. at AB

Load 2 at B

$$16 \frac{6.6}{66} + 4 \frac{20.6}{66} + 12 \frac{50.6}{66} + \frac{3 \cdot 14 \cdot 50.6}{15.4 \cdot 66} = 12.25 \text{ K}$$

Load 3 at B

$$3 \frac{6.6}{66} + 16 \frac{36.6}{66} + 4 \frac{50.6}{66} = 12.24 \text{ K}$$

Load 4 at B

$$12 \frac{0.166}{66} + 3 \frac{20.6}{66} + 16 \frac{50.6}{66} + \frac{4 \cdot 1.4 \cdot 50.6}{15.4 \cdot 66} = 14.62 \text{ K}$$

Max V at AB

Girder III

Max. LLV - cont.

LLV. at EF

Load 2 at E

$$\frac{3 \ 3.6}{66} + \frac{12 \ 17.6}{66} + \frac{3 \ 47.6}{66} + \frac{12 \ 61.6}{66} = 16.74 \text{ K}$$

Load 3 at E

$$\frac{3 \ 17.6}{66} + \frac{12 \ 31.6}{66} + \frac{4 \ 61.6}{66} = 18.7 \text{ K}$$

Load 4 at E

$$\frac{3 \ 3.6}{66} + \frac{12 \ 17.6}{66} + \frac{4 \ 47.6}{66} + \frac{16 \ 61.6}{66} = 21.15 \text{ K Max.}$$

Load 6 at E

$$\frac{4 \ 3.6}{66} + \frac{16 \ 17.6}{66} + \frac{3 \ 47.6}{66} + \frac{12 \ 61.6}{66} = 17.85 \text{ K}$$

BENDING MOMENT and SHEAR TOTALS

Max. LLBM (1 wheel) H20 306 KF

Max. LLV (1 wheel) H20 21.15 K

$$(37) \text{ Impact} \quad \frac{L + 20}{6L + 20} = \frac{66 + 20}{6 \cdot 66 + 20} = 20.6\%$$

(33) 4 Lanes 80%

Max. Reaction at Girder III of 1 Load each wheel across Girder $\frac{61.5}{16.5}$

$$\text{Total LLBM} = 306 \cdot 130.6 \cdot 80\% \cdot \frac{61.5}{16.5} = 1100 \text{ KF}$$

$$\text{Total LLV} = 21.15 \cdot 120.6 \cdot 80\% \cdot \frac{61.5}{16.5} = 76 \text{ K}$$

Max. DLBM 913.9 KF

Max. LLV 67.07 K

$$\text{Total Max. BM} \quad 1100 + 913.9 = 2013.9 \text{ KF}$$

$$\text{Total Max. V at EF} \quad 76 + 67.07 = 143.07 \text{ K}$$

Girder III

Dead Load Shear at DE

$$\frac{25169.4}{66} (15.4 + 50.8 + 46.2) + \frac{16329.4}{66} \frac{61.6}{2} + \frac{510}{2} \frac{66}{2} - 16329.4 - 510 \cdot 4.4 = 4426.6 \text{ # Max.}$$

Dead Load Shear at BC

$$\frac{16329.4}{66} \frac{4.4}{66} + \frac{25169.4}{66} (19.8 + 35.2 + 50.6) + \frac{510}{2} \frac{66}{2} - 25169.4 - 15.4 \cdot 510 = 25157.6 \text{ #}$$

Live Load Shear at BC H20 Loading 1 wheel of train of trucks

Load 3 at C

$$16 \frac{21.2}{66} + 4 \frac{35.2}{66} + 12 \frac{65.2}{66} - 12 = 7.17 \text{ K}$$

Load 4 at C

$$3 \frac{5.2}{66} + 16 \frac{35.2}{66} + 4 \frac{47.2}{66} - 4 \frac{1.4}{15.4} = 8.12 \text{ K}$$

Live Load Shear at DE H20 Loading 1 wheel of train of trucks

Load 3 at D

$$3 \frac{2.2}{66} + 12 \frac{16.2}{66} + 4 \frac{46.2}{66} + 16 \frac{60.2}{66} - \frac{16 \cdot 14}{15.4} = 5.71 \text{ K}$$

Load 4 at D

$$12 \frac{2.2}{66} + 4 \frac{32.2}{66} + 16 \frac{46.2}{66} = 13.52 \text{ K Max.}$$

Total Shear at DE

Max. Reaction at Girder III of 1st load on each wheel across Girder
61.5/16.5

Impact 20.6 %

4 Lanes 80 %

$$\text{Total LLM} = 13.52 \frac{61.5}{16.5} \cdot 120.6 \% \cdot 80 \% = 49.7 \text{ K}$$

DLV at DE = 44496.6 #

$$\text{Total V at DE} = 49700 + 44496.6 = 94196.6 \text{ #}$$

Girder III

Check Girder Cross Section

Gross Section of Flange 21.42 sq. in.
 Net " " " 18.45
 Web 3/4 in. by 60 3/8 in.
 h equals 58.34 in.

