### A SPECIFIC HEAT STUDY OF Cs<sub>2</sub> MnCl <sub>4</sub> ·2H <sub>2</sub> O IN A MAGNETIC FIELD

Thesis for the Degree of Ph. D. MICHIGAN STATE UNIVERSITY NORMAN DUANE LOVE 1967 THESIS



This is to certify that the

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A Specific Heat Study of

 $Cs_2MnC1_4.2H_20$  in a Magnetic Field

presented by

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#### ABSTRACT

# A SPECIFIC HEAT STUDY OF Cs<sub>2</sub>MnCl<sub>4</sub>·2H<sub>2</sub>O IN A MAGNETIC FIELD

by Norman Duane Love

Adiabatic calorimeters for studies at  $He^4$  and  $He^3$ temperatures, and the measuring electronics have been described. Specific heat studies of single crystals of  $Cs_2MnCl_4 \cdot 2H_2O$  have been made in zero and non-zero magnetic fields. The zero field specific heat study: 1) compares well with the calculated specific heat from the magnetic susceptibility, 2) gives the Néel temperature as  $1.84^\circ \pm 0.01^\circ$ K, 3) indicates that 25 percent of the entropy is recovered above the Néel temperature due to short range ordering, and 4) gives a sublattice magnetization curve as a function of reduced temperature which agrees with the measured magnetization curve from an nmr study and with the curve computed for a f.c.c. lattice using a three dimensional Ising model.

Specific heat studies for several external magnetic fields in each of three orientation A, B, and C which are approximately the  $(0 \ \overline{1} \ \overline{1})$ ,  $(1 \ \overline{1} \ \overline{1})$ , and  $(\overline{1} \ \overline{1} \ \overline{1})$  directions respectively, have been made. They show that the transition temperature are reduced, in agreement with the calculations A SPECIFIC HEAT STUDY OF

 $Cs_2MnC1_4 \cdot 2H_2O$ IN A MAGNETIC FIELD

By

Norman Duane Love

## A THESIS

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ii

# TABLE OF CONTENTS

		Page
ACKNO	WLEDGMENTS	ii
Ι.	INTRODUCTION	1
II.	THEORY	3 -
	A. Thermodynamics of Specific Heats	3
	B. Magnetism	7
	magnetism	16
	D. Transition Temperature	2.2
	E. Spin-flop	25
III.	EXPERIMENTAL APPARATUS AND PROCEDURE	28
	A. Helium Dewar	28
	B. He4 Calorimeter	30
	C He <sup>3</sup> Calorimeter	35
	D Electrical Measurement Apparatus	30
	E Drenenetion of Comple	12
	E. Preparation of Sample	42
	F. Experimental Procedure	45
	1. Pre-cooling	4 5
	2. Adding Exchange Gas	48
	3. Liquid-Helium Transfer	48
	4. The Calibration of Sample	
	Thermometer	50
	5 Specific Heat Measurements	51
	6 Voltago Calibration Data	51
	7 Chut lage	54
	7. Snut-down	22
	G. Data Reduction	55
	1. Calibration of Thermometer	55
	2. Voltage-Calbration	56
	3. Specific-Heat Data	61
IV.	RESULTS AND DISCUSSIONS	63
	A. Description of Crystal	63
	B. Zero-Field Results	63

	C. D.	Ma Ph	gne ase	eti e D	c- ia	Field gram.		.d	Re •	su •	ults		•	•	•	•	•	•	•	•	69 82
	Ε.	Co	nc1	us	io	n	•	•	•	•	•	•	•	•	•	•	•	•	•	•	90
REFERENCES	5	•••	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	95
APPENDIX 1	[	•••	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	97
APPENDIX 1	II		•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	100

# LIST OF TABLES

TABLE		Page
1.	Temperature-Calibration-Curve Parameters from an Experiment made January 13, 1967	56
2.	One-Millivolt-Voltage Calibration-Curve Parameters for an Experiment made January 13, 1967	59
3.	The Specific Heat of Cs <sub>2</sub> MnCl <sub>4</sub> • 2H <sub>2</sub> O for Sample 1, Run 2, September 16, 1966, Zero Field	100
4.	The Specific Heat of Cs <sub>2</sub> MnCl <sub>4</sub> ·2H <sub>2</sub> O for Sample 1, Run 3, September 21, 1966, Zero Field	102
5.	The Specific Heat of Cs <sub>2</sub> MnCl <sub>4</sub> ·2H <sub>2</sub> O for Sample 2, Run 1, October 5, 1966, Zero Field	104
6.	The Specific Heat of Cs <sub>2</sub> MnCl <sub>4</sub> ·2H <sub>2</sub> O for Sample 2, Run 2, October 17, 1966, Zero Field	106
7.	The Specific Heat of Cs <sub>2</sub> MnCl <sub>4</sub> •2H <sub>2</sub> O for Sample 1, Run 5, December 23, 1966, 8150 Gauss, Orientation A	107
8.	The Specific Heat of Cs <sub>2</sub> MnCl <sub>4</sub> ·2H <sub>2</sub> O for Sample 1, Run 6, January 12, 1967, 8150 Gauss Orientation A	108
9.	The Specific Heat of $Cs_2MnCl_4 \cdot 2H_2O$ for Sample 1, Run 7, January 13, 1967, 5150	110
	Gauss, Orientation A	110

10.	The Specific Heat of Cs <sub>2</sub> MnCl <sub>4</sub> ·2H <sub>2</sub> O for Sample 1, Run 8, January 18, 1967, 5150 Gauss, Orientation A	111
11.	The Specific Heat of Cs <sub>2</sub> MnCl <sub>4</sub> •2H <sub>2</sub> O for Sample 1, Run 9, January 20, 1967, 3500 Gauss, Orientation A	112
12.	The Specific Heat of Cs <sub>2</sub> MnCl <sub>4</sub> ·2H <sub>2</sub> O for Sample 1, Run 10, January 23, 1967, 3500 Gauss, Orientation A	114
13.	The Specific Heat of Cs <sub>2</sub> MnCl <sub>4</sub> •2H <sub>2</sub> O for Sample 1, Run 12, February 11, 1967, 8400 Gauss Orientation B	116
14.	The Specific Heat of Cs <sub>2</sub> MnCl <sub>4</sub> ·2H <sub>2</sub> O for Sample 1, Run 13, February 13, 1967, 8400	110
15.	Gauss, Orientation B	118
16.	Gauss, Orientation B	120
17.	Gauss, Orientation B	122
18.	Gauss, Orientation C	124
19.	Gauss, Orientation C	126
20.	Gauss, Orientation C	127
	Gauss, Orientation C	128

21.	The Specific Heat of $Cs_2MnCl_4 \cdot 2H_2O$ for Sample 1, Run 20, March 14, 1967, 6050 Gauss, Orientation C
22.	The Specific Heat of $Cs_2MnCl_4 \cdot 2H_2O$ for Sample 1, Run 21, March 22, 1967, 8900 Gauss, Orientation C
23.	The Specific Heat of $Cs_2MnCl_4 \cdot 2H_2O$ for Sample 1, Run 22, April 5, 1967, 9830 Gauss, Orientation C
24.	The Specific Heat of $Cs_2MnCl_4 \cdot 2H_2O$ for Sample 1, Run 23, April 5, 1967, 3500 Gauss, Orientation C
25.	The Specific Heat of $Cs_2MnCl_4 \cdot 2H_2O$ for Sample 1, Run 24, April 5, 1967, 8900 Gauss, Orientation C
26.	The Specific Heat of $Cs_2MnCl_4 \cdot 2H_2O$ for Sample 1, Run 25, April 7, 1967, 3500 Gauss, Orientation C
27.	The Temperature Changes from an Adiabatic Magnetization Experiment on Sample 1, Orientation C, April 21, 1967

# LIST OF FIGURES

FIGURE		Page
la.	Magnetization Curve Calculated from the Molecular-Field Theory	15
1b.	Shape of Specific Heat Curve Calculated from the Molecular-Field Theory	15
2.	The Susceptibility of an Antiferromagnetic Material as a Function of Temperature in	
	Reduced Units	21
3.	A Magnetic Dewar	29
4.	Scale Drawing of Lower Portion of He <sup>4</sup>	
	Calorimeter	31
5.	Front and Side View of Top of He <sup>4</sup> Calori-	
	meter	32
6.	Photograph of Unassembled Calorimeter	33
7.	The Needle Valve	36
8.	Schematic of He <sup>3</sup> Calorimeter	37
9.	Electrical-Measurement Circuit Diagrams	39
10.	A Photograph of Total System	46
11.	Schematic Diagram of Top of Dewar	47
12.	Sample Recorder Chart	52
13.	A Cross-Sectional View of Cs <sub>2</sub> MnCl <sub>4</sub> •2H <sub>2</sub> O	
	Perpendicular to the Elongated Axis with	
	an Arrow Indicating the Direction of Easy	<i>с</i> <b>н</b>
	Magnetization	64
14.	Specific Heat Curve in Zero Magnetic Field.	65
	viii	

15.	Sublattice Magnetization Curves	70
16.	Specific Heat Curve for Orientation A and	
	3500 Gauss	72
17.	Specific Heat Curve for Orientation A and	77
	5150 Gauss	/3
18.	Specific Heat Curve for Orientation A and	74
10	Constitution Read	
19.	6050 Gauss	75
20.	Specific Heat Curve for Orientation B and	
	8400 Gauss	76
21.	Specific Heat Curve for Orientation C and	
	3500 Gauss	77
22.	Specific Heat Curve for Orientation C and	
	6050 Gauss	78
23.	Specific Heat Curve for Orientation C and	
	8400 Gauss	79
24.	Specific Heat Curve for Orientation C and	
	8900 Gauss	80
25.	Specific Heat Curve for Orientation C and	
	9830 Gauss	81
26.	Entropy Curves for Orientation A	83
27.	Entropy Curves for Orientation B	84
28.	Entropy Curves for Orientation C	85
29.	Entropy, Field, and Temperature Surface for	
	Orientation A	86
30.	Entropy, Field, and Temperature Surface for	
	Orientation B	87
31.	Entropy, Field, and Temperature Surface for	
	Orientation C	88

Page

32.	Phase Diagram for Orientations A, B, and C.	89
33.	Temperature vs. Angle from Easy Direction for an Adiabatic Rotation of a Constant	
	External Magnetic Field of 8000 Gauss	92
34.	Circuit Diagram for a Simple Potentiometer.	98

# LIST OF APPENDICES

																						Page
APPENDIX	Ι.	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	97
APPENDIX	II.	•		•	•	•	•	•	•	•	•	•		•	•	•		•	•	•	•	100

### I. INTRODUCTION

Some nmr studies by Spence<sup>1</sup> and susceptibility measurements by Cowen<sup>2</sup> indicated an antiferromagnetic-paramagnetic transition at about  $1.8^{\circ}$ K in  $Cs_2$ MnCl<sub>4</sub> · 2H<sub>2</sub>O. Since 1.8°K is easily attained by He<sup>4</sup> calorimetry, a measure of its specific heat in a zero magnetic field would be of interest and would provide a check on the transition temperature, and a comparison with the molecular-field theory for the sublattice magnetization and magnetic susceptibility. After the zero-field study was completed, studies in an external magnetic field were begun. These studies show that the transition temperatures are reduced as the external magnetic field is increased, in agreement with the molecular-field theory. The magnetic phase diagram indicated which of the three crystal orientations is sufficiently close to having its sublattice magnetization direction parallel to the external magnetic-field direction.

This study has three purposes: 1) to construct He<sup>4</sup> and He<sup>3</sup> calorimeters for use in specific heat measurements for the temperature range  $0.4^{\circ}-4.2^{\circ}$ K, 2) to report the results of the specific heat study on  $Cs_2MnCl_4 \cdot 2H_2O$  in both zero and non-zero external fields, 3) to search for a possible spin-flop magnetic region by a calorimetric method.

The study is divided into three sections. The first section describes the theories pertinent to the present study. Section two describes the apparatus and the stepby-step procedures for measuring the specific heat. The last section discusses the results, using the theories and equations developed in section one.

It is hoped that the present study may provide sufficient information concerning the magnetic transition in  $Cs_2MnCl_4 \cdot 2H_2O$ , that additional problems which have been raised from these experiments may be pursued fruitfully.

#### **II. THEORY**

# A. Thermodynamics of Specific Heats<sup>3,4</sup>

When energy, as heat, is absorbed by a substance, a temperature change will be observed except for first-order phase transitions. The function which related this temperature change to the amount of heat absorbed by the substance is called heat capacity or specific heat, if divided by the mass of the material. This can formally be written as

$$d'Q = C_{v}dT \tag{1}$$

where d'Q is an increment of heat measured in calories, dT is the change in temperature measured in Kelvin degrees, and  $C_{r}$  is the heat capacity measured in calories/degree.

The First Law of Thermodynamics, more commonly known as the conservation of energy, can be written for a reversible process as

$$dU = d'Q - d'W.$$
 (2)

The function U is the internal energy and dU is an exact differential, the reason for the absence of the apostrophe. d'Q has already been defined and d'W is

d'W = PdV - HdM + other forms of work (3)
where P is pressure, V is volume, M is magnetization, and
H is the magnetic field. This study deals with solids at

low temperatures, and dV will be essentially zero for all of the measurements.

The Second Law of Thermodynamics defines another function with an exact differential, called entropy, which can be used as a measure of a material's disorder. d'Q may now be written for a reversible process as

$$d'Q = TdS$$
 (4)

Now the First Law becomes

$$TdS = dU - HdM.$$
(5)

Consider S and U functions of T and M only and write

$$dS = \frac{\partial S}{\partial T} \bigg|_{M} dT + \frac{\partial S}{\partial M} \bigg|_{T} dM$$
(6)

and

$$dU = \frac{\partial U}{\partial T} \bigg|_{M} dT + \frac{\partial U}{\partial M} \bigg|_{T} dM$$
 (7)

Substituting into equation (5),

$$T\frac{\partial S}{\partial T}\Big|_{M} dT + T\frac{\partial S}{\partial M}\Big|_{T} dM = \frac{\partial U}{\partial T}\Big|_{M} dT + \left[\frac{\partial U}{\partial M}\right]_{T} - H dM$$
(8)

But

$$\left. T \frac{\partial S}{\partial T} \right|_{M} = C_{M}.$$
 (9)

Therefore

$$C_{M} = \frac{\partial U}{\partial T} \Big|_{M}, \qquad (10)$$

and

$$\left. T \frac{\partial S}{\partial M} \right|_{T} = \left[ \frac{\partial U}{\partial M} \right|_{T} - H \right].$$
 (11)

Now consider S and M functions of H and T, and U a function of M and T. Using the results (10) and (11) write,

$$T\frac{\partial S}{\partial T}\Big|_{H}dT + T\frac{\partial S}{\partial H}\Big|_{T}dH = C_{M}dT + T\frac{\partial S}{\partial M}\Big|_{T}\left[\frac{\partial M}{\partial T}\right]_{H}dT + \frac{\partial M}{\partial H}\Big|_{T}dH \qquad (12)$$

But

$$\left. T \frac{\partial S}{\partial M} \right|_{H} = C_{H}$$
(13)

then

$$C_{\rm H} - C_{\rm M} = T \frac{\partial S}{\partial M} \bigg|_{\rm T} \left| \frac{\partial M}{\partial T} \right|_{\rm H}.$$
 (14)

Using Maxwell's equation,

$$\left.\frac{\partial H}{\partial T}\right|_{M} = \left.-\frac{\partial S}{\partial M}\right|_{T},$$
(15)

write

$$C_{\rm H} - C_{\rm M} = -T \frac{\partial H}{\partial T} \Big|_{\rm M} \frac{\partial M}{\partial T} \Big|_{\rm H}.$$
 (16)

It follows that for low temperatures,  $C_{H} \approx C_{M}$ . From equations (10) and (13), one may write,

$$S(T_1) - S(T_2) = \int_{T_1}^{T_2} C_x / T dt$$
 (17)

where x is either M or H. Statistical mechanics defines  $entropy^5$  as the natural logarithm of the volume of phase space or of the total number of states available. If a mole of substance has a quantum number J then there are

2J + 1 states and

$$\Delta S = R \ell n (2J + 1) \tag{18}$$

where

$$\Delta S = \int_0^\infty C_X / T \, dt. \qquad (19)$$

Energy may be absorbed by a solid in a variety of ways,<sup>6</sup> such as, through an increase in the oscillations of the atoms about their lattice sites  $(U_L)$ ; an increase in the kinetic energy of the free electrons  $(U_e)$ ; by the presence of a magnetic exchange energy  $(U_H)$ ; by the excitation of atoms  $(U_S)$  and nuclei  $(U_n)$  to higher energy levels. The internal energy can thus be written as a sum of terms,

$$U_{\rm T} = U_{\rm L} + U_{\rm H} + U_{\rm n} + \cdots$$
 (20)

Therefore the specific heat of the solid may be written as,

$$C_{T} = \frac{\partial U_{L}}{\partial T} + \frac{\partial U_{N}}{\partial T} + \frac{\partial U_{H}}{\partial T} + \dots \qquad (21)$$

where the appropriate variables are kept fixed during the process. Consequently,

$$C_{T} = C_{L} + C_{H} + C_{n} + \cdots$$
 (22)

can be written and specific heats are additive.  $C_L$  and  $C_n$  need only be measured or calculated and subtracted from  $C_T$  to give  $C_H$ .

### B. Magnetism

Magnetism has been a curiosity for centuries, as it revealed itself in the form of magnets called lodestones or magnetite. The formal study of magnetism did not begin until the beginning of the 17th century by Gilbert. It was not until the advent of quantum mechanics that a reasonable explanation for the origin of magnetism was forthcoming. It was first thought that magnetic effects could be explained on the basis that different paramagnetic ions coupled together through a magnetic dipole-dipole interaction. For most substances this interaction is too weak to account for high internal fields observed, 100 gauss calculated, compared to 10,000 gauss measured.

Heisenberg<sup>7</sup> suggested a quantum mechanical exchange interaction (between electrons of different paramagnetic ions) which gave internal fields of the order of those measured.