Tension Flange

$$f = 18000 \text{ #/in}^2$$

$$A_s = \frac{BM}{R f} \quad \text{--- } 1/8 \text{ of web}$$

$$18.45 = \frac{2013900 \cdot 12}{18000 \cdot R} \quad \text{--- } 1/8 \text{ } 603/8 \text{ } 3/4$$

$$h = 55.6 \text{ in. supplied h of } 58.34 \text{ in.}$$

Compression Flange

$$f = 18000 \text{ #/in}^2$$

$$A = \frac{2013900 \cdot 12}{17187.5 \cdot 58.34} \quad \text{--- } 1/8 \text{ } 603/8 \text{ } 3/4$$

$$A = 18.44 \text{ in}^2 \quad \text{supplied } 21.45 \text{ in}^2$$

Web

$$v = 12000 \text{ #/in}^2 \quad \text{allowable}$$

$$v = \frac{V}{A}$$

$$v = \frac{143070}{603/8 \text{ } 3/4} = 3160 \text{ #/in}^2$$

Girder IV

Dead Load

Conc. Dead Load

Max. Reaction of Beam between Girder III and IV

11020 #

" " " " " IV " V

12920

 2940

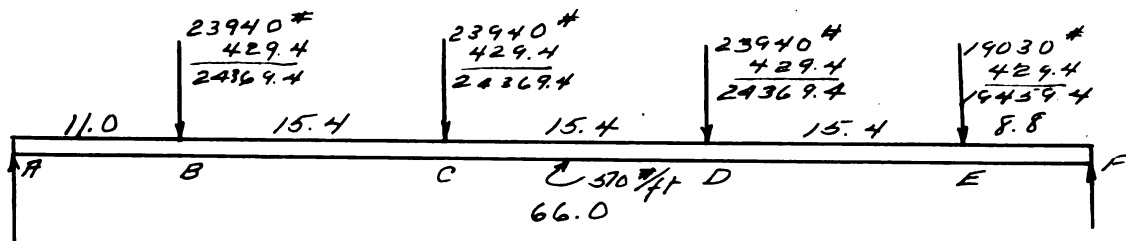
Panel Point -B two beams 23940
 " " -C two beams 23940
 " " -D two beams 23940
 " " -E

$$\frac{11020}{2} + \frac{11020 \times 27.7}{2 \times 15.4} = 3420$$

$$\frac{12920}{2} + \frac{12920 \times 9.9}{2 \times 15.4} = 12610$$

$$\text{total DL at } \frac{3420 + 12610}{2} = 13030$$

Uniform Dead Load 510 #/ft.



Max. Dead Load Bending Moment

DLBM at C

$$\frac{19459.4 \times 8.8 \times 26.4}{66} + \frac{24369.4 \times 26.4 \times (24.2 + 39.6 + 55)}{66} - 24369.4 \times 15.4 + \frac{510 \times 66^2}{8} = 871.9 \text{ KF}$$

DLBM at D

$$\frac{24369.4 \times 24.2 \times (11 + 26.4 + 41.8)}{66} + \frac{19459.4 \times 24.2 \times 57.2}{66} - 19459.4 \times 15.4 + \frac{510 \times 66^2}{8} = 830.9 \text{ KF}$$

Max. Dead Load Shear

DLV at B

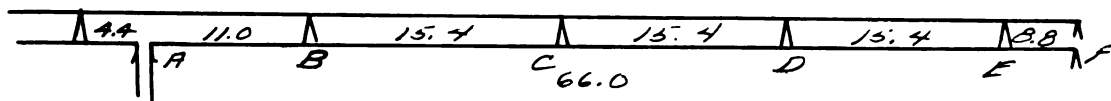
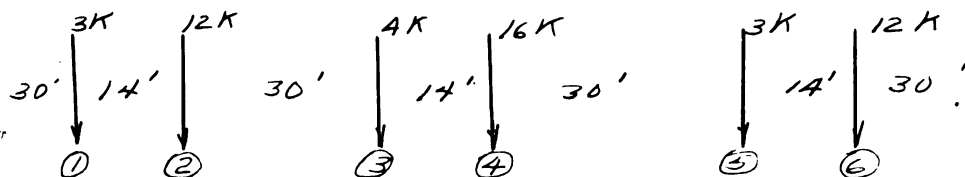
$$\frac{19459.4 \times 8.8}{66} + \frac{24369.4 \times (24.2 + 39.6 + 55)}{66} + \frac{510 \times 66}{2} = 63.02 \text{ K}$$

DLV at EF

$$\frac{24369.4 \times (11 + 26.4 + 41.8)}{66} + \frac{19459.4 \times 57.2}{66} + \frac{510 \times 66}{2} = 62.53 \text{ K}$$

Circle IV

H 50 Loading



Max. Live Load Bending Moment one wheel of a train of trucks

LLSM at C

Load 2 at C

$$3 \frac{13.4 \cdot 30.6}{66} + 12 \frac{26.4 \cdot 30.6}{66} + 4 \frac{56.4 \cdot 30.6}{66} - 30.4 = 228 \text{ KF}$$

Load 3 at C

$$4 \frac{30.6 \cdot 26.4}{66} + 16 \frac{26.4 \cdot 26.4}{66} + 12 \frac{0.2 \cdot 55 \cdot 26.4}{15.4 \cdot 66} - 12 \frac{0.2 \cdot 15.4}{15.4} = 231.1 \text{ KF}$$

Load 4 at C

$$4 \frac{12.4 \cdot 30.6}{66} + 12 \frac{26.4 \cdot 30.6}{66} + 3 \frac{56.4 \cdot 30.6}{66} - 3 \cdot 30 = 225 \text{ KF Max.}$$

LLSM at D

Load 4 at D

$$16 \frac{41.8 \cdot 24.2}{66} + 4 \frac{27.8 \cdot 24.2}{66} + 12 \frac{2.2 \cdot 11 \cdot 24.2}{15.4 \cdot 66} = 223 \text{ KF}$$