Two atoms each with one unpaired electron in similar potentials are considered. They are labeled "1" and "2" with coordinates  $r_1$  and  $r_2$ . The Hamiltonian<sup>8</sup> can be written as,

$$H(1,2) = -(\hbar^2/2M) \nabla_1^2 - (\hbar^2/2M) \nabla_2^2 + V_T(r_1,r_2,r_{12})$$
(23)

where

$$V_{T}(r_{1}, r_{2}, r_{12}) = V_{1}(r_{1}) + V_{2}(r_{2}) + V(r_{12})$$
 (24)

and  $r_{12}$  is the radius vector between the electrons. Assume

the electrons to be independent, then  $V(r_{12}) = 0$ , and

$$H\psi(r_{1}, r_{2}) = E_{T} \psi(r_{1}, r_{2})$$
(25)

Equation (23) is then separable into,

$$-(\hbar/2M)\nabla_{1}^{2}\psi_{\alpha}(r_{1}) + V_{1}(r_{1})\psi_{\alpha}(r_{1}) = E_{\alpha}\psi(r_{1})$$
(26)

$$-(\hbar/2M)\nabla_{2}^{2}\psi_{\beta}(r_{2}) + V_{2}(r_{2})\psi_{\beta}(r_{2}) = E_{\beta}\psi(r_{2})$$
(27)

where  $\psi_{\alpha}$  and  $\psi_{\beta}$  are the normalized wave functions of the separated equations and  $\alpha$  and  $\beta$  designate the energy state. Thus there exist two possible solutions

$$\psi(\mathbf{r}_1, \mathbf{r}_2) = \psi_{\alpha}(\mathbf{r}_1) \psi_{\beta}(\mathbf{r}_2)$$
(28)

or

$$\psi(\mathbf{r}_1, \mathbf{r}_2^0 = \psi_{\alpha}(\mathbf{r}_2) \ \psi_{\beta}(\mathbf{r}_1)$$
<sup>(29)</sup>

to equation (25) with the same energy  $E_T = E_{\alpha} + E_{\beta}$ . To keep the identical electrons indistinguishable when considering probability densities, two linear combinations, a symmetric  $\psi_S$  and an anti-symmetric  $\psi_A$ , of the above solutions must be used,

$$\psi_{S}(\mathbf{r}_{1},\mathbf{r}_{2}) = \frac{1}{\sqrt{2}} \left[ \psi_{\alpha}(\mathbf{r}_{1}) \ \psi_{\beta}(\mathbf{r}_{2}) + \psi_{\alpha}(\mathbf{r}_{2}) \ \psi_{\beta}(\mathbf{r}_{1}) \right]$$
(30)

$$\psi_{A}(\mathbf{r}_{1},\mathbf{r}_{2}) = \frac{1}{\sqrt{2}} \left[ \psi_{\alpha}(\mathbf{r}_{1}) \ \psi_{\beta}(\mathbf{r}_{2}) - \psi_{\alpha}(\mathbf{r}_{2}) \ \psi_{\beta}(\mathbf{r}_{1}) \right] \quad (31)$$

Spins have so far not been considered. All electrons have spin angular momentum  $\pm \pi/2$ . Thus a magnetic field

applied along the z-direction would orient the magnetic moment  $\mu_z$ , with magnitude of one Bohr magneton, either parallel or antiparallel to this field. The Pauli principle limits the total wave function for the electrons to be only anti-symmetric. Thus the two total wave functions including the spin wave functions ( $\chi$ ) may be written as,

$$\psi_{I} = B_{I} \psi_{s} \left[ \chi_{\alpha}(1) \chi_{\beta}(2) - \chi_{\alpha}(2) \chi_{\beta}(1) \right]$$
(32)  
$$\psi_{II} = B_{II} \psi_{A} \chi_{\alpha}(1) \left\{ \begin{array}{l} \chi_{\alpha}(1) \chi_{\beta}(2) \\ \chi_{\beta}(2) + \chi_{\alpha}(2) \chi_{\beta}(1) \\ \chi_{\alpha}(2) \chi_{\beta}(1) \end{array} \right\}$$
(33)

where  $\psi_{\rm I}$  represents the singlet state and  $\psi_{\rm II}$  represents the triplet state, and where B\_I and B\_{II} are the normalization factors.

Adding the interaction between the electrons  $V(r_{12})$ and applying first order perturbation theory the energies are,

$$E_{I} = B_{I}^{2} (A_{12} + J_{12})$$
(34)

and

$$E_{II} = B_{II}^{2} (A_{12} - J_{12})$$
(35)

where

$$A_{12} = \int \psi_{\alpha}^{*}(r_{1}) \psi_{\beta}^{*}(r_{2}) V(r_{12}) \psi_{\alpha}(r_{1}) \psi_{\beta}(r_{2}) d\tau_{1} d\tau_{2}$$
(36)

and

$$J_{12} = \int \psi_{\alpha}^{*}(r_{1}) \psi_{\beta}^{*}(r_{2}) V(r_{12}) \psi_{\alpha}(r_{2}) \psi_{\beta}(r_{1}) d\tau_{1} d\tau_{2}$$
(37)

 $\rm A_{12}$  is the average value of V(r\_{12}), and J\_{12} is called the exchange intergal.

If  $J_{12}$  is positive the ground state is  $E_{II}$  and the spins are parallel; but if  $J_{12}$  is negative,  $E_I$  is the ground state and the spins are antiparallel. If this process is applied to an assembly of electrons in a solid, such as the 3d electrons in a transition element, and  $J_{12}$  is positive, the internal magnetic moments add and may be detected externally as a magnetic field.  $J_{12}$  being positive results in a mechanism for ferromagnetism. If  $J_{12}$  is negative, the spins are coupled antiparallel, and there is no external field possible; this is called antiferromagnetism. Néel<sup>9</sup> and Van Vleck, <sup>10,11,12</sup> using two interpenetrating sublattices and the molecular field theory, calculated some properties that characterized an antiferromagnet. It was not until the development of neutron diffraction techniques that antiferromagnetism was directly verified, completing the exchange interaction picture.

In the above discussion on exchange, the interaction potential is assumed spin independent. But the spins are coupled with a scaler potential proportional to  $\vec{s}_1 \cdot \vec{s}_2$ . Keeping only the spin-dependent part, the exchange energy may be written as,

$$E_{ex} = -2J_{12}\vec{s}_1 \cdot \vec{s}_2.$$
 (38)

Considering two atoms which have more than one unpaired electron the exchange energy becomes,

$$E_{ex} = -2J_{12} \, \dot{s}_1 \cdot \dot{s}_2 \tag{39}$$

where  $\dot{S}$  is the total spin of the atom. All electrons are assumed to have the same exchange integral. If the exchange integral is assumed isotropic ( $J_e$ ) and is negligible except for nearest neighbors, then for all of the atoms in a crystal the exchange energy is

$$E_{ex} = -2J_{e} \sum_{i,j} \vec{s}_{i} \cdot \vec{s}_{j}$$
(40)

The summation is taken over all of the atoms in the crystal. The prime means i = j is not included.

Solving this Hamiltonian should give the properties of magnetism. This has not been possible without making further assumptions. The Bethe-Peierls-Weiss<sup>13,14,15</sup> method assumes a model where a central atom and its interaction with its nearest neighbors is calculated from (40) but the nearest neighbors are assumed to interact with an internal field due to their neighbors.

Instead, if the assumption is made that the interaction  $2J_e(S_{xi}S_{xj} + S_{yi}S_{yj})$  may be neglected, where  $S_x$ ,  $S_y$ , and  $S_z$  are the components of S, the exchange energy is then written as,

$$E_{ex} = -2J_{e} \sum_{i,j}' S_{zi} \cdot S_{zj}$$
(41)

The above assumption amounts to replacing the instantaneous

spin values with their time averages and is called the Ising<sup>16</sup> model. There is an extensive literature on the calculations made with the Ising model,<sup>17,18</sup> but these will not be discussed here.

Following Van Vleck,<sup>10</sup> the quantum mechanical justification will be made for the Weiss<sup>19</sup> molecular-field approximation. Since the interactions are only for the z nearest neighbors,

$$E_{ex} = -2J_e \sum_{i} S_{zi} \cdot \sum_{n=1}^{Z} \overline{S}_{zn}$$
(42)

$$E_{ex} = -g\beta \sum_{i} S_{zi} \cdot (2J_{e}/g\beta) \sum_{n=1}^{z} \overline{S}_{zn}$$
(43)

where g is the gyromagnetic ratio,  $\beta$  is the Bohr magneton, and  $\overline{S}_{zn}$  is the average of the neighboring spin. An internal field H<sub>i</sub> may be defined,

$$H_{i} = (2J_{e}/g\beta) \sum_{n=1}^{Z} \overline{S}_{2n}$$
 (44)

Then,

$$E_{ex} = -g\beta \sum_{i} S_{zi} \cdot H_{i}$$
 (45)

The magnetization of a specimen with N atoms is

$$M = Ng\beta\overline{S}$$
(46)

Thus

$$H_{i} = (2J_{e^{Z}}/Ng^{2}\beta^{2})M = \lambda M$$
(47)

where  $\lambda$  is Weiss' molecular-field constant.

The problem of magnetism has now been reduced to solving for the case of N independent atoms with a permanent moment ( $g\beta S$ ) in an applied magnetic field H. According to statistical mechanics the magnetization is,

$$M = N \frac{\sum_{s=g\beta Se^{-g\beta SH/kT}}^{S}}{\sum_{s=e^{-g\beta SH/kT}}}$$
(48)

where k is Boltzmann's constant, and S is the spin. Let  $x = g\beta H/kT$  and using the formula for the sum of the geometric progression, the reduced equation becomes,

$$M = Ng\beta S B_{s}(y)$$
(49)

where

$$B_{s}(y) = \left[\frac{2S+1}{2S}Coth\left(\frac{2S+1}{2S}y\right) - \frac{1}{2S}Coth\left(\frac{1}{2S}y\right)\right]$$
(50)

and is called the Brillouin function, and

$$y = (g\beta S/kT)H$$
(51)

Substituting  $H_i$  for H in (49), (50), and (51) gives the solution for the magnetization of a ferromagnet.

The sublattice magnetization for an antiferromagnet is found in a similar matter. Divide the lattice into two interpenetrating sublattices such that the next nearest neighbors of an atom in sublattice, a, all lie in sublattice, b, and vice versa. The molecular field acting on an atom at site, a, is

$$H_{ia} = \gamma M_{b}$$
(52)

and the molecular field acting on an atom at site, b, is

$$H_{ib} = \gamma M_a$$
(53)

where  $\gamma$  corresponds to the Weiss molecular-field constant and is assumed to be the same for both sublattices; but a distinction is made with  $\lambda$  for the ferromagnetic case, since now only one-half of the atoms contribute to each of the molecular fields.

If 
$$|M_a| = |M_b| = |M_o|$$
 and  $M_a = -M_b$  then,  

$$M_o = M_s B_s(y)$$
(54)

and

$$y = (g\beta S/kT)\gamma M_{O}$$
(55)

where  $M_s = \frac{1}{2}Ng\beta S$ . The  $\frac{1}{2}$  appears because each sublattice contains only half the atoms. The solution for  $M_o$  is found by solving equations (54) and (55) graphically. The curve in Figure 1a shows the reduced magnetization  $M_o/M_s$  as a function of the reduced temperature  $T/T_n$  for S = 5/2 and  $T_n$ is the Néel temperature about which more will be said later.

Since,

 $E_{ex} = -g\beta \sum_{i} S_{zi} \cdot \gamma M_{o}$  (56)

then

$$E_{ex} = -2\gamma M_o^2$$
 (57)

where  $M_0 = \frac{1}{2}Ng\beta\overline{S}$  and  $\overline{S}$  is the average spin.







Fig. 1b. Shape of Specific Heat Curve Calculated from the Molecular-Field Theory.

Now,

$$C_{\rm H} = \frac{\partial E_{\rm ex}}{\partial T} \bigg|_{\rm H} \sim M_{\rm o} \frac{\partial M_{\rm o}}{\partial T}$$
(58)

where  $C_{\rm H}$  is the magnetic specific heat. Since M<sub>o</sub> was determined graphically, equation (58) will have to be solved numerically. Figure 1b shows the curve which is proportional to the specific heat calculated from equation (58) using points on Figure 1a.

### C. Magnetic Susceptibility for Antiferromagnetism

The susceptibility curve is separated into parts by the Néel temperature, i.e. the region above the Néel temperature which is the normal paramagnetic state, and the region below the Néel temperature which is the antiferromagnetic state. All the calculations are based on the molecularfield theory and follow the method outlined in the text by Morrish.<sup>20</sup>

For temperature well above the Néel temperature there are no exchange forces and thus no molecular-field. If a small external field is applied at high enough temperatures, only the first term in the expansion of the Brillouin function need be considered for the calculation of the susceptibility. The expansion of the Brillouin function is,

$$B_{s}(y) = \frac{1}{3} \left( \frac{S+1}{S} \right) y + \frac{1}{6} B_{s}''(0) y^{3} + \dots$$
 (59)

where

$$B_{s}''(0) = -6(S + 1)[(S + 1)^{2} + S^{2}]/90S^{3}$$
(60)

Now,

$$y = (g\beta S/kT)H_{ex}$$
(61)

where  $H_{ex}$  is the external field instead of the internal molecular-field. M may be written using the first term of (59),

$$M = Ng\beta S \left[ \frac{1}{3} \frac{S+1}{S} \left( \frac{g\beta S}{kT} \right) H_{ex} \right]$$
(62)

Then

$$\chi = M/H_{ex} = \frac{Ng^2\beta^2S(S+1)}{3k} \left(\frac{1}{T}\right) = \frac{C}{T}$$
(63)

where C is the Curie constant. Equation (63) is called the Curie Law. For temperatures near the Néel temperature  $M_a$  and  $M_b$  must be considered since there is usually some short range ordering.

Now,

$$H_{Ta} = H_{ex} - \gamma M_{a}$$
 (64)

and

$$H_{Tb} = H_{ex} - \gamma M_{b}$$
 (65)

and notice that the magnetization vectors are both in the direction of the applied field because of the absense of the long range exchange forces. Again using the first term of the expansion of the Brillouin function and the total magnetization M, as the sum of the two sublattices magnetizations, write,

$$M = \frac{Ng\beta S}{2} \left( \frac{S+1}{3S} \right) \frac{g\beta S}{kT} \left[ 2 H_{ex} - \gamma (M_{a} + M_{b}) \right]$$
(66)

$$M = \frac{1}{2} C/T (2 H_{ex} - \gamma M)$$
 (67)

$$M\left(1 + \frac{C\gamma}{2T}\right) = \left(\frac{C H_{ex}}{T}\right)$$
(68)

$$\chi = \frac{C}{T + \theta}$$
(69)

where

$$\theta = \frac{1}{2}C\gamma \tag{70}$$

Equation (69) is the Curie-Weiss Law and  $\theta$  will turn out to be the Néel temperature.

Below the Néel temperature two cases must be considered, the case with external field parallel to the sublattice magnetization and the case with the external field perpendicular to the sublattice magnetization. Consider the parallel case first. Now the internal field will include the external and molecular fields; and,

$$y_a = (g\beta S/kT)(H + \gamma M_b)$$
 (71)

and

$$y_{\rm h} = (g\beta S/kT)(-H + \gamma M_a)$$
(72)

At H = 0,  $M_a = -M_b = M_o$ , and  $y_a = -y_b = y_o$ . Now expand the Brillouin function about  $y_o$  and keep only first order terms,

$$B_{s}(y_{o}) = B_{s}(y_{o}) + B'_{s}(y_{o}) \left[ H + \gamma (M_{b} - M_{o}) \right] \frac{g\beta S}{kT}$$
 (73)

and

$$B_{s}(y_{b}) = B_{s}(y_{o}) - B_{s}'(y_{o}) \left[H + \gamma (M_{o} - M_{a})\right] \frac{g\beta S}{kT}$$

$$B_{s}(y_{a}) = B_{s}(Y_{o}) - B_{s}'(y_{o}) \left[-H - \gamma (M_{b} - M_{o})\right] \frac{g\beta S}{kT}$$

$$(74)$$

where  $B'_{s}(y_{0})$  is the derivative of the Brillouin function with respect to its argument. Now  $M_{a}$  and  $M_{b}$  are computed from equation (54) and M the total magnetization is

$$M = M_a - M_b$$
(75)

Thus,

$$M = M_{s} \left[ B'_{s}(y_{o}) \left\{ \left[ H + \gamma (M_{b} - M_{o}) \right] + \left[ H + \gamma (M_{o} - M_{a}) \right] \right\} \frac{g_{\beta S}}{kT} \right]$$
(76)

$$M = \frac{1}{2} \frac{Ng^2 \beta^2 S^2}{kT} B'_{s}(y_{o}) [2H - \gamma M]$$
(77)

$$\chi_{//} = \frac{Ng^2 \beta^2 S^2 B'_{s}(y_{o})}{kT + \frac{1}{2}Ng^2 \beta^2 S^2 B'_{s}(y_{o})\gamma}$$
(78)

Now  $B'_{s}(y_{0})$  goes to zero exponentially as T goes to 0; and since

$$\chi_{//} = \frac{Ng^2 \beta^2 S^2}{\frac{1}{2}Ng^2 \beta^2 S^2 \gamma + \frac{kT}{B_s'(y_0)}},$$
(79)

then  $\chi_{//}$  goes to zero as T goes to zero.

The applied field when perpendicular to the sublattice magnetization will cause each of the magnetization vectors to rotate through a small angle  $\phi$ . At equilibrium the torque on the sublattice magnetization must be zero, therefore,

$$|\vec{M}_{a} x(\vec{H}_{ex} + \gamma \vec{M}_{b})| = 0$$
 (80)

or

$$M_{a}H\cos\phi - \gamma M_{a}M_{b}\sin 2\phi = 0$$
 (81)

$$2M_{\rm b} \sin \phi = H/\gamma \tag{82}$$

and since  $M_a = M_b$  then

$$M = (M_a + M_b) \sin \phi = 2M_b \sin \phi$$
(83)

Thus,

$$\chi_{|} = 1/\gamma \tag{84}$$

Figure 2 shows the qualitative plot of the susceptibility for an antiferromagnetic material.

Fisher<sup>21</sup> has also worked out a relationship between the parallel susceptibility and the specific heat. He calculates,

$$C_{M}(T) \simeq 2R f \left(1 - \frac{2}{3}\alpha\right) \frac{\partial}{\partial \theta} \left[ (T\chi_{//}) / (T\chi_{//})_{\infty} \right]$$
 (85)

where f is a slowly varying function of T and is equated to 1,  $\alpha$  is a measure of the anisotropy of the interaction (equal to zero for pure isotropic interactions),  $\theta$  is T/T<sub>n</sub>, and  $(TX_{//})_{\infty}$  is the value of  $(TX_{//})$  extrapolated to high temperatures. Assuming an isotropic interaction,

$$C_{M} = 2R \frac{T_{n}}{(TX_{//})_{\infty}} \frac{\partial (TX_{//})}{\partial T}$$
(86)

is the form of Fisher's equation which may be used to compare the zero field specific heat with the parallel susceptibility.



#### D. Transition Temperatures

As Figure 1a shows, the sublattice magnetization drops to zero at some transition temperature  $T_n$ , commonly called the Néel temperature to distinguish it from the Curie temperature for a ferromagnet. This value of  $T_n$  can be calculated by expanding  $B_s(y)$  in powers of y, equation (59); then allowing  $M_0$  to approach zero, which means that T goes to  $T_n$  and y becomes small, so that in the first approximation one may write,

$$M_{0}/M_{s} = \frac{1}{3} \left( \frac{S+1}{S} \right) y$$
(87)

Now combining equations (55), (87), and the definition for  $M_s$ , one obtains,

$$T_{n} = \frac{1}{2} \frac{Ng^{2}\beta^{2}S(S+1)}{3k}\gamma = \frac{1}{2}C\gamma$$
(88)

This result neglects any external field. Comparing the calculated specific heat curve in Figure 1b with the zero field measured curve in Figure 14 indicates that the molecular-field theory can only give qualitative results.

The following discussion will consider the case for  $H \neq 0$ , and its effect on the transition temperature. The method of Kubo<sup>12</sup> will be used, although several calculations, using other methods, have been performed. These have been, (1) calculations of the phase diagram by Gorter,<sup>22</sup> who used the molecular-field theory to find the Gibb's energy, (2) the calculations by Garrett<sup>23</sup> who obtained a graphical solution for the field parallel to the magnetization using
using the molecular-field theory, (3) the method used by Temperley<sup>24</sup> to calculate a phase diagram for pure dipole interactions, and (4) the technique of Callen<sup>25</sup> to calculate the phase diagram using spin waves with a Green's function method.

The transition temperature for the case of the applied field, parallel to the magnetization direction will be calculated first. To do this, one starts with,

$$M_{a} = M_{s} B_{s}(y_{a}),$$
 (89)

$$M_{b} = M_{s} B_{s}(y_{b}),$$
 (90)

$$y_a = (g\beta S/kT)(H - \gamma M_b),$$
 (91)

and

$$y_{b} = (g\beta S/kT)(H + \gamma M_{a})$$
(92)

where the field is the total field and  $M_a$  is parallal and  $M_b$  is antiparallel to the applied field H. As the temperature is raised  $M_b$  first decreases in magnitude, becoming zero, then it becomes parallel to H and finally coincides with  $M_a$ . The temperature at which this occurs will be denoted by  $T_n(H)$ . Now writing from (92),

$$(\partial M_a / \partial y_b)_H = (kT/g\beta S)\gamma$$
 (93)

and from (89),

$$(\partial M_a / \partial y_a)_H = M_s \frac{\partial}{\partial y_a} \left[ B_s(y_a) \right]$$
 (94)

The slopes in (93) and (94) become equal as T approaches  $T_n(H)$  in (93) and as  $M_b \rightarrow M_a$  which become zero as T goes to  $T_n(O)$  in (94). Now expanding the Brillouin function, neglecting all terms of  $\gamma M_a$  and powers of H/T greater than 3, the combination of (93) and (94) may be written as,

$$\frac{k T_{n}(H)}{\gamma g \beta S} = M_{S} \left[ \frac{1}{3} \left( \frac{S+1}{S} \right) + \frac{3}{6} B_{S}''(0) \frac{g^{2} \beta^{2} S^{2}}{k^{2}} \left( \frac{H^{2}}{T_{n}^{2}(0)} \right) \right]$$
(95)

Now,

$$T_{n}(H) = \frac{1}{2} \frac{Ng^{2}\beta^{2}S^{2}\gamma}{k} \left[ \frac{1}{3} \left( \frac{S+1}{S} \right) + \frac{1}{2} B_{s}''(0) \frac{g^{2}\beta^{2}S^{2}}{k^{2}} \left( \frac{H}{T_{n}(0)} \right)^{2} \right]$$
(96)

Applying the definition of C, equation (63), (96) reduces to,

$$T_{n}(H) = \frac{1}{2} C\gamma + \frac{1}{4} B_{s}''(0) \frac{Ng^{4}\beta^{4}S^{4}}{k^{3}} \left(\frac{H}{T_{n}(0)}\right)^{2}$$
(97)

Multiplying and dividing the last term on the right by  $C^3$  one gets,

$$T_{n}(H) = \frac{1}{2} C\gamma + \frac{1}{4} B''_{s}(0) \frac{3^{3}C^{3}S\gamma}{(S+1)^{3}N^{2}g^{2}\beta^{2}} \left(\frac{H}{T_{n}(0)}\right)^{2}$$
(98)

$$= \frac{1}{2} C_{\gamma} + \frac{1}{4} B_{s}^{\prime \prime \prime}(0) \left(\frac{3S}{S+1}\right)^{3} \frac{\gamma C^{3}}{N^{2} g^{2} \beta^{2} S^{2}} \left(\frac{H}{T_{n}(0)}\right)^{2}$$
(99)

$$= \frac{1}{2} C_{\gamma} + \frac{1}{4} B_{s}'''(0) \left(\frac{3S}{S+1}\right)^{3} \frac{\left(\frac{\gamma C}{2}\right)^{3} 2^{3}}{4M_{s}^{2} \gamma^{2}} \left(\frac{H}{T_{n}(0)}\right)^{2}$$
(100)

Applying the definition of  $T_n(0)$  and  $\chi_1$  the final result is

$$\frac{T_{n}(H) - T_{n}(O)}{T_{n}(O)} = \frac{1}{2} B_{s}''(O) \left(\frac{3S}{S+1}\right)^{3} \frac{\chi_{\perp}^{2} H^{2}}{M_{s}^{2}}$$
(101)

Kubo goes on to do a calculation for the case of the field perpendicular to the direction of magnetization. He gets results similar to those for the parallel case (101),

$$\frac{T_{n}(H) - T_{n}(O)}{T_{n}(O)} = -kH^{2}$$

where k is a function of S, g,  $\beta$ , etc. and is smaller than the constant terms on the right side of equation (101).

Note that both (101) and (102) predict that  $T_n(H) < T_n(O)$ since  $B'_{s}$ '(O) is negative [see equation (60)].

### E. Spin-Flop

If a large enough external field is applied parallel to the direction of the sublattice magnetization at sufficiently low temperatures, a phenomenon called spin-flop<sup>12,22,25,26</sup> may occur.

Consider the crystalline anisotropy energy for a uniaxial antiferromagnetic crystal.

$$F_{K} = \frac{1}{2}K(\sin^{2}\theta_{a} + \sin^{2}\theta_{b})$$
(103)

where  $\theta_a$  and  $\theta_b$  are the angles between the sublattice magnetization  $M_a$  and  $M_b$  and the easy direction, the direction in which the magnetization lies with no external forces. K is the anisotropy coefficient and is assumed the same for

both lattices. Now making the further assumptions that  $\theta_a = \theta_b = \theta$  and  $M_a = M_b = M_o$ , equation (103) may be written as,

$$F_{\rm K} = K \sin^2 \theta \tag{104}$$

Let  $\rm H_{K}$  be a magnetic field associated with the anisotropy energy, and let it be the same for both  $\rm M_{a}$  and  $\rm M_{b}.$  Then,

$$F_{K} = -2H_{K}M_{o} \cos \theta \qquad (105)$$

Now for an arbitrary variation.

$$\delta F_{K} = 2H_{K}M_{o} \sin \theta \delta \theta \qquad (106)$$

$$\delta F_{K} = 2K \sin \theta \cos \theta \delta \theta$$
 (107)

Therefore,

but

$$H_{K} = (K \cos \theta) / M_{O}$$
(108)

Now apply an external field parallel to the easy direction. The change in energy per unit volume is,

$$\Delta E = -\int H dM \qquad (109)$$

$$dM = \chi dH \tag{110}$$

and 
$$\Delta E_{//} = -\chi_{//} H^2/2$$
 (111)

Suppose the magnetization is perpendicular to this direction then,

$$\Delta E_{\perp} = -H_{K}M_{o} \cos (\pi/2) + H_{K}M_{o} \cos (0) - \chi_{\perp}H^{2}/2$$
(112)

$$\Delta E_{\perp} = K - \chi_{\perp} H^2 / 2 \qquad (113)$$

Now let  $H_f$  be some external-field value such that  $\Delta E_{\perp} = \Delta E_{//}$  then,

$$-X_{//}H_{f}^{2}/2 = K - X_{\perp}H_{f}^{2}/2$$
(114)

and

$$H_{f} = \left[\frac{2K}{\chi_{\perp} - \chi_{//}}\right]^{1/2}$$
(115)

For antiferromagnetic materials,  $\chi_{\perp} > \chi_{//}$  when  $T < T_n$ , and there may exist a magnetic field  $H_f$  such that the magnetization will flop from the easy direction to a direction normal to the easy direction.

This phenomenon was first observed<sup>27</sup> in  $CuCl_2 \cdot 2H_2O$ with  $T_n = 4.3^{\circ}K$ . Maximum fields were applied in the present study to see if such an effect could be observed.

### III. EXPERIMENTAL APPARATUS AND PROCEDURE

#### A. Helium Dewar

Before any low-temperature work can be performed, a container which will hold the cryogenic fluid for a reasonable period of time is necessary. Figure 3 shows one such container. It is made from pyrex glass and essentially consists of two dewars with separate silvered vacuum jackets for insulation. A slit in the silver allows the interior to be seen. The bottom has a smaller diameter so that narrower pole gaps may be used in conjunction with an electromagnet thus providing higher, more homogeneous fields for magnetic measurements.

The outer dewar holds about three liters of inexpensive (relatively speaking) liquid nitrogen. The nitrogen acts as a pre-coolant and a radiation shield for the inner dewar. The liquid nitrogen needs replenishing at the rate of approximately one liter per hour. This is done automatically. Occasionally, about 1000 microns of dry nitrogen gas is admitted into the vacuum jacket of the inner dewar by means of the stopcock to facilitate pre-cooling. This gas will condense, producing a good vacuum insulation when the liquid helium is transferred into the inner dewar. The vacuum jacket of the inner dewar is evacuated periodically since



Fig. 3. A Magnetic Dewar.

pyrex is porous to helium at room temperature. The inner dewar is designed to be connected to a vacuum system which allows the vapor pressure of the liquid helium to be lowered, thus making it possible to reduce and control the temperature. For the calorimeter described below, a six-liter transfer will maintain good experimental conditions for about six hours.

## B. He<sup>4</sup> Calorimeter

Figures 4 and 5 are drawn to scale and show the calorimeter used for all of the experiments in the liquid  ${
m He}^4$ temperature region. Figure 6 is a photograph of the assembled calorimeter. This calorimeter is mounted in the previously described dewar which contains the liquid helium. The top and flanges of the calorimeter are machined from brass. The outer can, the inner liquid helium container, and the elbows are made from copper. The calorimeter can is made from brass. All copper-to-copper tubing joints are hard silver soldered where strength is necessary. The remaining joints are soft soldered. All evacuation lines or tubes are low-thermal-conducting alloys such as german silver or stainless steel. Not shown in the diagrams is a bellows which was installed in the outer can evacuation line. This was necessary after several soft-solder joints failed from thermal stresses due to cooling. The calorimeter can and the bottom of the outer can, which must be removable, are soldered in place with the low-melting Cerrolow 117 alloy solder using a liquid non-acid flux (Superior #30).



<u>Fig. 4.</u> Scale Drawing of Lower Portion of  $\text{He}^4$  Calorimeter.



<sup>&</sup>lt;u>Fig. 5.</u> Front and Side View of Top of  $He^4$ 

Calorimeter.



Fig. 6.--Photograph of Unassembled Calorimeter.

All evacuation lines in contact with room temperature must have some means of trapping the radiation flowing down them. This was achieved by having the lines turn right angle corners in the outer liquid helium bath where the radiation is absorbed. Any reflected radiation is reduced by radiation shields at the mouth of the outer can evacuation line, and the calorimeter can evacuation line.

The bottom of the outer can is removable to allow the calorimeter can to be centered while it is being soldered into place. Once this has been determined the outer can is tightened, the nylon spacer is positioned, and the bottom is soldered into place.

The outer can and its evacuation line are sealed by lead o-rings. Care must be taken to tighten the o-rings uniformly. When the o-ring grooves, which are little more than a scratch, were machined, a deeper groove of the same diameter was cut into a die. A three ampere Buss Fuse Wire is laid in the groove on the die and is cut to fill the groove. A low flame of an oxygen-gas torch is passed over the junction of the ends until they fuse to make an o-ring. A proficiency of nearly 70 percent in making good o-rings can be achieved with practice.

The fourteen formex coated 0.0031-inch diameter manganin electrical leads enter by means of kovar seals mounted in flanges sealed by rubber o-rings at the top of the system. They extend down the calorimeter evacuation line inside a length of teflon spaghetti, and make a twist around the tip

of the He<sup>4</sup> container. A small amount of G. E. #1202 varnish is applied to hold them in place and to make good thermal contact with this temperature. Eight of the leads go to one side of the epoxy therminal block. Four leads go to the 56 ohm, 1/10 watt Allen-Bradley resistor used as a bath thermometer. The resistor is glued into a hole cut in the tip of the He<sup>4</sup> container with G. E. #1202 varnish. The remaining two leads go to the 120 ohm, 1/10 watt Allen-Bradley resistor used as the bath heater which is glued into a similar hole.

Since the needle value is a critical part of the system, Figure 7 shows the working parts. It allows liquid helium to be drawn into the inner He<sup>4</sup> container. The needle value must be closed, isolating the inner He<sup>4</sup> container from the outer dewar. The smallest leak through this value increases the lowest temperature that could be attained.

## C. He<sup>3</sup> Calorimeter

The advantage of using liquid  $He^3$  is that temperatures as low as 0.4°K can easily be attained as compared to 1°K for  $He^4$ . Figure 8 shows a schematic of a  $He^3$  calorimeter used for one of the zero field experiments. It is similar to the  $He^4$  calorimeter except that the  $He^3$  section is completely isolated from the  $He^4$ . It also has an additional line for measuring the  $He^3$  vapor pressure. All removable cans are soldered using Cerrolow 117 alloy. The electrical leads enter the system at the top by means of a kovar seal, reaching the interior of the outer can by means of its



Fig. 7. The Needle Valve.



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Fig. 8. Schematic of He<sup>3</sup> Calorimeter.

evacuation line. Any thermal conduction down these leads is minimized by having the leads make good thermal contact to the liquid He<sup>4</sup> bath, and then to the liquid He<sup>3</sup> bath. The leads enter the calorimeter through the bottom by means of a platinum-glass seal.

These seals are made from ten 0.010-inch diameter platinum wires about six inches long, a  $\frac{1}{4}$ -inch diameter tubing, and soft-glass tubing. The platinum tube has one end feathered, i.e. a very sharply ground edge. The feathered end of the platinum tube is fused to the soft glass tubing. Each platinum wire is individually fused inside two inches of glass capillary tubing, and the ten are fused This bundle is fused inside the glass of the together. glass-platinum tube. If constructed properly with the proper glass, these seals are He II tight. Any well equipped glass blower can produce these seals. It has later been discovered that Wheatley's<sup>28</sup> method of sealing manganin wires inside metallic tubing using epoxy is also satisfactory at He II temperatures.

### D. Electrical Measurement Apparatus

The four separate circuits which are used to make the specific heat measurements are the bath heater, the bath thermometer, the sample thermometer, and the sample heater. The sample thermometer and sample heater circuits are diagrammed in Figure 9. There are three boxes labeled "Pot." Two of them are Leeds and Northrup K-3 potentiometers, and the one across  $R_p$  is a Leeds and Northrup K-2 potentiometer.



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HEATER CIRCUIT



Fig. 9. Electrical-Measurement Circuit Diagrams.

The "D. C. Ampl." boxes are Leeds and Northrup D. C. Voltage Amplifiers. The two boxes marked "Recorders" which connect to the D. C. amplifiers represent a single variable range card, Leeds and Northrup 2-pen Speedomax G recorder. The remaining recorder is a Leeds and Northrup single pen Speedomax G recorder. "Gav." is a Leeds and Northrup box type galvanometer. The precision resistors are all manufactured by General Radio.

The bath heater is the simplest of the four circuits. It consists of a 120 ohm, 1/10 watt Allen-Bradley resistor in series with a 10,000 ohm rheostat. These are across a 0-115 volt Variac. The a. c. heater current is controlled by both the rheostat and the Variac.

The voltage measurement across the bath thermometer is identical to the one shown in Figure 9. Since the bath thermometer is used only for control, the precise temperature is not required and the tolerances on the current supply need not be so stringent. A transistorized constant current supply is used and will not be discussed since it is not pertinent to the experiment. The bath thermometer, supplied with a current of ten microamperes, gives adequate sensitivity for a 56 ohm, 1/10 watt Allen-Bradley resistor.

In the sample thermometer circuit  $V_T$  is a pair of Mallory 28 volt mercury batteries connected in series,  $R_A$ is a 50 megohm resistor in series with a 10 megohm variable resistor for adjusting the current, and  $R_p$  is a 0.1 megohm precision resistor with a tolerance of 0.01 percent. The galvanometer will read null when the potentiometer across

 $R_p$  is set for 0.1 volt and  $R_A$  is adjusted to allow one microampere of current to flow through the circuit. The current is monitored continually and can be kept constant manually. However, adjustments were found unnecessary because the thermometer resistance changes were small compared to  $R_A$ .

The multiplying scale factor of the D. C. amplifier, the range of the recorder, and the thermometer current all determine the sensitivity of the recorder in measuring the emf across the thermometer. The range of each pen in the 2-pen recorder can be changed to 10, 5, or 1 millivolt full scale with zero left by using different range cards. The thermometer current cannot be adjusted freely since the greater the current the more power dissipated by the thermometer. It is set to give the maximum tolerable power, and any further sensitivity increases must be attained electronically.

The heater voltage is measured by the same techniques applied to determine the thermometer voltage. A recorder measures the voltage across a precision resistor which determines the heater current. Several different precision resistors are available to keep the voltage within the range of the recorder. The heater current is controlled by varying a resistor in series with the heater ( $R_v$  in Figure 9) and by adjusting the voltage through the number of cells selected from the battery supply. When switch A makes contact to the right, current is bypassed through  $R_H$ , the substitute heater which has the same resistance as the heater.

The current is allowed to pass through the heater when switch A makes contact to the left. At the same time switch C is closed allowing the potentiometer to monitor the heater voltage. A timer operates both switches and measures the time that current flows through the heater for energy measurements. The timer can be programmed either to shut off after a predetermined time or to be stopped manually. The use of the substitute heater for balancing purposes is to eliminate a pulse of unknown current in the heater due to the unbalance of the measuring recorder. The heater circuit potentiometer is also used, by appropriate switching, to measure the bath thermometer voltage, voltage across a precision resistor in either the bath circuit or in the heater circuit, or across any external potential.

### E. Preparation of Sample

There are six steps in the preparation of a sample for an experimental run: 1) the selection of a single crystal of adequate size, 2) deciding on the proper resistor to be used for the thermometer, 3) connecting manganin leads to the thermometer and the heater, 4) gluing the heater and the thermometer to the crystal, 5) mounting the sample in its holder, and 6) orientating the crystal in the field.

 $Cs_2MnCl_4 \cdot 2H_2O$  crystals were grown from an aqueous solution at room temperature of a mixture of  $CsCl_2$  and  $MnCl_2 \cdot 2H_2O$ .<sup>\*</sup> Two crystals about one inch long and 0.25 cm.<sup>2</sup> in cross section area weighing about one gram each were used.

\* Crystals were kindly supplied by Professor J. Cowen.

The resistance thermometer selected will depend upon the temperature range to be covered. A 10 ohm, 1/10 watt carbon Ohmite resistor gives the best results for He<sup>3</sup> temperatures and a 56 ohm, 1/10 watt carbon Allen-Bradley resistor works best for He<sup>4</sup> temperatures. The plastic coating on these resistors were not removed, since no problems with thermal equilibrium were noticed previously and the carbon would have to be recoated to prevent the absorption of gas.

The sample heater consists of twelve inches (about 450 ohms) of enamel coated Evenohm\* wire 0.0014 inch in diameter. About one-half inch of the insulation is stripped from both ends of the heater and the ends are tinned using regular solder with a resin core. Eight formex coated manganin wires about six inches long (approximately 15 ohms) and 0.0031 inch in diameter are used as leads. They also have their ends stripped and tinned. Two manganin leads are joined to each side of the heater and two leads are soldered as close as physically possible to each side of the thermometer resistor. The excess terminal wire on the thermometer is cut off. The pairs of leads on each side of the heater and the thermometer are wound around a nail to form a coil of about one-quarter inch in diameter. On both the heater and the thermometer two leads provide current flow and two leads allow the voltage to be measured.