Load 5 at D

$$4 \frac{2.2 \cdot 11 \cdot 24.2}{15.4 \cdot 66} + 16 \frac{11.8 \cdot 24.2}{66} + 3 \frac{41.8 \cdot 24.2}{66} + \frac{12 \cdot 55.8 \cdot 24.2}{66} - 12 \cdot 14 = 195 \text{ KF}$$

Load 6 at D

$$12 \frac{41.8 \cdot 24.2}{66} + 3 \frac{27.8 \cdot 24.2}{66} + 16 \frac{2.2 \cdot 11 \cdot 24.2}{15.4 \cdot 66} = 277.5 \text{ KF}$$

Girder IV

Max. Live Load Shear one wheel of a train of trucks

LLV at E

Load 2 at E

$$\frac{3 \frac{1.4 \text{ 55}}{15.4 \text{ 66}} + \frac{12 \text{ 55}}{66} + \frac{4 \text{ 15}}{66} + \frac{16 \text{ 11}}{66} = 14.95 \text{ K}$$

Load 3 at E

$$\frac{4 \text{ 38}}{66} + \frac{16 \text{ 41}}{66} + \frac{3 \text{ 11}}{66} = 13.76 \text{ KF}$$

Load 4 at E

$$\frac{12 \text{ 11}}{66} + \frac{3 \text{ 35}}{66} + \frac{16 \text{ 55}}{66} + \frac{4 \frac{1.4 \text{ 55}}{15.4 \text{ 66}}}{66} = 16.76 \text{ K}$$

LLV at E

Load 3 at E

$$\frac{3 \frac{15.2}{66} + \frac{12 \text{ 27.2}}{66} + \frac{4 \frac{57.3}{66}}{66} = 9 \text{ K}$$

Load 4 at E

$$\frac{3 \frac{3.6 \text{ 11}}{15.4 \text{ 66}} + \frac{12 \text{ 17.2}}{66} + \frac{4 \text{ 43.2}}{66} + \frac{16 \frac{57.2}{66}}{66} = 19 \text{ K Max.}$$

Load 5 at E

$$\frac{4 \frac{13}{66} + \frac{16 \text{ 27.2}}{66} + \frac{3 \frac{57.2}{66}}{66} = 9.93 \text{ K}$$

Bending Moment and Shear Totals

Max. LLBM at C (1 wheel) 890 895 KF

Max. LLV at E (1 wheel) 890 19 K

(27) Impact 20.6 K

(3) 4 Lanes 890 K

Max. Reaction at Girder IV of 1 $\frac{1}{2}$ Load each wheel across Girder $\frac{60.5}{16.5}$

$$\text{Total LLBM } 895 \frac{120.6}{13.5} 890 \frac{60.5}{13.5} = 1047 \text{ KF}$$

$$\text{Total LLV } 19 \frac{120.6}{16.5} 890 \frac{60.5}{16.5} = 82.2 \text{ K}$$

Max. DLRM 873.9 KF

Max. DLV 62.53 K

$$\text{Total Max. BM } 1047 + 873.9 = 1920.9 \text{ KF}$$

$$\text{Total Max. V } 82.2 + 62.53 = 144.73 \text{ K}$$

Girder IV

Dead Load Shear At BC

$$\frac{19459.4 \times 8.8}{66} + \frac{24369.4 (24.2 + 39.6 + 55)}{66} + \frac{510 \times 66}{2} - 24369.4 - 11 \times 510 = 33040.6 \#$$

Dead Load Shear at DE

$$\frac{24369.4 (11 + 26.4 + 41.8)}{66} + \frac{19459.4 \times 57.2}{66} + \frac{510 \times 66}{2} - 19459.4 - 510 \times 8.8 = 34582.3 \# \quad \text{Max.}$$

Live Load Shear at BC H20 Loading 1 wheel of train of trucks

Load 5 at C

$$\frac{16 \times 25.6}{66} + \frac{4 \times 32.6}{66} + \frac{8 \times 12.65}{15.4 \times 66} - \frac{8 \times 12}{15.4} = 8.5 \text{ K}$$

Load 4 at C

$$\frac{3 \times 9.6}{66} + \frac{16 \times 39.6}{66} + \frac{4 \times 57.6}{66} - \frac{4 \times 14}{15.4} = 9.76 \text{ K}$$

Live Load Shear at DE H20 Loading 1 wheel of train of trucks

Load 3 at D

$$\frac{8 \times 2.2 \times 11}{15.4 \times 66} + \frac{12 \times 11.8}{66} + \frac{4 \times 41.8}{66} + \frac{16 \times 52.8}{66} - \frac{16 \times 14}{15.4} = 3.74 \text{ K}$$

Load 4 at D

$$\frac{12 \times 2.2 \times 11}{15.4 \times 66} + \frac{4 \times 57.8}{66} + \frac{16 \times 41.8}{66} = 12.1 \text{ K} \quad \text{Max.}$$

Total Shear at DE

Max. Reaction at Girder IV of 1/2 load on each wheel across Girder
60.5/16.5

Impact 20.6 %

4 Lanes 80 %

$$\text{Total LL} = 12.1 \times \frac{60.5}{16.5} \times 120.6 \times 80 \% = 48.9 \text{ K}$$

DLV at DE = 32582.3 #

$$\text{Total V at DE} = 48900 + 32582.3 = 81382.3 \#$$

Girder IV

Check Girder Cross Section

Gross Section of Flange 21.42 sq. in.
 Net " " " 18.45
 Web 3/4 in. by 60 3/8 in.
 h equals 52.34 in.