After the surfaces have been coated with G. E. varnish #1202, the twelve inches of heater wire are wound as

<sup>\*</sup>Trade name for wire supplied by Wilber B. Driver Co., Newark, N.J.

non-inductively as possible around the crystal. The thermometer is tied to a smooth face of the crystal by means of a nylon thread and is covered by a drop of varnish for better thermal contact.

A C-shaped holder (see Figure 4) is made from onequarter inch german-silver tubing pressed into a metal strip. A nylon thread is looped through two small holes at the top and at the bottom, so that there are two parallel lines across the opening of the holder. The crystal is placed between these threads and held in place by an application of varnish. The tip of a small brass tack wedged between the loop of thread and the bottom of the holder pulls the sample rigid. A larger hole is drilled in the top to mount the holder to the tip of the inner helium container. The holder can be rotated about the mounting screw and all orientations of the crystal around this axis of rotation are possible.

The crystal is now orientated with respect to the field. The calorimeter system without the outer or inner calorimeter cans is positioned in the dewar. By use of a flashlight and the slit in the dewar, one of the previously placed marks on the epoxy terminal block is chosen to be normal to the magnetic field. The calorimeter system is then removed from the dewar and the chosen fiducial mark is then used to place two other similar indices on the epoxy, such that a line drawn through them is parallel to the field. The orientation of the crystal is made using these two latter

indices. It is estimated that there is an error of approximately 5° in this orientation technique.

After the above steps have been completed, the leads are soldered to the terminal block, which in turn connect them to the outside through the kovar seals at the top of the system.

#### F. Experimental Procedure

After the system has been prepared, the following is the step-by-step procedure necessary for taking data. Figure 10 shows a photograph of the total assembled system. For the name of pumps and valves etc. refer to Figure 11.

<u>1. Pre-Cooling</u>.--At least six hours before the transfer of liquid helium the outer dewar should be filled, and kept filled with liquid nitrogen. In preparation for this, evacuate the vacuum jacket of the inner dewar for about twenty minutes. In the meantime valve C is closed and the needle valve is opened. Just before the transfer of liquid nitrogen the inside of the dewar is evacuated with the large two inch Kinney pump (pump Y). The inner container is then flushed with helium gas and re-evacuated but care must be taken since pyrex glass is porous to helium gas at room temperature. With pump Y still pumping on the inner dewar, liquid nitrogen is added to the outer container.

Shortly after the liquid nitrogen has been transferred, pump Y is closed off and helium gas is added to the inner dewar to act as an exchange gas. This helium gas also keeps liquid oxygen from condensing and frost from clouding the



Fig. 10.--A Photograph of Total System.



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Fig. 11. Schematic Diagram of Top of Dewar.

inner dewar. The largest decrease in pressure of the helium gas due to its cooling occurs during the first hour after it has been added. From then on a three pound per square inch over-pressure will last twelve hours or longer.

Valves A and B are closed before or soon after the liquid nitrogen has been transferred.

2. Adding Exchange Gas. -- Sometime before the transfer of liquid helium, helium gas for heat exchange must be added to the calorimeter and outer cans. This should be done after the six-hour pre-cooling period, since the calorimeter will be evacuated and if the crystal is not cold enough it may be damaged. Valves A and B are opened to evacuate the cans. After twenty minutes the ion gauge should read about  $5 \times 10^{-4}$  millimeters of mercury; if not, a possibility of leaks in the seals or solder joints may be suspected. If there are no leaks, valves A and B are closed and the pumping line is flushed and filled with helium gas slightly above one millimeter of mercury. The pressure should read one millimeter of mercury after the opening of valves A and If the pressure is too high carefully pump it down, if Β. it is too low add more helium gas in the same manner as above.

Once the desired pressure is obtained values A and B are closed and the pumping line is evacuated. The system is now ready for the transfer of the liquid helium.

3. Liquid-Helium Transfer.--The needle value is closed and the vent of the liquid helium dewar is connected to the

recovery system by means of a hose. A rubber hose through which there is a slight flow of helium gas is connected to the pressurizing port of the transfer tube. The liquid helium storage container is moved into position and the transfer tube is lowered simultaneously into the storage container and dewar. The transfer tube is sealed from the atmosphere and pressure is applied to the surface of the liquid helium in the storage container by means of helium gas through the transfer tube's pressurizing port. Liquid helium will be forced over into the dewar and any vapor from the boiling due to the "warm" system is vented and recovered.

The liquid level is watched for, using the observation slit and a flashlight. When the level reaches the desired height the pressurizing gas is shut off and the transfer tube is removed. The container is sealed. If the system has been pre-cooled sufficiently a transfer of about six to seven liters will result.

The bath thermometer is watched and when its resistance has come to equilibrium at a value about ten times its room temperature resistance open the needle value filling the inner  $\text{He}^4$  container. Value B is opened to evacuate the outer can of exchange gas allowing the isolation of the inner  $\text{He}^4$  container thermally from the outer bath.

The electromagnet is turned on and the field is adjusted to the desired value. When the sample thermometer comes to equilibrium the first temperature calibration point is taken.

<u>4. The Calibration of Sample Thermometer</u>.--The thermometer resistance is calibrated against the helium vapor pressure whose temperatures are listed in the  $T_{58}$  liquid helium vapor pressure table.<sup>29</sup> After the thermometer has come to equilibrium the thermometer resistance, the mercury manometer readings, room temperatures, and height of liquid helium above the sample's position are recorded. The room temperature reading and height of liquid helium are unneccessary below the  $\lambda$ -point.

The needle valve is closed and valve C is opened. Immediately begin to slowly pump on the inner  $\mathrm{He}^4$  container with pump Y. The pumping speed is manually adjusted by opening and closing a valve, not shown, in the pumping line of Y. The vapor pressure is reduced ten centimeters on the mercury manometer and is manually held at this pressure by watching the bath thermometer and the manometer. This pressure is kept constant until the sample thermometer achieves an equilibrium resistance. This takes several minutes at the beginning and up to three quarters of an hour for the final calibration points. The thermometer equilibrium resistance and the vapor pressure are recorded. Continue to lower the pressure in ten centimeter steps until four centimeters pressure remain. This calibration point is recorded and then the oil manometer is connected to the system. This manometer is subsequently used for observing the pressure as the pumping valve is adjusted. Below 2.5 centimeters of mercury, the vapor pressure is read from the McLeod gauge. Continue to pump down in steps of ten centimeters

on the oil manometer. This procedure is maintained until all valves are open to pump Y and the lowest possible pressure is attained. This will give a temperature of approximately 1°K.

Since carbon resistors are used for the thermometers a temperature calibration must be made every time a resistor has had its temperature changed by approximately 20°K. Although it has been discovered that a magnetic field as high as 10,000 gauss does not change the temperature calibration within the tolerances of this study.

<u>5. Specific Heat Measurements</u>.--After recording the final temperature calibration point, the bath thermometer is turned off, valve B is closed, and valve A is opened evacuating the calorimeter of exchange gas and thermally isolating the sample. After five minutes the ion gauge should read approximately  $10^{-5}$  millimeters of mercury and specific heat data can be taken. The sample can never be completely isolated from its surroundings for there are always heat leaks due to radiation, and to thermal conduction along electrical leads and nylon threads. These heat leaks constitute the "background."

Since it is not always possible to eliminate the background, some means must be established to measure it or subtract off its heat.

A method of subtracting off the background heat is described using the lettered points in Figure 12. The figure shows how a portion of a recorder chart would appear. The



# Fig. 12. Sample Recorder Chart.

lines AB and CD represent the change in resistance due to the background heating. The slopes of these lines can be altered by changing the pumping speed of the bath or by supplying power to the bath heater which changes the temperature surrounding the sample. The slope of line BC is due to the background heat and the power added to the crystal by the sample heater. The resistance change resulting from the background heat while the sample heater was on can be eliminated in the following manner. Line EF is constructed midway between points B and C. Lines AB and CD are extended to cross EF.  $D_s$  and  $D_e$  represent the resistance change due only to the power put into the sample by this heater. The line segment B'D represents the resistance change from the background on first half of heating cycle and  $D_{\rho}C'$  is the resistance change from the background of final half of heating cycle. If the change in the temperature of the sample during the heating cycle is small compared to the temperature difference between the sample and its surroundings then  $B'D_s$  and  $D_eC'$  are equal. This is usually the case and it is preferred since no assumption is made as to where the background slope changed.

These lines are drawn and  $D_s$ ,  $D_e$ , heater current, heater voltage, and the time that the current flowed through the heater are recorded for each point as the experiment progresses. A specially constructed apron for the recorder, facilitates the drawing of the lines.

Before any specific heat data are taken the background heating of the sample is adjusted. When at the desired level

the potentiometer setting is changed to move the pen of the recorder to the extreme left. Here the resistance is recorded. This resistance corresponds to the thermometer resistance at the null position. This resistance is noted whenever the pen is moved from the extreme right to the extreme left of the recorder chart. This process is continued until the highest temperature desired is attained.

Since the specific heat of the sample may change, the difference between  $D_s$  and  $D_e$  will change. To obtain minimum scatter in specific heat points the heater current should be adjusted to maintain this difference greater than ten chart divisions in 20 to 30 seconds of heating.

<u>6. Voltage-Calibration Data</u>. -- Voltage calibration data are also taken while the specific heat points are being recorded. When the pen of the recorder reaches the right of the chart  $(D_r)$  due to the increase in temperature, the potentiometer setting is changed and the recorder pen moves back to the left  $(D_1)$ , see Figure 12. Two potentiometer settings, in terms of resistances, and the pen position, in chart divisions are recorded. Since neither the change in potentiometer setting nor the pen's movement can be instantaneous the slopes of the background heating are extrapolated to give the positions of the pen for an instantaneous movement across the chart. Continue taking this data until the last specific heat point has been recorded. The pen is moved to the left and the final voltage calibration point is taken.

7. Shut-down.--By the time the final point has been recorded pump Y may have been closed off and the system vented. To begin shut down, pump Y is opened to both outer and inner helium baths by opening the needle valve. Valve B is reopened and the diffusion pump on the high vacuum system is turned off allowing the cooling water and forepump to run. All electrical measuring equipment is switched off. Liquid nitrogen is maintained in the outer dewar until it is certain all of the liquid helium has been evaporated. When there is no more liquid helium in the inner dewar, pump Y is shut off, and the outer can, inner calorimeter can, and inner dewar are vented with dry nitrogen gas. When the diffusion pump is cold the forepump and cooling water are turned off.

#### G. Data Reduction

<u>1. Calibration of Thermometer</u>.--The T<sub>58</sub> liquid helium vapor-pressure table lists all of the vapor pressures in microns of mercury at 0°C. The mercury-manometer reading must be normalized from room temperature to 0°C. This correction is unnecessary for the McLeod gauge.

The vapor pressure must be corrected for the height of liquid helium above the level of the sample. Below the  $\lambda$ -point this correction becomes unnecessary, because He II has a very high thermal conductivity and the temperature is uniform throughout the liquid.

The calibration temperatures and their corresponding resistances are fitted to the two parameter Clement-Quinnell<sup>30</sup> equation,
$$\left[\frac{\log R}{T}\right]^{1/2} = a + b \log R$$
 (116)

by the method of least squares. The relative deviations from this curve are then fitted by the method of least squares to a sixth-degree polynomial,

$$\frac{\left[\frac{\log R}{T}\right]_{\text{meas.}}^{1/2} - \left[\frac{\log R}{T}\right]_{\text{calc.}}^{1/2} = \frac{6}{\sum_{n=0}^{\infty} C_n (\log R)^n} (117)$$

$$\frac{\left(\frac{\log R}{T}\right)_{\text{meas.}}^{1/2} = \sum_{n=0}^{\infty} C_n (\log R)^n (117)$$

where the  $C_n$ 's are arbitrary constants. The temperature is calculated from the resistance by combining the parameters of these two fitted equations into the following,

$$T = \log R \left[ \frac{a + b \log R}{1 - \sum_{n=0}^{6} C_n (\log R)^n} \right]^{-2}$$
(118)

Table 1 shows the temperature calibration, curve fitting results for an experiment made January 13, 1967. The maximum deviation is about ten millidegrees at the higher temperatures. This deviation becomes smaller for lower temperatures. Temperature changes of the order of one millidegree or less can be detected but the actual temperature is known only to ten millidegrees.

2. Voltage-Calibration.--The voltage calibration or the volts-per-division data is needed to calculate the thermometer resistance  $(R_t)$  from the potentiometer reading, when the recorder pen is not at the null position. When the

Table 1.	Temperature-Ca]	libration-Curve Par	ameters from an I	Experiment made
January 13, 196;	7.			
	61 = 1	1.813236, b = 0.470	429,	
C <sub>0</sub> = -3.570883, (	$c_{1} = 1.687682, C_{2}$	$2 = -0.2906558, C_3$	= 0.02152158, C <sub>4</sub>	<pre>= -0.0005747483</pre>
Measured Resistance (ohm)	Measured Temperature (°K)	Calculated Temperature (°K)	Difference (milli-°K)	Percent Difference
663.0	4.18660	4.17754	9.06	0.2163
709.5	4.00930	4.01017	- 0.77	-0.0193
764.0	3.83500	3.84114	-6.14	-0.1601
840.0	3.63890	3.64348	-4.58	-0.1258
946.2	3.41760	3.42127	-3.67	-0.1075
1,145.0	3.11810	3.11498	3.12	0.1001
1,538.0	2.73760	2.73287	4.73	0.1727
3,513.9	2.01490	2.01643	-1.53	-0.0759
4,308.4	1.88740	1.88764	-0.24	-0.0129
5,955.0	1.70620	1.70700	-0.80	-0.0467
10,010.2	1.46320	1.46210	1.10	0.0749
20,600.0	1.18470	1.18490	-0.20	-0.0170

thermometer is replaced by a variable resistor,  $R_t$  can be calculated from the equation,

$$R_{t} = \frac{R_{0} - C_{1}D}{1 + C_{2}D}$$
(119)

where  $R_0$  is the potentiometer reading divided by the thermometer current. D is the distance from the pen position to the null position on the recorder chart. This is taken as positive if the pen position is to the right of the null position and negative if it is to the left.  $C_1$  and  $C_2$  are obtained from a least-squares fit of the voltage-calibration data to the equation,

$$\frac{R_{01} - R_{02}}{D_1 - D_2} = C_1 + C_2 \left(\frac{R_{01} + R_{02}}{2}\right)$$

or

$$\Delta R / \Delta D = C_1 + C_2 \overline{R} . \qquad (121)$$

For the derivation of these equations see Appendix I.

When the variable resistor is replaced by the thermometer, the plot of  $\Delta R/\Delta D$  vs  $\overline{R}$  is fitted best by a thirddegree polynomial instead of (121). Table II gives the results of this fit. The necessity for such an analysis for the voltage-calibration curve is due to the off-balance readings of the potentiometer. Since such off-balance readings introduce an error current in the thermometer, the proper correction is necessary. Inserting an amplifier with a high-impedance input would reduce the error current, and

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One-Millivolt-Voltage	January 13, 1967.	
Table 2.	Experiment made	

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=1.99669 x 10 <sup>-1</sup> , C <sub>2</sub> =5.004588 x 10 <sup>-4</sup> , (

$\binom{R_0}{(ohms \times 10^3)}$	Measured $\Delta R/\Delta D$ (ohms/div.)	Calculated $\Delta R/\Delta D$ (ohms/div.)	Difference (ohms/div.)	Percent Difference
17.5809	8.7829	8.7413	0.0417	0.47
14.8228	7.3024	7.3710	-0.0686	-0.94
12.4671	6.0976	6.2255	-0.1279	-2.10
10.4346	5.4798	5.2488	0.2311	4.22
8.6217	4.4023	4.3821	0.0203	0.46
7.2512	3.6675	3.7273	-0.0599	-1.63
6.0750	3.1250	3.1643	-0.0393	-1.26
5.3227	2.8409	2.8031	0.0378	1.33
4.5363	2.3713	2.4244	-0.0531	-2.24
3.7382	2.0559	2.0383	0.0176	0.85

Table 2. (Continued)

$\begin{array}{c} R_{0} \\ \text{(ohms x 10^{3})} \end{array}$	Measured ∆R/∆D (ohms/div.)	Calculated $\Delta R/\Delta D$ (ohms/div.)	Difference (ohms/div.)	Percent Difference
3.2126	1.7801	1.7831	-0.0031	-0.17
2.6603	1.5133	1.5140	-0.0006	-0.04
2.3076	1.2976	1.3416	-0.0439	-3.38
1.9633	1.1667	1.1726	-0.0060	-0.51
1.5956	1.0081	0.9918	0.0163	1.62
1.3010	0.8538	0.8464	0.0074	0.87
1.0797	0.7511	0.7370	0.0141	1.87
0.8645	0.6466	0.6304	0.0162	2.50

it has been tried with several amplifiers, but the noise level was increased beyond a tolerable level.

An empirical formula which gives  $R_t$ , using the cubic fit,  $R_0$ , and D has been derived by trial and error. This is,

$$R_{t} = \frac{R_{0} - \left[C_{1} - C_{2}R - 2C_{3}R^{2} - 3C_{4}R^{3}\right]D}{1 + \left[C_{2} + 2C_{3}R + 3C_{4}R^{2}\right]D}$$
(122)

where the C's are the coefficients of the third-degree polynomial fit, and  $R_t$  in the first approximation, is calculated using  $R = R_0$ . The calculation is iterated using  $R = R_t$  until the previous calculated value differs by 0.1 percent from the final value.

<u>3. Specific Heat Data</u>.--The specific heat of the point ABCD in Figure 12 can now be calculated. The resistance at  $D_s$  and  $D_e$  are determined using the voltage-calibration data and the empirical formula. The temperature for these resistances are computed using the thermometer calibration equation. The heater current ( $I_h$ ), heater voltage ( $V_h$ ), the time of heating (t), and the mass of the sample in moles (M) have all been measured. Therefore  $C_m$  may be written as,

$$C_{m} = \frac{I_{h} \times V_{h} \times t}{(T_{e} - T_{s})M}$$
 (123)

The specific heat  $(C_m)$  curve is the plot of  $C_m$  versus  $\overline{T}$ where  $\overline{T} = \frac{1}{2}(T_e + T_s)$ , the average of the temperatures calculated from  $D_e$  and  $D_s$ . There are several possible sources of errors, but the largest is reading distances on the chart. The scatter caused by this error, as mentioned before, is kept to a minimum by keeping the difference between  $D_e$  and  $D_s$  greater than ten small divisions, where the chart is divided into 100 of these divisions. Another source of error is the additional heat capacities of the thermometer, heater wire, and varnish. This error is largest at 4°K and the calculation indicates that it contributes approximately 2.8 percent of the total specific heat at that temperature.

### IV. RESULTS AND DISCUSSION

# A. Description of Crystal

The samples each consisting of a single crystal of  $Cs_2MnCl_4 \cdot 2H_2O$  were studied. They both are about one inch long with a cross sectional area of 0.25 cm<sup>2</sup>. The mass of sample 1 is 1.353 grams or 0.00272 mole, and the mass of sample 2 is 0.905 gram or 0.00181 mole, using 498.63 grams/ mole as the molecular weight. S. J. Jensen<sup>30</sup> has made an x-ray study of  $Cs_2MnCl_4 \cdot 2H_2O$ . The crystals are triclinic, of space group PI with one formula unit per unit cell. The parameters are:

a	=	5.75Å	α	=	67.0°
b	=	6.66Å	β	=	87.8°
с	=	7.27Å	γ	=	84.3°

Figure 13 shows a cross section of the crystal and identifies several faces.