Tension Flange

$$f = 18000$$

$$A = \frac{BM}{s \cdot f} - 1/8 \text{ of web}$$

$$18.45 = \frac{1220200 \cdot 12}{18000 \cdot h} - 1/8 \cdot 3/4 \cdot 603/8$$

$$h = 52.2 \text{ in. supplied } 52.34$$

Compression Flange

$$f = 17157.5$$

$$A = \frac{1220200 \cdot 12}{17157.5 \cdot 52.34} - 1/8 \cdot 3/4 \cdot 603/8$$

$$A = 17.44 \text{ supplied } 21.45 \text{ sq. in.}$$

Web

$$v = 12000 \text{ allowable}$$

$$v = \frac{V}{A} = \frac{124730}{3/4 \cdot 603/8} = 2760 \text{ #/ sq. in.}$$

Girder V

Dead Load

Conc. Dead Load

Max. Reaction of Beam between Girder V and IV 11840 #
 Max. Reaction of Cantilever Beam 29887

Panel Point-B one beam and one cantilever 41727 #
 Panel Point-C one beam and one cantilever 41727 #
 Panel Point-D one beam and one cantilever 41727 #
 Panel Point-E $\frac{1}{2} 11840 + \frac{12.1}{15.4} \frac{11840}{2} = 10580$ Beam
 $\frac{1}{2} 29887 + \frac{(13.2+1.47)}{15.4} \frac{29887}{2} = 29173.5$ Cantilever
 Total DL at E $10580 + 29173.5 = 39753.5$ #

wt. of connection of beam and cantilever to girder 429.4 #

Uniform Load #/ft.

2 CP 24.8 #/ft.
 web 153.0
 4 angles 91.2
 concrete over girder
 $\left(\frac{1.2}{2} + .5\right) .5 = 1.05$ sq. in.
 $\frac{(1.6 + .5) .5}{12} = 0.9$
 $.5 \frac{7}{12} = \frac{0.3}{12}$
 tot. 2.25 sq. in.
 conc. load 1688.5 #

$$w = \frac{1688.5}{66} + 24.8 + 153 + 91.2 + 2.25 \frac{150}{66} = 640.9 \text{ #/ft.}$$

say 641

Max. Dead Bending Moment

DLBM at C

$$\frac{40182.9}{66} \frac{13.2}{2} + \frac{42156.4}{66} \frac{22}{2} (23.6 + 44 + 59.4) + \frac{641}{8} \frac{66^2}{2} = 42156.4 \frac{15.4}{2}$$

= 1416667.0 ft. lbs.

DLBM at D

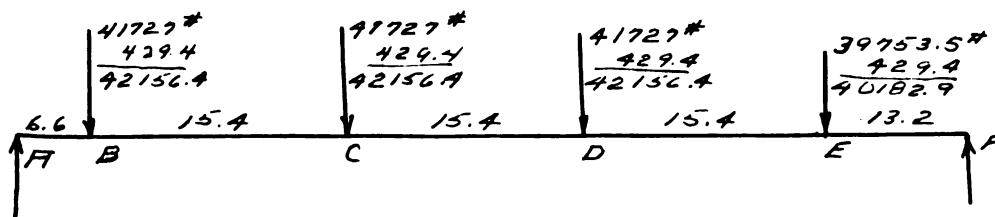
$$\frac{42156.4}{66} (6.6 + 22 + 37.4) \frac{23.6}{2} + \frac{40182.9}{66} \frac{52.8}{2} \frac{23.6}{2} - \frac{40182.9}{66} \frac{15.4}{2}$$

$$+ \frac{641}{8} \frac{66^2}{2} = 1345000 \text{ ft. lbs.}$$

Max. Dead Load Shear

DLV at AB

$$\frac{40182.9}{66} \frac{13.2}{2} + \frac{42156.4}{66} (23.6 + 44 + 59.4) + \frac{641}{2} \frac{66}{2} = 113502.8 \text{ #}$$



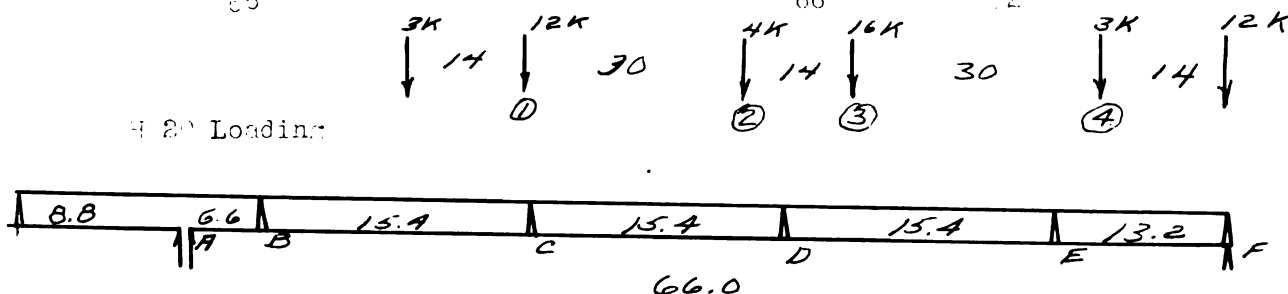
Girder V

Max. Dead Load Shear -cont.

DLV at LF

$$\frac{4 \times 156.4}{66} (0.6 + 22 + 37.4) + 4 \times 102.9 \frac{52.6}{66} + 641 \frac{66}{12} = 94406.4$$

4 20' Loading



Max. Live Load Bending Moment

one wheel of a train of trucks

LLBM at C

Load 1 at C

$$4 \frac{14 \cdot 22}{66} + \frac{12 \cdot 44 \cdot 11}{66} + \frac{3 \cdot 51 \cdot 22}{66} - 3 \cdot 14 = 144 \text{ KF}$$

Load 2 at C

$$16 \frac{30 \cdot 22}{66} + 4 \frac{44 \cdot 22}{66} = 204 \text{ KF}$$

Load 3 at C

$$3 \frac{14 \cdot 22}{66} + \frac{16 \cdot 44 \cdot 22}{66} + \frac{4 \cdot 58 \cdot 22}{66} - 4 \cdot 14 = 270 \text{ KF}$$

LLBM at D

Load 2 at D

$$16 \frac{51.4 \cdot 22.6}{66} + 4 \frac{37.4 \cdot 22.6}{66} + \frac{12 \cdot 7.4 \cdot 22.6}{66} - 16 \cdot 14 = 236 \text{ KF}$$

Load 3 at D

$$16 \frac{22.6 \cdot 37.4}{66} + 4 \frac{23.4 \cdot 22.6}{66} = 300 \text{ KF} \quad \text{Max.}$$

Load 4 at D

$$16 \frac{7.4 \cdot 22.6}{66} + 3 \frac{37.4 \cdot 22.6}{66} + \frac{12 \cdot 51.4 \cdot 22.6}{66} - 12 \cdot 14 = 199 \text{ KF}$$

Girder V

Max. Live Load Shear one wheel of a train of trucks

LLV at AE

Load 1 at B

$$\frac{16 \cdot 15.4}{66} + \frac{4 \cdot 59.4}{66} + \frac{12 \cdot 59.4}{66} + \frac{3 \cdot 1.4 \cdot 59.4}{15.4 \cdot 66} = 16.6 \text{ K}$$

Load 2 at

$$\frac{3 \cdot 15.4}{66} + \frac{16 \cdot 45.4}{66} + \frac{4 \cdot 59.4}{66} = 15.3 \text{ K}$$

Load 3 at B

$$\frac{12 \cdot 15.4}{66} + \frac{5 \cdot 29.4}{66} + \frac{16 \cdot 59.4}{66} + \frac{4 \cdot 1.4 \cdot 59.4}{66 \cdot 15.4} = 18.86 \text{ K Max.}$$

LLV at EF

Load 2 at E

$$\frac{3 \cdot 8.8}{66} + \frac{12 \cdot 32.8}{66} + \frac{4 \cdot 52.8}{66} = 9.75 \text{ K}$$

Load 3 at E

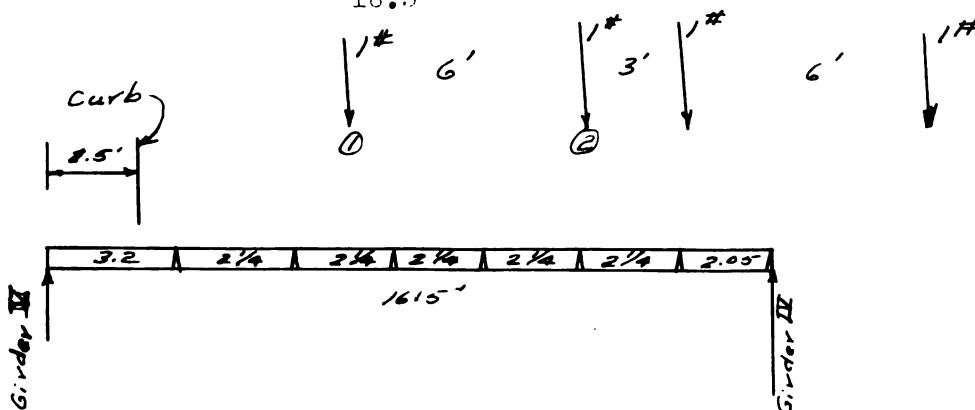
$$\frac{3 \cdot 6.6 \cdot 6.6}{15.4 \cdot 66} + \frac{12 \cdot 8.8}{66} + \frac{4 \cdot 32.8}{66} + \frac{16 \cdot 52.8}{66} = 16.83 \text{ K}$$

Load 4 at E

$$\frac{4 \cdot 8.8}{66} + \frac{16 \cdot 32.8}{66} + \frac{5 \cdot 52.8}{66} = 9.45 \text{ K}$$

Max. Reaction at Girder I of 1st Load on each wheel across Girder
 // and Max. when wheel 1 is closest to curb

$$16.5 (14 + 5 + \dots) = \frac{27}{16.5}$$



Girder V

Dead Load Shear at DL

$$\frac{42156.4}{66} (6.6 + 22 + 37.4) + \frac{40182.9}{66} \frac{52.8}{2} + \frac{641}{2} \frac{66}{2} - 40182.9 - 13.2 \frac{641}{2} = 46762.3 \#$$

Dead Load Shear at BC

$$\frac{40182.9}{66} \frac{13.2}{2} + \frac{42156.4}{66} (28.6 + 44 + 59.4) + \frac{641}{2} \frac{66}{2} - 42156.4 - 6.6 \frac{641}{2} = 67115.8 \# \text{ Max.}$$

Live Load Shear at BC H20 Loading 1 wheel of train of trucks

Load 2 at C

$$\frac{16}{66} \frac{30}{66} + \frac{4}{66} \frac{44}{66} + \frac{12}{15.4} \frac{.8}{66} \frac{59.4}{66} - \frac{.8}{15.4} \frac{12}{66} = 8.406 \text{ K}$$