## B. Zero Field Results

Four separate specific heat studies were made in a zero magnetic field. Two studies were made on sample 1 in the He<sup>4</sup> calorimeter between  $1.4^{\circ} - 5.0^{\circ}$ K. Sample 2 was studied first in the He<sup>4</sup> calorimeter, and then secondly in the He<sup>3</sup> calorimeter between 0.6° and 3.0°K. Figure 14 shows these results plotted as a function of temperature, and



<u>Fig. 13</u>. A Cross Sectional View of  $Cs_2MnCl_4 \cdot 2H_2O$ Perpendicular to the Elongated Axis with an Arrow Indicating the Direction of Easy Magnetization.



Appendix II, Tables 3, 4, 5, and 6 list the experimental values. The transition temperature is  $1.84^\circ \pm 0.01^\circ$ K.

The specific heat curve shown in Figure 14 is the total specific heat. This includes the lattice specific heat, the specific heat due to the nuclear-spin interaction, and that due to the spin-spin exchange interaction. The electronic specific heat will be negligible since the samples are non-metals. The specific heat measurements of  $MnF_2$  made by Cooke and Edmond<sup>31</sup> suggest that the nuclear-spin interaction contributes less than 2 percent at 0.6°K. Since this interaction tails off as  $1/T^2$ , it will contribute even less at higher temperature.

To calculate the lattice contribution the well known  $Debye^{32}$  function is used,

$$C_{L} = 9Nk \left(\frac{T}{\theta}\right)^{3} \int_{0}^{\theta/T} \frac{x^{4}}{(e^{x} - 1)(1 - e^{-x})} dx$$
 (124)

where  $\theta$  is a constant and called the Debye theta, and x is given by  $M\omega/kT$ . For low temperature the integral can be approximated by a constant, so that,

$$C_{L} = DT^{3}$$
(125)

Van Vleck has indicated that the specific heat above the Néel temperature, i.e. in the paramagnetic state, may be written as,

$$C_{\rm m} = A/T^2 + B/T^3 + C/T^4$$
 (126)

where A, B, and C are arbitrary. Combining (125) and (126) the total specific heat above  $T_n$  is,

$$C_{T} = A/T^{2} + B/T^{3} + C/T^{4} + DT^{3}$$
 (127)

Fitting (127) by the method of least squares, to the specific heat data above 2.2°K gives A = 8.24, B = -14.95, C = 22.39, and D = 0.00118. The Debye theta calculated from D is found to be 73°K.  $C_L$  represents 14 percent of  $C_T$  at 4.0°K but the area under the  $C_L$  curve is just 1 percent of the total area under the curve in Figure 14. Therefore the curve in Figure 14 may be considered the specific heat for the exchange interaction only. The dashed curve in Figure 14 represents the specific heat, calculated from the parallel susceptibility results, equation (86), where  $(TX_{//})_{\infty}$  was found to be 3.01°K·cc/mole. The agreement is remarkably good in the light of the approximation made for equation (86).

If the total change in entropy is calculated graphically, using (17), between 0° and 2.2°K, and mathematically, using (126) between 2.2°K and  $\infty$ , it is found to be 3.75 cal./mole.°K. (The extrapolated value from 0° - 0.6°K amounts to 0.13 cal./mole.°K.) This value compares favorably with the theoretical value, 3.56 cal./mole.°K, computed from equation (18) using J = 5/2. Some short range ordering above the transition temperature is indicated since 25 percent of the measured entropy is recovered above the Néel temperature.

The exchange energy, evaluated by computing the area under the magnetic specific heat curve, is equal to 7.25 cal./mole. Using this energy value, together with S = 5/2, and the expression for  $E_{ex}$ , equation (57),  $T_n$  can be calculated. The calculated value of 3.4°K is almost twice the measured value of 1.84°K for the transition temperature. This would indicate that the molecular-field theory does not give exact agreement as far as details are concerned, although it appears to predict the qualitative features.

In the temperature region  $0.6^{\circ} - 1.6^{\circ}K$ ,  $C_{\rm m}$  is found to fit a curve of the form,

$$C_{m} = 0.94T^{3.22}$$
(128)

Now from equation (58), this may be written as,

$$\int C_{\rm m} dT = k \int M dM \qquad (129)$$

where k is just a constant of proportionality. Then,

$$aT^{4.22} = (k/2)M^2 + p$$
 (130)

where a = 0.94/4.22 and p is the constant of integration. At T = T<sub>n</sub>, M = 0 thus,

$$p = aT_n^{4.22}$$
, (131)

but at T = 0,  $M = M_s$  and,

$$p = -(k/2)M_s^2$$
 (132)

Divide by p and write,

$$(T/T_n)^{4.22} = -(M/M_s)^2 + 1$$
 (133)

Solving for  $M/M_s$  one obtains,

$$M/M_{s} = \left[1 - (T/T_{n})^{4.22}\right]^{1/2}$$
(134)

Burley,  $^{33}$  using a three dimensional Ising model and, by expanding the partition function and extrapolating to T<sub>n</sub> predicts that near T<sub>n</sub>,

$$M/M_{s} \sim (1 - T/T_{n})^{m}$$
 (135)

where m is between 0.25 and 0.50. Plotting log  $(M/M_S)$  as measuring in (134) against log  $(1 - T/T_n)$  the slope of the best straight line will be m. Using only points close to  $T_n$ , m is found to be 0.27. Figure 15 shows  $M/M_S$  plotted as a function of reduced temperature for the specific heat results, for the calculation of Burley's f.c.c. model, and for the calculation based on the molecular-field theory with S = 5/2. Figure 15 also show the sublattice magnetization as measured by nmr. The specific heat results agree fairly well with the nmr data, and appear to be better represented by the Burley calculation than by the molecularfield theory. Again, the molecular-field theory appears to represent the experimental results in a qualitative way.

### C. Magnetic-Field Results

Using the zero field transition temperature for  $Cs_2MnCl_4 \cdot 2H_2O$  an order of magnitude of the critical field  $(H_c)$ , the value of the field needed to break the exchange forces at 0°K, can be calculated from the expression



Fig. 15. Sublattice Magnetization Curves.

 $g\beta SH_c/kT_n = 1.^{23}$  This gives  $H_c = 5500$  gauss. Since fields of almost 10,000 gauss are available, the specific heat measured in a magnetic field should show an observable difference from the similar study in a zero field.

The specific heat of sample 1 has been measured in several applied magnetic fields for each of three different orientations of the crystal. Two separate runs were made for each field and orientation. The three orientations are A, B, and C in the directions (0 T T), (1 T T), and (T T T) respectively, as shown in Figure 13. Figure 16, 17, and 18 show the results of the specific heat measurements for three different fields for orientation A, and Appendix II, Tables 7-12 list the results. Figure 19 and 20 show the results for orientation B and two applied fields, and Appendix II, Tables 13-16 list the results. Figures 21, 22, 23, 24, and 25 show the specific heat results for orientation C for five applied fields, and Appendix II, Tables 17-26 list the experimental values.

It should be noted that the transition temperature decreases with increasing magnetic field for all three orientations, and that the lowest transition temperature occurred for orientations C in an applied field of 9830 gauss. This phenomenon is predicted from the theory and will be discussed in Section D. (Phase Diagram). Qualitatively, one can also see that, in general, the specific heat peaks become sharper as the field is increased and this is reflected in the entropy curves.





















Figures 26, 27, and 28 show the entropy as calculated from the specific heats. The curves in Figure 26 and 27 are normalized by extrapolating the  $C_m/T$  curves to 0°K. The curves in Figure 28 are normalized to the zero field entropy curve by an adiabatic magnetization experiment. This experiment was performed in the following way. The sample was thermally isolated and the temperatures were measured as the field was increased to a maximum and then decreased to zero. Table 27 in Appendix II list these temperatures. The entropy remains constant and its value for each magnetization is found from the zero field entropy curve. The points shown in Figure 28 are the results of this experiment.

Figures 29, 30, and 31 are three-dimensional plots of entropy, magnetic field, and temperature. These results indicate that at low temperatures, adiabatic magnetization may produce cooling by as much as  $0.3^{\circ}$ K, when the field is increased from zero to 8900 gauss.

## D. Phase Diagram

Figure 32 is a plot of the applied magnetic field against the transition temperature, called the H-T phase diagram. All points to the right and above the curves are in the paramagnetic state and all points to the left and below the curves are in the antiferromagnetic state. The smooth curves were plotted assuming the points of each orientation follow the  $H^2$  dependence as given by equation (101). Orientation C is the direction closest to the easy





Fig. 27. Entropy Curves for Orientation B.





Entropy, Field, and Temperature Surface for Orientation A. Fig. 29.





Entropy, Field, Temperature Surface for Orientation C. 31. Fig.



direction of magnetization since it has the greatest curvature. This agrees with the nmr and susceptibility results.

Using the slope of the straight line fit to the T vs H<sup>2</sup> plot and S = 5/2, X<sub>⊥</sub> is calculated using equation (101). X<sub>⊥</sub> is found to be 0.58 cc/mole compared to the maximum of the parallel susceptibility curve which is 0.64 cc/mole. This is a reasonably good check on the reliability of equation (101).

Comparing the curvatures of the three curves on the phase diagram gives: C/B = 3.6, C/A = 1.6, and A/B = 2.2. The errors in these ratios may be as large as 45 percent because of the insufficient data in the A and B directions.

If spin-flop had occurred then the curvature of C would approximate that of B below the spin-flop transition temperature as indicated on Figure 32 by the dashed curve. Since this did not happen, it is believed that no spin-flop took place under the present experimental conditions. This does not preclude the possibility that such a spin-flop transition may occur at lower temperatures using higher fields. This suggestion is prompted by the fact that there may be large anisotropy in this crystal. Such anisotropy is also revealed in the magnetic susceptibility results.

#### E. Conclusions

In this specific heat study of single crystals of  $Cs_2MnCl_4 \cdot 2H_2O$ , the following conclusions may be drawn:

1. The zero-field experimental data cannot be fitted, in detail, by the molecular-field theory, although the general qualitative features may be seen.

2. The specific heat curve in zero-field agrees quite well with the curve predicted by Fisher using the magnetic susceptibility results.

3. The non-zero-field results are in agreement with the modified form of the molecular-field theory. It was possible to predict  $T_n(H)$  as a function of H, as well as verifying the value of  $\chi_{\parallel}$ .

4. The entropy curves predict the possibility of cooling by adiabatic magnetization in the low temperature region.

5. A spin-flop transition was not observed.

In connection with the failure to observe a spin-flop transition, several additional comments may be added. Since large anisotropy is indicated, higher-field measurements at lower temperatures are necessary before any definite statement can be made concerning the existence of a spin-flop transition in  $Cs_2MnCl_4 \cdot 2H_2O$ . Furthermore, it has been observed in  $CuCl_2 \cdot 2H_2O^{34}$  that a misalignment of the applied field from the axis of easy magnetization by as little as 5° could explain the non-observation of the spin-flop transition. This is on the very edge of the uncertainty in the alignment in the present experiment. A possible method for improved alignment is suggested in Figure 33.

Figure 33 is a plot of the temperature change caused by rotating the magnet, at a constant field, under adiabatic conditions. The three points are from the approximate 8000 gauss entropy curves (for entropy = 1.35 cal./mole.°K) of




92

(wyoy)

the three different orientations. The curve is drawn assuming 2-fold symmetry, although the present crystal has only an inversion axis and the angles between A, B, and C are approximate. This method, however, will still be useful. On the right of Figure 33 are the resistances of the thermometer for the three plotted points. Therefore enough sensitivity exists so that by simply rotating the magnet and watching the thermometer, the crystal can be aligned so that the external field will be parallel to the direction of magnetization. This is achieved when maximum resistance is attained on the thermometer.

Neutron-diffraction studies would also be useful to help confirm the axis of easy magnetization.

Referring again to Figure 33, if a spin-flop transition did occur for a field of 8000 gauss at orientation C the spins would now be ordered in the same configuration as they would be in orientation B. It would appear that the temperatures for these two configurations should be identical for the same entropy value. Then if the crystal is adiabatically rotated in constant magnetic field from orientation B to orientation C, the temperatures would change as shown in Figure 33 until within approximately 5° of orientation C. Since spin-flop can only occur within approximately 5° of the easy direction, the temperature in Figure 33 will rise from about 1.20° to 1.34°K, the value of the temperature for orientation B. This is indicated by the dashed curve in Figure 33, and may be another method for detecting

the spin-flop transition. Justification for this technique would be evident from the fact that the three-dimensional S-H-T curves would show a depression in their surface.

In the above discussion it has been tacitly assumed that the shape of the crystal does not affect the results. To test the affect of the shape of the sample it would be necessary to grow larger crystals and grind them into spheres, etc. and repeat the experiment. In this way it may be possible to determine whether the field is uniform over the entire length of the crystal.

The effect of the external magnetic field on the nuclear-spin specific heat has, of course, been neglected, just as it was for the zero-field measurements. Such effects will not appear much before very low temperatures, and in external fields, probably greater than 50,000 gauss, since it would involve the further splitting of the nuclearspin levels.

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## APPENDIX I

Using Kirchoff's Circuit Law for the current loop  $I_{\mu}$  in Figure 34 one can write,

$$(I_{e} - I_{p})R_{p} + I_{e}R + (I_{e} + I_{t})R_{t} = 0$$
(1)

where  $I_p$  is the potentiometer current,  $R_p$  is the potentiometer resistance,  $R_t$  is the thermometer resistance,  $I_t$  is the thermometer current, R is the lead resistance, and  $I_e$ is the unbalance current. When  $I_e = 0$  then  $I_pR_p = I_tR_t$ . Thus  $I_pR_p = V_o$ , where  $V_o$  is the voltage read from the potentiometer. Rewriting (1) using  $V_o$  one gets,

$$(1 - I_e/I_p)V_o = I_eR + (1 + I_e/I_t)I_tT_t.$$
 (2)

 $I_e$  has been measured and found to be proportional to the recorder-pen deflection from zero, positive when deflected to the right and negative when deflected to the left. Let D be the deflections measured in chart divisions.  $I_e$ has never exceeded 0.1 microampere in any of the experiments to date.  $I_p$  is never less than 200 microamperes, therefore,  $I_e/I_p$  is always less than 0.0005 which can be neglected compared to 1. So that (2) may be written as,

$$V_{o} = \alpha DR + (1 + \alpha D/I_{+})I_{+}R$$
(3)

where  $I_e = \alpha D$  and  $\alpha$  is a proportionality constant depending



Fig. 34. Circuit Diagram for a Simple Potentiometer.

upon the range card and the D. C. amplifier scale factor. The  $\alpha$ 's of different scales differ by an integral multiplying factor.

Since  $I_t$  is held constant, let  $R_0 = V_0/I_t$  then (3) becomes,

$$R_0 = (\alpha/I_t)RD + [1 + (\alpha/I_t)D]R_t$$
(4)

Keeping  $R_t$  and R constant change the voltage setting on the potentiometer, and obtain,

$$R_{01} = (\alpha/I_t)RD_1 + [1 + (\alpha/I_t)D_1]R_t$$
 (5)

$$R_{02} = (\alpha/I_t)RD_2 + [1 + (\alpha/I_t)D_2]R_t$$
(6)

Subtracting (6) from (5), gives,

$$R_{01} - R_{02} = (\alpha/I_t)(R + R_t)(D_1 - D_2)$$
(7)

or

$$\Delta R_0 / \Delta D = C_1 + C_2 R_t$$
(8)

where  $C_1 = (\alpha/I_t)R$  and  $C_2 = \alpha/I_t$ . Solving equation (4) for  $R_t$  gives,

$$R_{t} = [R_{0} - (\alpha/I_{t})RD] / [1 + (\alpha/I_{t})D]$$
(9)

or finally,

$$R_{t} = \frac{R_{0} - C_{1}D}{1 + C_{2}D}.$$
 (10)

<u>Table 3</u>. The Specific Heat of  $Cs_2MnCl_4 \cdot 2H_2O$  for Sample 1, Run 2, September 16, 1966, Zero Field.

Cm	dT	T	Cm	dT	T	Cm	dT	Т
2.959	0.001	1.408	3.719	0.002	1.548	4.573	0.003	1.664
3.032	0.003	1.414	3.831	0.002	1.556	4.495	0.003	1.669
3.026	0.003	1.423	3.664	0.002	1.560	4.506	0.003	1.674
2.904	0.003	1.428	3.550	0.002	1.564	4.706	0.003	1.680
2.947	0.003	1.434	3.804	0.002	1.568	4.982	0.002	1.689
3.147	0.002	1.443	4.045	0.002	1.572	4.885	0.003	1.694
3.118	0.003	1.449	3.789	0.002	1.576	4.845	0.003	1.698
3.091	0.003	1.455	3.848	0.003	1.580	4.909	0.002	1.703
3.299	0.002	1.463	3.856	0.003	1.585	4.825	0.003	1.709
3.239	0.002	1.468	4.052	0.003	1.590	4.890	0.002	1.713
3.269	0.002	1.474	4.094	0.003	1.594	5.188	0.002	1.717
3.322	0.002	1.482	4.053	0.003	1.600	5.200	0.002	1.721
3.293	0.002	1.487	3.929	0.003	1.604	5.212	0.002	1.725
3.265	0.002	1.492	3.936	0.003	1.608	5.766	0.002	1.729
3.383	0.002	1.499	4.179	0.003	1.611	5.301	0.002	1.735
3.321	0.002	1.504	4.297	0.003	1.615	5.246	0.002	1.738
3.324	0.002	1.509	4.250	0.003	1.620	5.748	0.002	1.742
3.500	0.002	1.516	4.113	0.003	1.625	5.333	0.002	1.746
3.468	0.002	1.521	4.088	0.003	1.630	5.663	0.005	1.751
3.508	0.002	1.525	4.134	0.003	1.636	6.091	0.005	1.760
3.664	0.002	1.530	4.537	0.003	1.643	6.230	0.005	1.767
3.401	0.002	1.535	4.505	0.003	1.648	6.293	0.004	1.774
3.441	0.002	1.540	4.309	0.003	1.653	6.764	0.004	1.782
3.633	0.002	1.544	4.320	0.003	1.658	6.786	0.004	1.789