Load 3 at C

$$\frac{3}{66} \frac{14}{66} + \frac{16}{66} \frac{44}{66} + \frac{4}{66} \frac{58}{66} + \frac{4}{15.4} \frac{14}{66} = 11.18 \text{ K Max.}$$

Live Load Shear at DE H20 Loading 1 wheel of train of trucks

Load 2 at D

$$\frac{3}{15.4} \frac{2.2}{66} \frac{6.6}{66} + \frac{12}{66} \frac{.8}{66} \frac{7.4}{66} + \frac{4}{66} \frac{57.4}{66} + \frac{16}{66} \frac{51.4}{66} - \frac{16}{15.4} \frac{14}{66} = 1.95 \text{ K}$$

Load 3 at D

$$\frac{12}{15.4} \frac{2.2}{66} \frac{6.6}{66} + \frac{4}{66} \frac{23.4}{66} + \frac{16}{66} \frac{57.4}{66} = 10.63 \text{ K}$$

Total Shear at BC

Max. Reaction at Girder V of 1# load on each wheel across Girder
27/16.5

Impact = 20.6 %

$$\text{Total LLV} = 11.18 \frac{27}{16.5} \frac{120.6}{66} = 22.1 \text{ K}$$

DLV at BC = 67115.8 #

Total V at BC = 67115.8 + 22100 = 89215.8 #

Girder V

Bending Moment and Shear Totals

Max. LLBM (1 wheel) 300 KF
 Max. LLV (1 wheel) 18.36 K

$$(37) \text{ Impact} = \frac{L + 20}{6 L + 20} = \frac{66 + 20}{6 \cdot 66 + 20} = 20.6 \%$$

Max. Reaction at Girder V of 1 # Load on each wheel across Girder
 27/ 16.5

$$\text{Total LLBM} = 300 \cdot 20.6 \% \cdot 27/16.5 = 592 \text{ KF}$$

$$\text{Total LLV} = 18.36 \cdot 20.6 \% \cdot 27/16.5 = 37.15 \text{ K}$$

Max. DLBM 1545 KF
 Max. DLV 113502.8 #

$$\begin{aligned} \text{Total Max. BM} &= 1545 + 592 = 2137 \text{ KF} \\ \text{Total Max. V} &= 37150 + 113502.8 = 150652.8 \# \end{aligned}$$

Check Girder Cross Section

Gross Section of Flange 21.42 sq. in.
 Net " " " 18.45
 Web 3/4 in. by 60 3/8 in.
 h equals 58.34 in.

Tension Flange $f = 18000 \text{ #/sq. in.}$

$$A = \frac{BM}{f \cdot h} - 1/8 \text{ of web}$$

$$18.45 = \frac{2137000 \cdot 12}{18000 \cdot h} - 1/8 \cdot 3/4 \cdot 603/8$$

$$h = 58.7 \text{ supplied } 58.34 \text{ in.}$$

Compression Flange $f = 17157.5 \text{ #/sq. in.}$

$$A = \frac{2137000 \cdot 12}{17157.5 \cdot 58.34} - 1/8 \cdot 3/4 \cdot 603/8 = 18.45 \text{ sq. in. supplied } 21.42$$

Web $v = 12000 \text{ #/sq. in.}$ allowable

$$v = \frac{V}{A} = \frac{150652.8}{603/8 \cdot 3/4} = 3330 \text{ #/sq. in.}$$

Rivets in Girder First Panel (between end and first Beam)

Flange Angle Rivets

Girder II

Max. V 148630 #

Girder II has uniform load of concrete on top of flange of
205.9 #/ft.

Due to the fact that Girder II is in contact with concrete slab, there is a live load applied to top of Flange of Girder which is the Max. LLV (H20) of Slab betw en Girder and 12 in. @ 25 # CB Stringer and is equal to 4480 # on a ft. of slab.

$$\text{Total } w = 4480 + 205.9 = 4685.9 \text{ #/ft.}$$

$$\begin{aligned} HI &= \frac{V}{h} \times \frac{A_f}{A_f + A_w/8} \\ &= \frac{148630}{58.34} \times \frac{21.42}{21.42 + 5.68/8} = 2020 \# \end{aligned}$$

Bearing = 15200 #

Double Shear = 11960 #

$$\text{Pitch} = \frac{R}{\sqrt{HI^2 + w^2}} = \frac{11960}{\sqrt{2020^2 + (4685.9/12)^2}} = 5.72 \text{ in.}$$

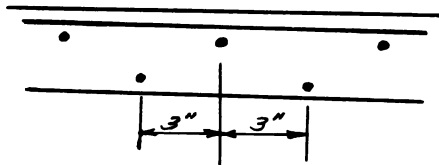
supplied 3 in.

Rivets in Girder First Panel (between end and first beam)

Max. V of Each Girder

Girder I	144500 #
Girder II	149630
Girder III	145070
Girder IV	134730
Girder V	150652.8 Max.