Table 3 (Continued)

	dT	Т	Cm	Tb	Т	C <sub>m</sub>	Tb	Т
7.165	0.004	1.795	1.362	0.014	2.091	0.573	0.033	3.214
7.525	0.004	1.801	1.399	0.013	2.119	0.542	0.035	3.258
7.832	0.004	1.810	1.289	0.015	2.147	0.521	0.036	3.311
7.917	0.004	1.815	1.242	0,015	2.182	0.502	0.037	3.356
8.440	0.003	1.820	1.122	0.017	2.217	0.498	0.038	3.429
9.034	0.003	1.826	1.124	0.017	2.256	0.489	0.039	3.485
9.906	0.003	1.832	1.077	0.017	2.294	0.472	0.040	3.554
7.022	0.004	1.837	1.041	0.018	2.332	0.462	0.041	3.612
3.787	0.007	1.846	0.999	0.019	2.369	0.449	0.042	3.691
2.798	0.010	1.860	0.960	0.020	2.409	0.429	0.044	3.757
2.502	0.011	1.873	0.944	0.020	2.450	0.421	0.045	3.837
2.277	0.012	1.890	0.898	0.021	2.496	0.412	0.046	3.906
2.151	0.013	1.905	0.872	0.022	2.546	0.396	0.048	4.002
1.988	0.014	1.922	0.856	0.022	2.591	0.391	0.048	4.078
1.882	0.015	1.938	0.826	0.023	2.641	0.377	0.050	4.194
1.809	0.016	1.955	0.763	0.025	2.695	0.363	0.052	4.279
1.740	0.016	1.972	0.759	0.025	2.744	0.358	0.053	4.391
1.648	0.011	1.986	0.734	0.026	2.795	0.342	0.055	4.480
1.603	0.012	1.997	0.701	0.027	2.846	0.339	0.055	4.621
1.624	0.012	2.009	0.670	0.028	2.897	0.329	0.057	4.716
1.561	0.012	2.020	0.650	0.029	2.949	0.325	0.058	4.832
1.606	0.012	2.032	0.629	0.030	3.005	0.322	0.058	4.913
1.563	0.012	2.044	0.601	0.031	3.066	0.318	0.059	4.986
1.608	0.012	2.056	0.558	0.034	3.119	0.315	0.063	5.077
1.481	0.013	2.068	0.573	0.033	3.160	0.309	0.064	5.158

<u>Table 4</u>. The Specific Heat of  $Cs_2MnCl_4 \cdot 2H_2O$  for Sample 1, Run 3, September 21, 1966, Zero Field

Cm	dT	Т	Cm	dT	Т	Cm	dT	Т
3.019	0.004	1.365	4.348	0.004	1.594	7.128	0.004	1.794
2.774	0.003	1.381	4.492	0.004	1.600	7.462	0.004	1.802
2.953	0.003	1.399	4.454	0.004	1.610	7.613	0.004	1.808
3.089	0.004	1.411	4.535	0.004	1.616	7.948	0.004	1.814
3.093	0.004	1.423	4.048	0.005	1.623	8.060	0.004	1.819
3.252	0.004	1.438	4.998	0.004	1.630	8.594	0.003	1.826
3.414	0.004	1.452	4.932	0.004	1.636	9.289	0.003	1.832
3.390	0.004	1.459	4.951	0.004	1.646	10.010	0.003	1.838
3.501	0.004	1.468	5.028	0.004	1.652	10.410	0.003	1.843
3.473	0.004	1.475	5.063	0.006	1.663	11.057	0.003	1.849
3.597	0.003	1.484	5.217	0.005	1.673	10.347	0.003	1.853
3.621	0.003	1.491	5.292	0.005	1.684	4.981	0.006	1.860
3.594	0.003	1.501	5.442	0.005	1.693	3.399	0.008	1.872
3.655	0.003	1.506	5.569	0.005	1.704	3.036	0.006	1.883
3.724	0.003	1.515	5.857	0.005	1.712	2.598	0.007	1.896
3.766	0.003	1.521	5.811	0.005	1.724	2.478	0.008	1.906
3.820	0.003	1.529	5.916	0.005	1.731	2.313	0.008	1.920
3.911	0.003	1.535	6.080	0.005	1.742	2.198	0.009	1.931
4.015	0.005	1.544	6.166	0.005	1.749	2.058	0.009	1.947
4.062	0.005	1.551	6.216	0.005	1.758	1.976	0.010	1.962
4.165	0.005	1.561	6.382	0.004	1.765	1.899	0.010	1.974
4.123	0.005	1.568	6.718	0.004	1.772	1.864	0.010	1.992
4.252	0.004	1.578	6.834	0.004	1.781	1.788	0.011	2.005
4.325	0.004	1.585	6.736	0.004	1.787	1.703	0.011	2.023

Table 4 (Continued)

C <sub>m</sub>	đΤ	Т	Cm	dT	Т	Cm	ТЪ	Т
1.667	0.011	2.037	1.071	0.018	2.371	0.621	0.030	3.140
1.606	0.012	2.055	1.044	0.018	2.416	0.597	0.032	3.214
1.583	0.012	2.070	0.958	0.020	2.463	0.597	0.032	3.300
1.494	0.013	2.088	0.924	0.020	2.505	0.554	0.034	3.382
1.473	0.013	2.104	0.915	0.021	2.552	0.559	0.034	3.474
1.412	0.013	2.126	0.832	0.023	2.602	0.533	0.036	3.570
1.381	0.014	2.144	0.861	0.022	2.653	0.521	0.036	3.682
1.347	0.014	2.161	0.819	0.023	2.707	0.498	0.038	3.782
1.413	0.013	2.178	0.768	0.025	2.762	0.537	0.035	3.849
1.306	0.015	2.195	0.727	0.026	2.818	0.486	0.039	3.955
1.273	0.015	2.223	0.725	0.026	2.877	0.475	0.040	4.063
1.222	0.015	2.253	0.711	0.027	2.935	0.493	0.038	4.127
1.153	0.016	2.293	0.694	0.027	3.005	0.401	0.047	5.015
1.068	0.018	2.329	0.659	0.029	3.072	0.497	0.038	5.207
						0.496	0.057	5.281

C <sub>m</sub>	dT	T	Cm	dT	Т	C <sub>m</sub>	dT	Т
3.322	0.006	1.417	4.670	0.009	1.635	10.292	0.004	1.835
3.294	0.006	1.430	4.775	0.009	1.650	10.233	0.004	1.840
3.245	0.006	1.442	4.959	0.008	1.665	4.624	0.009	1.848
3.418	0.005	1.450	5.120	0.008	1.679	3.216	0.009	1.861
3.291	0.006	1.461	5.230	0.008	1.692	2.917	0.009	1.872
3.362	0.005	1.475	5.520	0.007	1.703	2.529	0.011	1.887
3.477	0.005	1.484	5.657	0.007	1.718	2.363	0.012	1.900
3.460	0.005	1.494	5.823	0.007	1.727	2.192	0.013	1.917
3.566	0.005	1.509	5.902	0.007	1.740	2.065	0.013	1.935
3.658	0.005	1.516	6.285	0.007	1.749	1.948	0.014	1.954
3.713	0.005	1.526	6.424	0.006	1.762	1.872	0.015	1.972
3.817	0.005	1.535	6.280	0.007	1.770	1.772	0.016	1.991
3.679	0.005	1.545	6.901	0.006	1.780	1.708	0.016	2.011
3.873	0.005	1.553	7.086	0.006	1.788	1.649	0.017	2.032
3.912	0.005	1.563	7.351	0.006	1.796	1.596	0.017	2.052
3.994	0.005	1.571	7.542	0.005	1.804	1.527	0.018	2.075
4.095	0.004	1.581	7.979	0.005	1.811	1.475	0.019	2.098
4.188	0.004	1.588	8.271	0.005	1.817	1.430	0.019	2.121
4.170	0.010	1.601	8.902	0.005	1.823	1.426	0.019	2.140
4.355	0.009	1.618	9.637	0.004	1.830	1.404	0.020	2.159

Table 5 (Continued)

C <sub>m</sub>	dT	Т	Cm	dT	Т	Cm	dТ	Т
1.359	0.020	2.190	0.853	0.032	2.659	0.559	0.049	3.421
1.373	0.020	2.221	0.826	0.033	2.723	0.587	0.047	3.506
1.288	0.021	2.257	0.814	0.034	2.781	0.624	0.044	3.595
1.216	0.023	2.300	0.746	0.037	2.848	0.655	0.021	3.665
1.178	0.023	2.343	0.727	0.038	2.910	0.492	0.056	3.820
1.101	0.025	2.388	0.684	0.040	2.982	0.607	0.023	3.904
1.057	0.026	2.437	0.646	0.043	3.069	0.576	0.048	4.006
1.020	0.027	2.487	0.603	0.046	3.147	0.413	0.033	4.233
0.972	0.028	2.541	0.578	0.048	3.237	0.552	0.025	4.290
0.886	0.031	2.601	0.563	0.049	3.331	0.587	0.023	4.395
						0.519	0.026	4.506

C <sub>m</sub>	dT	Т	C <sub>m</sub>	dТ	Т	Cm	dT	Т
0.856	0.012	0.673	1.473	0.014	0.844	2.533	0.036	1.215
0.838	0.013	0.686	1.453	0.015	0.855	2.644	0.035	1.227
0.818	0.013	0.701	1.522	0.012	0.863	2.665	0.034	1.253
0.928	0.011	0.714	1.561	0.012	0.871	2.854	0.073	1.292
0.965	0.011	0.722	1.585	0.011	0.880	3.146	0.067	1.350
1.025	0.010	0.732	1.609	0.011	0.888	3.494	0.060	1.403
1.061	0.010	0.740	1.620	0.025	0.899	3.771	0.056	1.445
1.147	0.009	0.747	1.663	0.024	0.916	4.022	0.052	1.483
1.111	0.010	0.752	1.734	0.023	0.928	4.142.	0.051	1.515
1.151	0.009	0.759	1.751	0.023	0.945	4.371	0.048	1.545
1.112	0.010	0.764	1.767	0.023	0.961	4.565	0.046	1.569
1.181	0.009	0.768	1.819	0.022	0.978	4.497	0.047	1.585
1.216	0.009	0.772	1.846	0.022	0.994	5.074	0.093	1.633
1.263	0.015	0.782	1.832	0.022	1.007	6.218	0.076	1.700
1.293	0.015	0.793	1.898	0.021	1.019	7.800	0.061	1.749
1.340	0.014	0.802	1.924	0.021	1.034	5.328	0.089	1.814
1.332	0.014	0.810	1.920	0.021	1.038	2.044	0.232	1.933
1.336	0.014	0.820	2.043	0.049	1.064	1.428	0.331	2.143
1.398	0.013	0.827	2.159	0.045	1.103	1.185	0.400	2.333
1.425	0.015	0.833	2.234	0.041	1.132	0.917	0.516	2.608
1.420	0.009	0.836	2.319	0.039	1.162	0.763	0.620	2.926
			2.428	0.038	1.190	0.639	0.741	3.255

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Cm	dT	Т	C <sub>m</sub>	dT	Т	C <sub>m</sub>	dT	T
1.655	0.004	1.040	2.689	0.018	1.324	1.231	0.059	2.035
1.707	0.007	1.045	2.861	0.017	1.343	1.180	0.062	2.080
1.635	0.008	1.052	2.995	0.026	1.363	1.312	0.055	2.113
1.766	0.028	1.069	3.145	0.024	1.388	1.199	0.061	2.057
1.722	0.016	1.086	3.225	0.024	1.410	1.174	0.062	2.118
1.909	0.014	1.099	3.475	0.022	1.432	1.121	0.065	2.175
1.924	0.014	1.111	3.618	0.021	1.453	1.063	0.068	2.232
1.934	0.014	1.123	4.054	0.019	1.485	1.007	0.072	2.288
1.884	0.014	1.134	4.567	0.024	1.546	1.028	0.071	2.352
1.923	0.014	1.145	4.887	0.022	1.573	0.927	0.078	2.453
2.024	0.013	1.156	5.271	0.021	1.596	0.909	0.080	2.547
2.027	0.020	1.160	5.606	0.019	1.617	0.810	0.090	2.647
2.094	0.019	1.178	6.913	0.016	1.635	0.775	0.094	2.743
2.102	0.019	1.195	7.320	0.015	1.650	0.759	0.096	2.900
2.315	0.017	1.211	11.166	0.019	1.667	0.716	0.102	3.013
2.168	0.018	1.227	15.555	0.014	1.683	0.604	0.121	3.140
2.289	0.017	1.243	3.157	0.129	1.754	0.605	0.120	3.238
2.346	0.017	1.257	1.565	0.053	1.840	0.542	0.134	3.333
2.442	0.016	1.273	1.465	0.050	1.887	0.542	0.134	3.428
2.470	0.016	1.287	1.339	0.054	1.936	0.506	0.216	3.661
2.588	0.019	1.303	1.288	0.056	1.985	0.611	0.179	3.972
						0.446	0.245	4.297

<u>Table 7</u>. The Specific Heat of  $Cs_2MnCl_4 \cdot 2H_2O$  for Sample 1, Run 5, December 23, 1966, 8150 Gauss, Orientation A.

Table 8.	The Specific	Heat of $Cs_2MnCl_4 \cdot 2H_2O$ for Sample
l, Run 6, Janua	ary 12, 1967,	8150 Gauss, Orientation A.

C <sub>m</sub>	dT	Т	C <sub>m</sub>	dT	Т	C <sub>m</sub>	dT	T
2.178	0.004	1.186	3.124	0.016	1.412	12.112	0.008	1.685
2.166	0.004	1.190	3.114	0.016	1.429	3.634	0.027	1.708
2.270	0.005	1.193	3.161	0.016	1.445	2.427	0.023	1.731
2.149	0.014	1.200	3.654	0.014	1.460	2.059	0.029	1.752
2.289	0.013	1.213	3.769	0.013	1.474	1.886	0.032	1.779
2.294	0.015	1.225	3.859	0.013	1.487	1.722	0.034	1.799
2.326	0.012	1.237	3.976	0.013	1.500	1.761	0.023	1.830
2.417	0.012	1.247	4.363	0.007	1.510	1.500	0.028	1.863
2.497	0.010	1.256	4.418	0.026	1.527	1.551	0.019	1.886
2.455	0.010	1.265	4.656	0.025	1.553	1.531	0.019	1.905
2.520	0.011	1.274	4.997	0.023	1.576	1.602	0.018	1.923
2.437	0.020	1.290	4.891	0.023	1.598	1.507	0.019	1.942
2.527	0.019	1.309	5.860	0.020	1.618	1.508	0.019	1.958
2.802	0.018	1.327	6.371	0.018	1.637	1.485	0.019	1.977
2.849	0.018	1.344	7.249	0.016	1.653	1.421	0.020	1.997
2.873	0.018	1.383	7.807	0.015	1.667	1.475	0.019	2.016
2.887	0.012	1.398	9.706	0.010	1.678	1.372	0.021	2.037

	Table 8	(Continued)
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C <sub>m</sub>	dT	T	Cm	dT	Т	Cm	dT	T
1.431	0.020	2.057	0.762	0.038	2.654	0.512	0.056	3.444
1.388	0.021	2.069	0.790	0.040	2.719	0.506	0.057	3.556
1.150	0.025	2.102	0.765	0.041	2.776	0.466	0.061	3.636
1.153	0.025	2.139	0.748	0.038	2.832	0.489	0.058	3.706
1.176	0.024	2.172	0.727	0.039	2.900	0.478	0.060	3.770
1.067	0.027	2.212	0.684	0.042	2.956	0.508	0.056	3.828
1.035	0.028	2.262	0.635	0.045	3.029	0.523	0.055	3.883
0.935	0.031	2.315	0.638	0.045	3.095	0.580	0.049	3.935
0.839	0.034	2.418	0.595	0.048	3.200	0.656	0.044	3.982
0.889	0.032	2.490	0.685	0.042	3.284	0.634	0.045	4.026
0.875	0.032	2.560	0.545	0.052	3.369	0.505	0.057	4.066

C<sub>m</sub> dT C<sub>m</sub> dT T Τb C<sub>m</sub> T T 2.083 0.009 1.190 3.916 0.013 1.496 1.681 0.020 1.954 3.774 0.013 1.509 2.231 0.009 1.198 1.517 0.034 2.005 2.429 0.012 1.206 1.428 0.035 2.053 4.154 0.012 1.522 2.269 0.013 1.215 3.961 0.013 1.534 1.320 0.040 2.105 2.298 0.012 1.227 4.081 0.029 1.554 1.254 0.042 2.151 2.431 0.012 1.238 4.424 0.021 1.580 1.202 0.043 2.195 2.519 0.011 1.246 4.938 0.019 1.600 1.155 0.045 2.239 2.421 0.012 1.256 4.477 0.021 1.618 1.196 0.044 2.284 2.536 0.011 1.266 5.252 0.018 1.637 1.063 0.049 2.321 2.492 0.011 1.277 5.188 0.018 1.655 1.059 0.049 2.363 2,561 0,011 1.289 5.766 0.016 1.673 0.929 0.056 2.434 2.594 0.011 1.300 6.070 0.016 1.689 0.905 0.058 2.537 0.861 0.061 2.632 2.729 0.010 1.309 5.801 0.016 1.704 2.801 0.010 1.319 7.037 0.017 1.720 0.821 0.064 2.770 2.841 0.018 1.333 7.881 0.015 1.736 0.754 0.069 2.876 2.820 0.018 1.350 8.986 0.013 1.750 0.676 0.077 3.019 0.692 0.073 3.130 2.833 0.018 1.366 11.160 0.011 1.761 2.784 0.018 1.379 6.262 0.019 1.777 0.607 0.086 3.280 3.040 0.017 1.395 2.763 0.034 1.803 0.576 0.091 3.405 3.125 0.016 1.421 2.297 0.033 1.834 0.544 0.096 3.523 3.410 0.015 1.435 2.023 0.017 1.857 0.495 0.105 3.695 3.518 0.014 1.454 2.018 0.026 1.869 0.484 0.108 3.809 0.588 0.089 3.907 3.518 0.014 1.468 1.897 0.028 1.895 0.463 0.113 4.026 3.628 0.014 1.482 1.823 0.029 1.920

<u>Table 9</u>. The Specific Heat of  $Cs_2MnCl_4 \cdot 2H_2O$  for Sample 1, Run 7, January 13, 1967, 5150 Gauss, Orientation A.

C <sub>m</sub>	dT	T	Cm	dT	Т	C <sub>m</sub>	dT	Т
1.796	0.008	1.138	3.465	0.015	1.506	1.480	0.034	2.070
1.824	0.008	1.146	3.461	0.015	1.521	1.257	0.040	2.144
2.121	0.007	1.153	3.500	0.015	1.535	1.224	0.041	2.192
2.153	0.014	1.164	3.493	0.015	1.550	1.132	0.045	2.242
2.144	0.013	1.177	4.075	0.012	1.563	1.097	0.046	2.287
2.134	0.013	1.189	3.809	0.013	1.576	1.095	0.046	2.333
2.172	0.013	1.201	4.368	0.012	1.590	0.981	0.051	2.416
2.257	0.013	1.210	4.639	0.025	1.608	0.868	0.058	2.507
2.277	0.013	1.221	4.949	0.023	1.632	0.788	0.064	2.630
2.297	0.012	1.231	5.185	0.022	1.654	0.709	0.071	2.819
2.316	0.012	1.241	5.313	0.022	1.675	0.682	0.074	2.934
2.398	0.012	1.252	6.233	0.018	1.695	0.628	0.080	3.085
2.666	0.011	1.271	6.847	0.017	1.712	0.537	0.094	3.209
2.806	0.010	1.288	7.355	0.016	1.728	0.626	0.080	3.308
2.853	0.010	1.306	8.341	0.014	1.743	0.533	0.095	3.432
2.646	0.011	1.327	8.864	0.013	1.756	0.489	0.103	3.552
2.860	0.010	1.342	11.579	0.010	1.767	0.488	0.103	3.673
2.851	0.010	1.359	3.957	0.029	1.787	0.514	0.098	3.797
3.033	0.009	1.377	2.482	0.033	1.816	0.449	0.112	3.942
3.239	0.016	1.397	2.112	0.035	1.848	0.423	0.119	4.088
2.795	0.018	1.421	1.919	0.040	1.884			
3.490	0.015	1.448	1.719	0.044	1.923			
3.674	0.014	1.467	1.520	0.050	1.967			
3.718	0.014	1.486	1.563	0.032	2.021			

<u>Table 10</u>. The Specific Heat of  $Cs_2MnCl_4 \cdot 2H_2O$  for Sample 1, Run 8, January 18, 1967, 5150 Gauss, Orientation A.

<u>Table 11</u>. The Specific Heat of  $Cs_2MnCl_4 \cdot 2H_2O$  for Sample 1, Run 9, January 20, 1967, 3500 Gauss, Orientation A.

C <sub>m</sub>	dT	Т	Cm	dT	Т	Cm	dT	Т
1.757	0.011	1.007	2.534	0.011	1.286	3.897	0.013	1.589
1.962	0.010	1.016	2.556	0.011	1.296	4.034	0.013	1.602
1.920	0.010	1.024	2.640	0.011	1.306	4.722	0.011	1.616
1.630	0.012	1.032	2.613	0.011	1.316	4.763	0.024	1.633
1.897	0.010	1.056	2.623	0.011	1.326	5.062	0.023	1.656
2.051	0.009	1.071	2.647	0.011	1.336	5.280	0.022	1.678
2.021	0.009	1.084	2.536	0.011	1.345	6.179	0.018	1.720
1.776	0.011	1.099	3.096	0.009	1.354	6.783	0.017	1.738
1.950	0.010	1.109	2.804	0.010	1.362	6.868	0.017	1.754
2.046	0.009	1.119	2.885	0.010	1.370	7.625	0.015	1.770
1.987	0.009	1.128	2.857	0.010	1.379	10.244	0.011	1.798
2.049	0.009	1.144	2.976	0.017	1.391	6.231	0.018	1.812
2.015	0.009	1.152	2.949	0.017	1.404	3.032	0.022	1.832
2.033	0.009	1.160	3.084	0.017	1.421	2.548	0.022	1.853
2.026	0.009	1.168	3.153	0.016	1.438	2.321	0.025	1.877
2.123	0.009	1.176	3.230	0.016	1.454	1.866	0.031	1.902
2.089	0.013	1.190	3.326	0.015	1.472	1.913	0.030	1.929
2.122	0.013	1.206	3.263	0.016	1.487	2.026	0.017	1.949
2.186	0.013	1.219	3.463	0.015	1.503	1.975	0.017	1.966
2.281	0.012	1.232	3.300	0.015	1.518	1.898	0.018	1.983
2.074	0.014	1.242	3.717	0.014	1.535	1.789	0.019	2.002
2.366	0.012	1.255	3.603	0.014	1.549	1.789	0.019	2.020
2.400	0.012	1.265	3.813	0.013	1.563	1.687	0.020	2.039
2.376	0.012	1.276	4.007	0.013	1.576	1.486	0.023	2.052

Table 11 (Continued)

C <sub>m</sub>	dT	Т	C <sub>m</sub>	dT	Т	Cm	dT	Т
1.417	0.024	2.079	1.008	0.034	2.400	0.675	0.075	2.879
1.329	0.025	2.105	0.964	0.035	2.441	0.624	0.082	3.033
1.349	0.025	2.131	0.974	0.035	2.494	0.597	0.085	3.186
1.268	0.027	2.158	0.875	0.039	2.534	0.534	0.095	3.374
1.182	0.029	2.186	0.890	0.038	2.575	0.498	0.102	3.529
1.280	0.026	2.217	0.856	0.040	2.616	0.478	0.106	3.674
1.198	0.028	2.249	0.840	0.040	2.655	0.461	0.110	3.843
1.145	0.030	2.281	0.853	0.040	2.696	0.508	0.100	3.996
1.125	0.030	2.322	0.965	0.035	2.734	0.403	0.126	4.165
1.047	0.032	2.360	0.801	0.063	2.783			

<u>Table 12</u>. The Specific Heat of  $Cs_2MnCl_4 \cdot 2H_2O$  for Sample 1, Run 10, January 23, 1967, 3500 Gauss, Orientation A.

C <sub>m</sub>	dT	T	Cm	dT	T	Cm	Tb	T
1.542	0.012	0.979	2.301	0.008	1.238	3.628	0.014	1.514
1.542	0.012	0.990	2.375	0.008	1.246	4.533	0.011	1.526
1.516	0.013	1.000	2.464	0.014	1.257	4.229	0.012	1.546
1.533	0.012	1.011	2.432	0.014	1.270	4.386	0.012	1.572
1.587	0.012	1.020	2.427	0.014	1.283	4.400	0.017	1.594
1.485	0.013	1.050	2.532	0.013	1.295	4.735	0.016	1.616
1.862	0.010	1.077	2.486	0.014	1.308	4.967	0.015	1.639
1.825	0.010	1.107	2.948	0.011	1.336	5.167	0.015	1.660
2.078	0.009	1.128	2.920	0.012	1.354	5.406	0.014	1.680
2.207	0.009	1.152	3.076	0.016	1.379	5.935	0.013	1.709
1.959	0.010	1.167	3.072	0.017	1.401	6.351	0.018	1.730
2.143	0.009	1.179	2.874	0.018	1.420	7.016	0.016	1.752
1.913	0.010	1.192	2.870	0.018	1.439	7.264	0.016	1.772
1.893	0.010	1.203	3.269	0.016	1.456	7.325	0.016	1.791
2.223	0.009	1.213	3.336	0.015	1.471	9.397	0.009	1.804
2.226	0.009	1.221	3.514	0.014	1.486	5.077	0.014	1.815
2.300	0.008	1.230	3.476	0.015	1.500	2.683	0.013	1.828

Table 12 (Continued)

Cm	dT	Т	Cm	đT	Т	Cm	Ъ	T
2.365	0.024	1.847	1.262	0.040	2.163	0.765	0.066	2.836
2.421	0.011	1.867	1.238	0.041	2.204	0.762	0.067	2.952
2.067	0.021	1.892	1.176	0.043	2.245	0.673	0.076	3.112
1.622	0.021	1.921	1.169	0.044	2.288	0 625	0.081	3.228
1.813	0.019	1.945	1.166	0.044	2.332	0.611	0.083	3.332
1.780	0.019	1.970	1.118	0.045	2.374	0.522	0.097	3.541
1.605	0.021	1.998	0.960	0.053	2.419	0.594	0.086	3.659
1.583	0.021	2.023	0.942	0.054	2.457	0.530	0.096	3.791
1.471	0.023	2.051	0.932	0.055	2.495	0.535	0.095	3.961
1.362	0.037	2.084	0.880	0.058	2.597	0.493	0.103	4.103
1.280	0.040	2.123	0.856	0.059	2.702			

Cm	dT	Т	Cm	dT	Т	Cm	Ъ	Т
2.421	0.011	1.206	3.320	0.016	1.404	4.476	0.012	1.599
2.762	0.014	1.218	3.152	0.017	1.416	4.595	0.011	1.609
2.719	0.012	1.230	3.401	0.015	1.429	4.799	0.007	1.618
2.700	0.012	1.239	3.366	0.016	1.442	5.096	0.007	1.624
2.710	0.012	1.250	3.428	0.015	1.455	4.807	0.007	1.630
2.730	0.012	1.255	3.492	0.015	1.468	5.143	0.007	1.636
2.700	0.012	1.264	3.639	0.014	1.480	4.926	0.007	1.641
2.719	0.012	1.273	3.532	0.015	1.493	5.362	0.006	1.647
2.736	0.012	1.283	3.692	0.014	1.503	4.890	0.004	1.651
2.741	0.012	1.294	3.924	0.013	1.515	5.149	0.007	1.654
2.688	0.013	1.305	3.852	0.014	1.527	5.968	0.006	1.664
3.099	0.011	1.312	3.949	0.013	1.539	5.620	0.006	1.669
2.936	0.018	1.325	4.013	0.013	1.549	5.642	0.006	1.674
2.843	0.018	1.342	4.176	0.013	1.561	5.374	0.007	1.678
2.907	0.018	1.358	4.184	0.013	1.572	5.627	0.006	1.682
3.073	0.017	1.373	4.329	0.012	1.580	6.127	0.006	1.686
3.093	0.017	1.388	4.289	0.012	1.591	5.614	0.006	1.691

<u>Table 13</u>. The Specific Heat of  $Cs_2MnCl_4 \cdot 2H_2O$  for Sample 1, Run 12, February 11, 1967, 8400 Gauss, Orientation B.

Table 13 (Continued)

C <sub>m</sub>	dT	Т	Cm	Ъ	Т	Cm	ТБ	Т
6.819	0.005	1.695	7.710	0.005	1.735	1.162	0.045	2.152
5.737	0.006	1.700	7.196	0.007	1.740	1.188	0.044	2.196
7.195	0.005	1.705	8.032	0.007	1.745	1.224	0.043	2.241
8.083	0.004	1.709	8.131	0.006	1.750	1.075	0.049	2.287
6.610	0.005	1.714	8.312	0.006	1.754	1.081	0.048	2.336
7.093	0.005	1.718	8.934	0.006	1.758	1.063	0.049	2.384
6.953	0.005	1.723	9.990	0.005	1.763	1.085	0.048	2.432
6.525	0.005	1.726	1.313	0.028	2.035	1.000	0.052	2.482
7.320	0.005	1.730	1.299	0.040	2.069	0.722	0.072	2.536
6.700	0.005	1.733	1.288	0.041	2.109			

<u>Table</u>	<u>14</u> . The	Specific	Heat of	$Cs_2MnCl_4 \cdot 2H_2O$	for Sample
1, Run 13, 1	February	13, 1967,	, 8400 G	auss, Orientat	ion B.

C <sub>m</sub>	Τb	Т	C <sub>m</sub>	ТБ	Т	Cm	Tb	Т
2.634	0.013	1.196	3.332	0.010	1.377	4.635	0.011	1.598
2.889	0.012	1.207	3.230	0.015	1.390	4.607	0.011	1.608
2.832	0.012	1.217	3.134	0.016	1.403	4.849	0.010	1.618
2.765	0.012	1.227	3.005	0.017	1.423	5.032	0.010	1.627
2.657	0.013	1.234	3.499	0.014	1.439	5.069	0.010	1.637
2.687	0.012	1.243	3.612	0.014	1.453	5.050	0.010	1.646
2.746	0.012	1.253	3.571	0.014	1.467	5.030	0.010	1.656
2.730	0.012	1.263	3.553	0.014	1.481	4.986	0.010	1.665
2.673	0.012	1.273	3.397	0.015	1.491	5.056	0.010	1.674
2.745	0.012	1.283	4.021	0.012	1.505	5.622	0.009	1.687
2.733	0.012	1.300	3.944	0.013	1.517	6.177	0.008	1.697
2.927	0.011	1.312	4.079	0.012	1.530	5.709	0.009	1.708
2.906	0.011	1.324	4.029	0.012	1.542	5.608	0.009	1.719
2.903	0.011	1.335	4.010	0.012	1.553	6.408	0.008	1.727
2.918	0.011	1.346	4.691	0.011	1.565	6.642	0.008	1.735
2.780	0.012	1.356	4.468	0.011	1.576	7.002	0.007	1.742
3.173	0.011	1.367	4.594	0.011	1.587	7.397	0.007	1.749

Table 14 (Continued)

C <sub>m</sub>	Τb	Т	C <sub>m</sub>	Τb	Т	C <sub>m</sub>	Tb	Т
8.447	0.006	1.755	1.329	0.038	2.066	0.654	0.077	3.018
7.723	0.006	1.761	1.248	0.040	2.124	0.624	0.080	3.104
10.091	0.005	1.767	1.201	0.042	2.176	0.628	0.080	3.184
8.163	0.006	1.772	1.143	0.044	2.235	0.662	0.076	3.262
3.906	0.013	1.782	1.060	0.047	2.299	0.573	0.087	3.329
2.772	0.012	1.795	0.948	0.053	2.360	0.591	0.085	3.421
2.509	0.013	1.807	0.944	0.053	2.423	0.589	0.085	3.506
2.733	0.012	1.823	0.892	0.056	2.503	0.564	0.089	3.572
2.212	0.015	1.845	0.840	0.060	2.571	0.487	0.103	3.656
2.037	0.025	1.876	0.801	0.062	2.645	0.446	0.112	3.799
1.729	0.029	1.921	0.747	0.067	2.742	0.456	0.110	3.959
1.537	0.033	1.974	0.714	0.070	2.827	0.544	0.092	4.124
1.425	0.035	2.022	0.903	0.055	2.910	0.482	0.104	4.312

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<u>Table 15</u>. The Specific Heat of  $Cs_2MnCl_4 \cdot 2H_2O$  for Sample 1, Run 14, February 16, 1967, 6050 Gauss, Orientation B.

Cm	dT	T	C <sub>m</sub>	dT	Τ	Cm	dT	Т
2.221	0.015	1.193	3.133	0.011	1.415	5.105	0.010	1.641
2.487	0.014	1.207	3.159	0.011	1.425	5.248	0.010	1.651
2.484	0.014	1.218	3.173	0.011	1.451	5.510	0.009	1.660
2.448	0.014	1.230	3.340	0.010	1.465	5.431	0.009	1.670
2.436	0.014	1.241	3.453	0.010	1.478	6.072	0.019	1.706
2.551	0.013	1.251	3.037	0.011	1.490	6.690	0.017	1.724
2.620	0.013	1.262	3.609	0.009	1.500	6.979	0.016	1.741
2.686	0.013	1.272	3.586	0.009	1.510	7.383	0.015	1.756
2.624	0.013	1.283	3.116	0.016	1.523	9.825	0.012	1.785
2.634	0.013	1.293	3.934	0.013	1.537	6.116	0.019	1.800
2.506	0.014	1.308	4.102	0.012	1.550	3.318	0.015	1.817
2.981	0.011	1.321	4.093	0.012	1.562	2.710	0.019	1.835
3.002	0.011	1.332	4.202	0.012	1.575	2.473	0.020	1.854
2.930	0.012	1.343	4.620	0.011	1.586	2.088	0.024	1.875
2.876	0.012	1.354	4.698	0.011	1.610	2.046	0.025	1.899
2.758	0.012	1.392	4.925	0.010	1.621	1.973	0.026	1.925
3.019	0.011	1.404	5.065	0.010	1.631	2.042	0.025	1.946

Table 15 (Continued)

Cm	Τb	Т	Cm	dT	Т	C <sub>m</sub>	dT	Т
1.523	0.033	2.004	0.763	0.066	2.843	0.544	0.093	3.705
1.403	0.036	2.055	0.744	0.068	2.935	0.582	0.087	3.739
1.354	0.037	2.103	0.666	0.076	3.046	0.581	0.087	3.826
1.293	0.039	2.162	0.641	0.079	3.134	0.548	0.092	3.886
1.164	0.044	2.217	0.636	0.080	3.213	0.531	0.095	3.948
1.115	0.045	2.276	0.670	0.076	3.290	0.485	0.104	4.009
1.037	0.049	2.358	0.701	0.072	3.370	0.489	0.103	4.070
1.012	0.050	2.438	0.666	0.076	3.445	0.505	0.100	4.124
0.892	0.057	2.544	0.599	0.085	3.512	0.504	0.101	4.183
0.849	0.060	2.635	0.596	0.085	3.579	0.529	0.096	4.238
0.781	0.065	2.745	0.558	0.091	3.648			

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<u>Table 16</u>. The Specific Heat of  $Cs_2MnCl_4 \cdot 2H_2O$  for Sample 1, Run 15, February 16, 1967, 6050 Gauss, Orientation B.

C <sub>m</sub>	dT	Т	Cm	dT	Т	Cm	dT	Т
2.612	0.013	1.194	3.223	0.010	1.381	4.218	0.012	1.574
2.835	0.012	1.205	3.293	0.010	1.396	4.417	0.011	1.581
2.621	0.013	1.216	3.209	0.010	1.405	4.498	0.011	1.590
2.646	0.013	1.226	3.294	0.010	1.413	4.422	0.011	1.600
2.658	0.013	1.236	3.188	0.011	1.422	4.709	0.011	1.610
2.364	0.014	1.251	2.978	0.011	1.431	4.774	0.024	1.626
2.710	0.012	1.265	3.404	0.015	1.443	4.870	0.023	1.649
2.781	0.012	1.276	3.420	0.015	1.456	5.199	0.022	1.665
2.854	0.012	1.288	3.515	0.014	1.469	5.877	0.019	1.686
2.732	0.012	1.299	3.614	0.014	1.483	5.964	0.019	1.705
2.534	0.013	1.310	3.605	0.014	1.495	6.180	0.019	1.723
2.897	0.012	1.321	3.655	0.014	1.506	6.187	0.018	1.740
2.889	0.012	1.331	3.835	0.013	1.517	7.831	0.015	1.759
2.860	0.012	1.341	3.857	0.013	1.529	7.774	0.015	1.773
2.938	0.011	1.351	4.107	0.012	1.540	8.762	0.013	1.785
2.945	0.011	1.361	4.156	0.012	1.552	9.161	0.012	1.797
2.745	0.012	1.369	4.083	0.012	1.563	3.713	0.026	1.815

Table 16 (Continued)

Cm	dT	Т	Cm	dT	Т	Cm	dT	Т
2.631	0.019	1.835	1.440	0.035	2.086	0.678	0.075	2.959
2.637	0.019	1.844	1.350	0.037	2.136	0.537	0.094	3.073
2.354	0.022	1.864	1.323	0.038	2.181	0.586	0.086	3.252
2.216	0.023	1.886	1.201	0.042	2.243	0.570	0.089	3.374
2.096	0.024	1.910	1.181	0.043	2.306	0.508	0.100	3.484
2.021	0.025	1.935	1.139	0.044	2.398	0.524	0.097	3.591
1.799	0.028	1.960	0.994	0.051	2.507	0.530	0.096	3.687
1.722	0.029	1.997	0.798	0.063	2.668	0.534	0.095	3.777
1.598	0.032	2.035	0.754	0.067	2.790			

<u>Table 17</u>. The Specific Heat of  $Cs_2MnCl_4 \cdot 2H_2O$  for Sample 1, Run 16, March 1, 1967, 8400 Gauss, Orientation C.