Flange Angle Rivets



Girder V

Girder V has a uniform load of concrete on top of flange of
 $2.25 \times 150 = 337.5 \text{ #/ft.}$

No live load on flange, because of direct contact of Girder with Slab, because the curb keeps wheels at a distance of 2.5 ft. from center line of Girder

$$HI = \frac{V}{h} \times \frac{A_f}{A_f + A_w/8}$$

$$= \frac{150652.8}{53.84} \times \frac{21.42}{21.42 + 5.66} = 2040 \text{ #}$$

Bearing of 3/4 Rivet on 3/4 Web Bearing = 27000 #/sq. in.
 $3/4 \times 3/4 \times 27000 = 15200 \text{ #}$

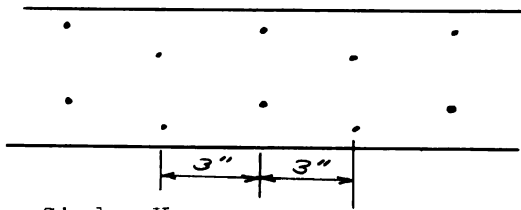
Double Shear of 3/4 Rivet shear 13500 #/sq. in.
 $2 \times .443 \times 13500 = 11960 \text{ #}$

$$\text{Pitch} = \frac{R}{\sqrt{HI^2 + w^2}} = \frac{11960}{\sqrt{2040^2 + (337.5/12)^2}} = 4.85 \text{ in.}$$

supplied 3 in.

Rivets in Girder First Panel (between end and first Beam)

Cover Plate Rivets



Girder V

$$V = 150652.8 \text{ \#}$$

$$h = 58.34 \text{ in.}$$

$$HI = \frac{V}{h} \times \frac{A_c}{A_f + A_w/8} = \frac{150652.8}{58.34} \times \frac{8.02}{21.48 + 5.66} = 765 \text{ \#}$$

Bearing of 1 Rivet on 9/16 in. Flange

$$9/16 \times 37000 = 11400 \text{ \#}$$

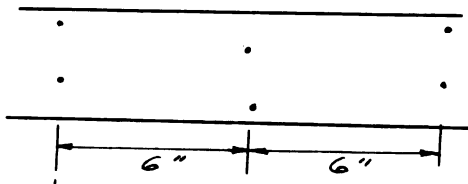
Shear one Rivet 3/4

$$.443 \times 13500 = 5980 \text{ \#}$$

$$\text{pitch} = \frac{R \cdot 2}{V/h} = \frac{2 \cdot 5980}{765} = 15.6 \text{ in. supplied } 3 \text{ in.}$$

Rivets in Girder Second Panel (between first and second Beam)

Cover Plate Rivets



Girder III

$$V = 97196.6 \text{ \#}$$

$$h = 58.34 \text{ in.}$$

$$HI = \frac{V}{h} \times \frac{A_c}{A_f + A_w/8} = \frac{97196.6}{58.34} \times \frac{8.02}{21.48 + 5.66} = 494 \text{ \#}$$

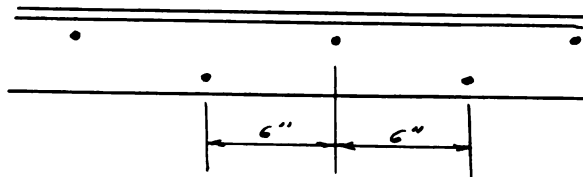
$$\text{Pitch} = \frac{2 \cdot R}{V/h} = \frac{2 \cdot 5980}{494} = 24.2 \text{ in. supplied } 6 \text{ in.}$$

Rivets in Girder Second Panel (between first and second Beam)

Max. V of Each Girder between first and second Beam

Girder I	85532.3 #	
Girder II	98016.6	
Girder III	97196.6	Max.
Girder IV	81322.3	
Girder V	89215.2	

Flange Angle Rivets



Girder III

Girder III has a uniform load of concrete on top of flange of 205.9 #/ft.

Due to fact that Girder III is in contact with surface there is a Live Load applied to top of Flange of Girder, which is the Max. LLv (H20) of slab between Girder III and 12 in. @ 31.5 # I Bm. Stringer of 3500 # on a ft. of slab.

$$\text{Total } w = 205.9 + 4500 = 4705.9 \text{ #/ft.}$$

$$h = 58.34 \text{ in.}$$

$$R_1 = \frac{V}{h} \times \frac{A_f}{A_f + A_w/8}$$

$$= \frac{97196.6}{58.34} \times \frac{21.43}{21.43 + 5.86} = 1320 \text{ #}$$

$$\text{Bearing} = 15200 \text{ #}$$

$$\text{Double Shear} = 11960 \text{ #}$$

$$\text{Pitch} = \frac{P}{\sqrt{R_1^2 + w^2}} = \frac{11960}{\sqrt{1320^2 + (4705.9/12)^2}} = 8.7 \text{ in.}$$

supplied 6 in.

Intermediate Stiffeners

(137)(8)

Clear Distance between Flange Angles

$$603/8 - 2(5\frac{1}{4}) = 47.87 \text{ in.}$$

60 times the thickness of web $60 \frac{3}{4} = 45 \text{ in.}$

47.87 is more than 45; therefore need stiffeners

Outstanding Leg of angle shall width of not more than 16 times
its thickness $16 \frac{3}{8} = 6 \text{ in.}$ supplied 5 in.and not less than (2 in. + 1/30 of depth of web)
 $2 + 1/30 \cdot 603/8 = 4 \text{ in.}$ supplied 5 in.Intervals between stiffeners should not more than 72 in.
nor that given by formulae.

$$d = \frac{(255000 t)}{s} \sqrt[3]{\frac{s t}{a}}$$

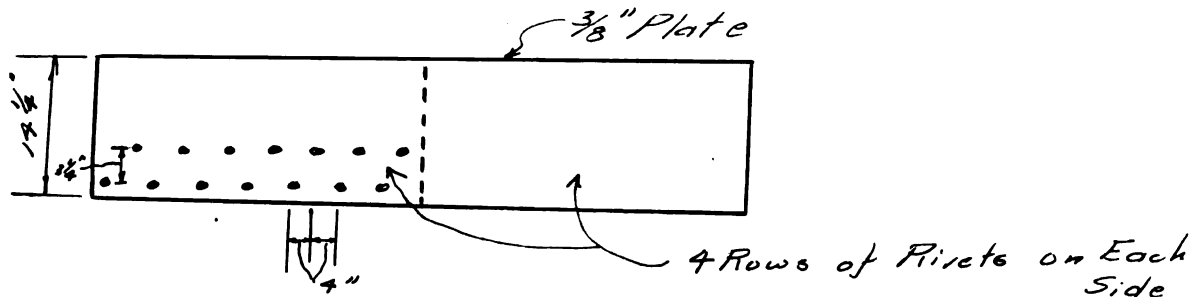
 d = clear distance between stif. t = thickness of web s = Shear, in pounds per sq. in.
in the gross vertical sect.
of the web at the point
considered a = clear depth of web between
flanges of side plates

Girder I	$V = 17450 \text{ \#}$	DE	$s = 3120 \text{ \#/sq. in.}$
	$V = 98382.8$	DE	$s = 1240$

$$\text{DE} \quad d = \frac{255000 \cdot 3/4}{3120} \sqrt[3]{\frac{3120 \cdot 3/4}{47.87}} = 321 \text{ in.} \quad \text{supplied } 36 \text{ in.}$$

$$\text{DE} \quad d = \frac{255000 \cdot 3/4}{1240} \sqrt[3]{\frac{1240 \cdot 3/4}{47.87}} = 312 \text{ in.} \quad \text{supplied } 35 \text{ in.}$$

Girder Cover Plate Splice



Cover Plate $9/16$ by $14\frac{1}{2}$ in.
 Gross Section = 8.02 sq. in.
 Net section

(83) 2-3/4 Rivets

$$x = 1 - \frac{3^2}{4 \cdot 5 \cdot 7/8} = 0.211 \text{ of 2 Holes}$$

$$2 \cdot 7/8 \cdot 9/16 \cdot 0.21 = 1.21 \text{ sq. in.}$$

$$\text{Net Sec.} = 8.02 - 1.21 = 6.81 \text{ sq. in.}$$

Cover Plate Splice $5/8$ by $14\frac{1}{2}$ in.
 Gross Section = 8.9 sq. in.
 Net Section

(83) 2-3/4 Rivets

$$x = 1 - \frac{3^2}{4 \cdot 5 \cdot 7/8} = 0.21 \text{ of 2 Holes}$$

$$2 \cdot 7/8 \cdot 5/8 = 1.1 \text{ sq. in.}$$

$$0.21 \cdot 2 \cdot 7/8 \cdot 5/8 = 0.22 \text{ sq. in.}$$

$$\text{tot. } 1.32 \text{ sq. in.}$$

$$\text{Net Sec.} = 8.9 - 1.32 = 7.58 \text{ sq. in. supplied}$$

(127) (e) Net Sec. of Splice $\geq 110\%$ of Net Sec. of CP
 $110\% \cdot 6.81 = 7.5 \text{ sq. in. supplied } 7.58$

Tension Side

Bearing of one Rivet Bearing $27000 \text{ \#/sq. in.}$
 $3/4 \cdot 27000 \cdot 9/16 = 11400 \text{ \#}$
 Single Shear of one Rivet shear $13500 \text{ \#/sq. in.}$
 $.4418 \cdot 13500 = 5960 \text{ \#}$

$$\text{Number of Rivets} = \frac{6.81 \cdot 13000}{5960} = 20.5 \text{ supplied } 23$$

Girder Cover Plate Bolts

Compression side

$$f = 17157.5 \text{ #/sq. in.}$$

$$\text{Number of Rivets} = \frac{8.0 \times 17157.5}{5000} = 23 \text{ Rivets}$$

supplied 23

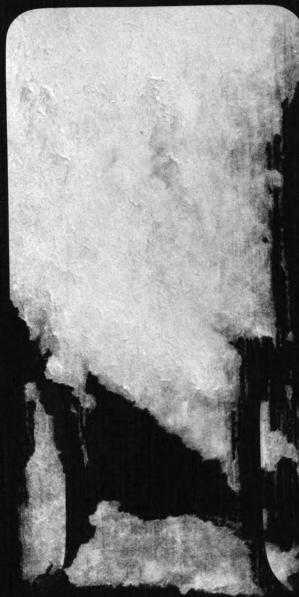
Conclusion:

Although, it may be satisfactory for the bridge to have H20 Loading, the safety factor is cut down considerably in a few places. The Girders and Stringers will carry this loading without sacrificing any of their safety factor, but in the Beams and Sills this loading will raise stresses beyond that allowed in the specifications.

The greatest failure occurred in carrying bending moment, by continuous action of beams, into the connection of the beams to the girder. The bending moment of the beam could be taking care of within the beam itself if the fiber stress in the flange area were raised to about 30,000 $\pm$ /sq. in.; therefore, by having a freely supported beam, the connection would more than satisfactorily carry the maximum reaction at the end of the beams.

It may be possible that this bridge should have been analyzed with H15 Loading instead of H20, but according to specification number 21 the bridge seems in that class of bridges which should be designed with H20 Loading.

Pocket has: 1 Suppl.



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