C <sub>m</sub>	Tb	Т	Cm	Τb	T	Cm	ТБ	T
4.372	0.007	1.396	9.276	0.005	1.522	1.637	0.021	1.727
5.016	0.006	1.402	9.343	0.005	1.527	1.555	0.022	1.745
5.293	0.005	1.408	9.565	0.005	1.533	1.426	0.024	1.821
5.238	0.005	1.413	9.709	0.005	1.537	1.427	0.024	1.845
5.058	0.010	1.421	9.412	0.005	1.542	1.435	0.024	1.869
5.031	0.010	1.431	9.476	0.005	1.547	1.375	0.025	1.889
5.002	0.010	1.440	8.589	0.006	1.553	1.289	0.026	1.912
5.192	0.010	1.449	8.653	0.006	1.559	1.265	0.027	1.945
5.077	0.010	1.458	8.717	0.006	1.565	1.242	0.027	1.981
5.464	0.009	1.466	6.593	0.014	1.580	1.189	0.028	2.030
5.875	0.009	1.474	2.908	0.019	1.602	1.177	0.029	2.068
6.202	0.008	1.482	2.164	0.017	1.622	1.163	0.029	2.102
7.066	0.007	1.490	2.048	0.017	1.639	1.045	0.032	2.145
7.415	0.007	1.497	1.950	0.017	1.656	1.007	0.034	2.181
7.288	0.007	1.503	1.803	0.019	1.673	1.005	0.034	2.215
8.087	0.006	1.510	1.699	0.020	1.691	1.057	0.032	2.248
8.393	0.006	1.516	1.556	0.022	1.708	1.196	0.028	2.270

Table 17 (Continued)

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C <sub>m</sub>	Tb	Т	Cm	dT	Т	Cm	dT	T
1.132	0.030	2.299	0.919	0.037	2.606	0.644	0.079	3.149
1.060	0.032	2.330	0.811	0.063	2.655	0.587	0.086	3.224
1.086	0.031	2.356	0.845	0.060	2.716	0.701	0.072	3.302
1.005	0.034	2.388	0.776	0.065	2.766	0.809	0.063	3.369
1.039	0.033	2.421	0.768	0.066	2.831	0.581	0.087	3.444
0.912	0.037	2.456	0.743	0.068	2.898	0.564	0.090	3.533
0.945	0.036	2.492	0.747	0.068	2.966	0.485	0.104	3.624
0.857	0.039	2.530	0.731	0.069	3.029	0.535	0.095	3.724
0.890	0.038	2.568	0.737	0.069	3.098			
<u>Table 18</u>. The Specific Heat of  $Cs_2MnCl_4 \cdot 2H_2O$  for Sample 1, Run 17, March 3, 1967, 8400 Gauss, Orientation C.

C <sub>m</sub>	ат	Т	C <sub>m</sub>	ТБ	Т	C <sub>m</sub>	ТБ	Т
4.093	0.012	1.263	5.651	0.009	1.464	1.818	0.019	1.637
4.215	0.012	1.274	5.759	0.013	1.484	1.889	0.018	1.657
3.680	0.014	1.295	6.132	0.012	1.500	1.743	0.029	1.689
3.585	0.014	1.311	8.489	0.009	1.511	1.639	0.025	1.727
4.018	0.013	1.324	9.995	0.008	1.519	1.436	0.035	1.782
4.030	0.013	1.336	11.924	0.006	1.526	1.371	0.037	1.835
4.245	0.012	1.348	11.822	0.006	1.533	1.285	0.039	1.921
4.112	0.012	1.360	10.298	0.007	1.540	1.136	0.044	2.010
4.023	0.013	1.369	10.118	0.008	1.547	1.077	0.047	2.076
4.394	0.011	1.380	8.391	0.009	1.555	0.982	0.051	2.165
4.657	0.011	1.390	6.444	0.012	1.566	0.949	0.036	2.238
4.737	0.011	1.400	3.407	0.015	1.578	0.810	0.042	2.427
4.717	0.011	1.410	2.605	0.019	1.593	0.800	0.042	2.533
4.697	0.011	1.419	2.234	0.015	1.608	0.808	0.063	2.625
5.313	0.009	1.436	2.042	0.017	1.621			

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C <sub>m</sub>	dT	T	Cm	dT	Т	Cm	dT	Т
3.421	0.015	1.302	5.335	0.009	1.602	1.376	0.037	2.040
3.197	0.016	1.315	5.253	0.010	1.612	1.260	0.040	2.079
3.159	0.016	1.329	5.771	0.009	1.621	1.317	0.038	2.118
3.077	0.016	1.343	6.525	0.008	1.639	1.264	0.040	2.160
3.119	0.016	1.357	6.168	0.008	1.647	1.144	0.044	2.202
3.207	0.016	1.387	6.760	0.007	1.655	1.156	0.044	2.246
3.208	0.016	1.402	6.923	0.007	1.662	1.134	0.045	2.287
3.477	0.015	1.418	6.988	0.007	1.669	1.050	0.048	2.361
3.625	0.014	1.432	7.591	0.010	1.678	0.844	0.060	2.538
3.679	0.014	1.446	8.182	0.009	1.688	0.794	0.064	2.658
3.971	0.013	1.457	8.455	0.009	1.697	0.796	0.064	2.742
4.101	0.012	1.470	4.596	0.017	1.709	0.703	0.072	2.828
4.230	0.012	1.482	2.527	0.020	1.725	0.642	0.079	2.939
4.467	0.011	1.494	2.476	0.020	1.743	0.612	0.083	3.064
4.345	0.012	1.505	2.248	0.023	1.762	0.604	0.084	3.186
4.167	0.012	1.516	2.067	0.025	1.783	0.553	0.092	3.314
4.513	0.011	1.526	1.904	0.027	1.806	0.527	0.096	3.425
4.323	0.012	1.562	1.735	0.029	1.828	0.528	0.096	3.539
5.004	0.010	1.573	1.663	0.030	1.881	0.471	0.108	3.689
4.940	0.010	1.583	1.491	0.034	1.942	0.514	0.098	3.827
5.374	0.009	1.593	1.507	0.034	1.989	0.412	0.123	3.979

<u>Table 19</u>. The Specific Heat of  $Cs_2MnCl_4 \cdot 2H_2O$  for Sample 1, Run 18, March 8, 1967, 6050 Gauss, Orientation C.

<u>Table 20</u>. The Specific Heat of  $Cs_2MnCl_4 \cdot 2H_2O$  for Sample 1, Run 19, March 10, 1967, 9830 Gauss, Orientation C.

Cm	dT	Т	Cm	dT	Т	Cm	dT	Т
4.279	0.012	1.314	1.638	0.021	1.536	0.806	0.042	2.348
4.441	0.011	1.335	1.532	0.022	1.561	0.850	0.040	2.438
4.557	0.011	1.345	1.422	0.024	1.587	0.795	0.042	2.540
4.673	0.011	1.355	1.351	0.025	1.611	0.759	0.044	2.617
4.789	0.011	1.365	1.394	0.024	1.636	0.746	0.045	2.677
4.941	0.010	1.374	1.352	0.025	1.659	0.748	0.045	2.743
5.225	0.010	1.382	1.274	0.027	1.682	0.677	0.050	2.791
5.967	0.008	1.399	1.280	0.026	1.702	0.715	0.047	2.821
6.863	0.007	1.405	1.266	0.027	1.725	0.703	0.072	2.890
7.214	0.007	1.413	1.162	0.029	1.750	0.590	0.086	3.008
7.800	0,006	1.419	1.233	0.027	1.775	0.595	0.085	3.130
8.593	0.006	1.426	1.250	0.027	1.872	0.601	0.084	3.250
9.230	0.005	1.431	1.102	0.031	1.916	0.598	0.085	3.406
10.123	0.005	1.437	1.039	0.033	1.954	0.545	0.093	3.523
10.010	0.005	1.440	1.030	0.033	1.986	0.508	0.099	3.644
14.591	0.003	1.444	1.066	0.032	2.012	0.501	0.101	3.744
6.324	0.008	1.442	0.993	0.034	2.045	0.513	0.099	3.876
4.500	0.011	1.450	0.982	0.034	2.073	0.568	0.089	3.977
3.402	0.015	1.462	0.970	0.035	2.100	0.568	0.089	4.057
2.115	0.016	1.476	1.074	0.031	2.148	0.521	0.097	4.089
1.972	0.017	1.509	0.982	0.034	2.202			

	Table	<u>21</u> . Th	e Specif	ic Heat of (	$Cs_2^{MnC1}4 \cdot 2H_2^{O}$	for Sample
1,	Run 20,	March 1	4, 1967,	6050 Gauss	, Orientation	С.

C <sub>m</sub>	dT	Ť.	Cm	Tb	Т	Cm	dT	Т
3.201	0.016	1.308	5.019	0.010	1.568	3.467	0.012	1.714
3.370	0.015	1.321	5.233	0.010	1.578	2.810	0.012	1.726
3.249	0.016	1.334	4.890	0.010	1.588	2.590	0.012	1.738
3.193	0.016	1.347	4.583	0.011	1.599	2.368	0.012	1.750
3.117	0.016	1.360	6.201	0.008	1.608	2.294	0.015	1.762
3.346	0.015	1.378	6.039	0.008	1.616	1.808	0.019	1.777
3.427	0.015	1.393	5.629	0.009	1.625	1.997	0.017	1.794
3.398	0.015	1.407	6.645	0.008	1.633	1.922	0.018	1.810
3.406	0.015	1.420	6.009	0.008	1.642	1.772	0.019	1.825
3.488	0.015	1.432	6.285	0.008	1.650	1.759	0.019	1.833
3.942	0.013	1.476	5.653	0.009	1.657	1.655	0.020	1.851
3.924	0.013	1.493	6.704	0.008	1.664	1.572	0.021	1.870
4.018	0.013	1.507	6.427	0.008	1.671	1.607	0.021	1.891
4.029	0.013	1.524	9.584	0.005	1.685	1.581	0.021	1.911
4.456	0.011	1.536	8.727	0.006	1.690	1.546	0.022	1.932
4.819	0.011	1.547	8.307	0.006	1.696	1.470	0.023	1.953
4.490	0.011	1.557	5.449	0.009	1.704	1.458	0.023	1.960

Table 21 (Continued)

Cm	dт	Т	Cm	dT	Т	Cm	dT	Т
1.449	0.023	1.981	1.025	0.049	2.330	0.579	0.087	3.341
1.457	0.023	2.002	0.941	0.054	2.449	0.585	0.087	3.428
1.353	0.025	2.024	0.883	0.057	2.542	0.583	0.087	3.514
1.347	0.025	2.005	0.802	0.063	2.669	0.529	0.096	3.639
1.432	0.024	2.040	0.793	0.064	2.770	0.502	0.101	3.771
1.369	0.025	2.099	0.692	0.073	2.922	0.461	0.110	3.894
1.295	0.026	2.141	0.659	0.077	3.022	0.511	0.099	3.998
1.226	0.028	2.180	0.616	0.082	3.114	0.561	0.090	4.079
1.094	0.046	2.252	0.608	0.083	3.244			

Cm	dT	Т	Cm	dT	Т	Cm	dT	Т
3.835	0.013	1.318	13.579	0.004	1.494	1.083	0.031	2.039
4.144	0.012	1.331	7.342	0.007	1.502	1.064	0.032	2.070
4.422	0.011	1.341	6.827	0.007	1.508	1.106	0.030	2.101
4.100	0.012	1.352	4.828	0.010	1.515	1.076	0.031	2.128
4.374	0.012	1.363	3.986	0.013	1.525	1.050	0.032	2.164
4.367	0.012	1.373	2.800	0.012	1.536	1.106	0.030	2.205
4.428	0.011	1.383	2.490	0.014	1.539	0.987	0.034	2.251
4.755	0.011	1.393	2.074	0.016	1.558	0.922	0.037	2.321
4.901	0.010	1.402	1.856	0.018	1.575	0.969	0.035	2.388
5.764	0.009	1.412	1.827	0.018	1.593	0.865	0.039	2.515
5.219	0.010	1.421	1.712	0.020	1.612	0.751	0.045	2.673
5.654	0.009	1.428	1.718	0.020	1.631	0.738	0.046	2.761
5.969	0.008	1.437	1.528	0.022	1.651	0.681	0.050	2.907
6.372	0.008	1.444	1.445	0.023	1.690	0.670	0.050	3.011
6.592	0.008	1.452	1.407	0.024	1.721	0.652	0.052	3.102
7.636	0.007	1.459	1.375	0.025	1.766	0.626	0.081	3.236
8.269	0.006	1.466	1.389	0.024	1.824	0.655	0.077	3.346
8.774	0.006	1.472	1.422	0.024	1.868	0.595	0.085	3.482
10.751	0.005	1.479	1.197	0.028	1.922	0.501	0.101	3.680
11.812	0.004	1.483	1.219	0.028	1.962	0.496	0.102	3.828
14.589	0.003	1.487	1.155	0.029	1.998	0.409	0.124	3.978
10.271	0.005	1.491						

<u>Table 23</u>. The Specific Heat of  $Cs_2MnCl_4 \cdot 2H_2O$  for Sample 1, Run 22, April 5, 1967, 9830 Gauss, Orientation C.

C <sub>m</sub>	Τb	Т	Cm	dT	T	C <sub>m</sub>	dT	Т
3.429	0.015	1.271	6.781	0.007	1.415	1.048	0.032	2.084
3.850	0.013	1.284	4.430	0.011	1.422	1.011	0.033	2.128
3.865	0.013	1.296	3.104	0.016	1.434	0.962	0.035	2.185
3.880	0.013	1.308	2.028	0.025	1.452	0.916	0.037	2.245
3.922	0.013	1.319	1.768	0.019	1.498	0.921	0.037	2.294
3.965	0.013	1.330	1.615	0.021	1.526	0.882	0.038	2.346
3.656	0.014	1.340	1.508	0.022	1.553	0.859	0.039	2.407
3.757	0.013	1.350	1.420	0.024	1.580	0.819	0.041	2.457
4.560	0.011	1.360	1.401	0.024	1.603	0.819	0.041	2.501
4.758	0.011	1.369	1.336	0.025	1.627	0.747	0.045	2.546
5.220	0.010	1.377	1.290	0.026	1.651	0.774	0.044	2.627
5.400	0.009	1.385	1.253	0.027	1.673	0.739	0.069	2.709
5.771	0.009	1.392	1.304	0.026	1.697	0.738	0,069	2.795
6.818	0.007	1.399	1.259	0.027	1.720	0.676	0.075	2.886
6.801	0.007	1.405	1.223	0.028	1.807	0.570	0.089	2.971
7.876	0.006	1.411	1,155	0.029	1.865	0.570	0.089	3.092
7.969	0.006	1.409	1.253	0.027	1.904	0.567	0.089	3.316
9.274	0.005	1.414	1.135	0.030	1.950	0.563	0.090	3.646
13.220	0.004	1.418	1.069	0.032	1.995	0.464	0.109	3.953
13.474	0.004	1.426	0.976	0.035	2.038	0.511	0.099	4.171

133

<u>Table 24</u>. The Specific Heat of  $Cs_2MnCl_4 \cdot 2H_2O$  for Sample 1, Run 23, April 5, 1967, 3500 Gauss, Orientation C.

C <sub>m</sub>	dT	Т	C <sub>m</sub>	Tb	Т	C <sub>m</sub>	Τb	Т
2.703	0.019	1.290	4.453	0.011	1.623	2.358	0.021	1.859
2.688	0.019	1.306	4.706	0.011	1.634	2.087	0.024	1.914
2.458	0.021	1.323	4.674	0.011	1.645	1.658	0.032	1.954
2.493	0.020	1.339	5.156	0.010	1.656	1.657	0.031	1.985
2.607	0.019	1.355	5.460	0.009	1.665	1.505	0.034	2.071
2.671	0.019	1.374	4.949	0.010	1.675	1.410	0.037	2.130
3.227	0.016	1.391	5.327	0.010	1.682	1.238	0.042	2.199
2.777	0.018	1.406	5.701	0.009	1.692	1.171	0.045	2.246
2.801	0.018	1.421	5.563	0.009	1.701	1.202	0.044	2.291
3.127	0.016	1.444	5.195	0.010	1.708	1.181	0.043	2.336
3.381	0.015	1.459	6.342	0.008	1.717	1.111	0.047	2.381
3.583	0.014	1.474	5.954	0.009	1.725	1.103	0.047	2.449
3.716	0.014	1.488	6.167	0.008	1.731	0.877	0.058	2.553
3.743	0.014	1.501	6.800	0.007	1.739	0.855	0.059	2.647
3.250	0.016	1.516	7.690	0.007	1.746	0.742	0.068	2.779
3.575	0.014	1.526	7.879	0.006	1.753	0.754	0.067	2.887
3.702	0.014	1.539	8.583	0.006	1.765	0.681	0.074	3.029
3.713	0.014	1.552	9.158	0.006	1.770	0.613	0.083	3.149
3.917	0.013	1.561	9.596	0.005	1.776	0.672	0.075	3.298
3.829	0.013	1.573	8.553	0.006	1.781	0.544	0.093	3.437
4.011	0.013	1.583	5.301	0.010	1.788	0.507	0.100	3.586
3.946	0.013	1.594	4.136	0.012	1.798	0.449	0.113	3.800
3.829	0.013	1.605	2.813	0.018	1.813	0.434	0.117	3.986
4.716	0.011	1.612	2.450	0.021	1.830	0.420	0.121	4.171

	Table	25.	The	Specif	ic He	eat of	$Cs_2^{MnC1}4 \cdot {}^{2H}2^{C}$	) for	Sample
1,	Run 24,	Apri1	5,	1967,	8900	Gauss,	Orientation	C.	

Cm	dT	Т	Cm	Tb	Т	Cm	Tb	T
3.381	0.015	1.266	6.995	0.007	1.514	1.063	0.033	2.024
3.449	0.015	1.279	5.112	0.010	1.522	1.136	0.031	2.074
3.501	0.015	1.293	3.324	0.016	1.535	1.119	0.032	2.119
3.491	0.015	1.305	2.170	0.024	1,555	1.097	0.032	2.178
3.525	0.015	1.318	1.779	0.020	1.576	1.045	0.034	2.224
3.497	0.015	1.331	1.780	0.020	1.596	0.941	0.038	2.310
3.859	0.014	1.343	1.682	0.021	1.615	0.856	0.041	2.376
3.787	0.014	1.356	1.573	0.023	1.635	0.882	0.040	2.472
3.913	0.013	1.368	1.529	0.023	1.655	0.832	0.043	2.546
4.091	0.013	1.378	1.516	0.023	1.677	0.809	0.044	2.654
4.203	0.012	1.389	1.444	0.025	1.699	0.754	0.047	2.735
4.126	0.013	1.428	1.398	0.025	1.721	0.766	0.046	2.851
4.796	0.011	1.440	1.458	0.024	1.741	0.720	0.049	2.933
5.246	0.010	1.450	1.311	0.027	1.763	0.645	0.055	3.000
6.005	0.009	1.460	1.310	0.027	1.787	0.619	0.057	3.094
6.089	0.009	1.468	1.259	0.028	1.811	0.750	0.047	3.196
6.985	0.007	1.476	1.372	0.026	1.853	0.603	0.059	3.320
8.141	0.006	1.483	1.366	0.026	1.894	0.532	0.098	3.468
9.105	0.006	1.489	1.157	0.031	1.940	0.571	0.092	3.608
9.629	0.005	1.495	1.195	0.030	1.970	0.494	0.106	3.751
11.642	0.004	1.498	1.154	0.031	1.997	0.507	0.103	3.851
13.337	0.004	1.508						

Cm	dT	Т	Cm	dT	Т	Cm	dT	Т
2.713	0.019	1.309	5.155	0.010	1.660	1.966	0.026	1.878
2.620	0.019	1.326	5.667	0.009	1.670	1.991	0.025	1.905
2.661	0.019	1.342	5.091	0.010	1.679	1.794	0.028	1.964
2.625	0.019	1.358	6.253	0.008	1.688	1.616	0.031	2.024
2.736	0.018	1.374	5.765	0.009	1.697	1.439	0.035	2.098
2.878	0.018	1.392	6.367	0.008	1.705	1.411	0.036	2.150
3.025	0.017	1.409	5.867	0.009	1.713	1.217	0.042	2.231
3.036	0.017	1.426	7.531	0.007	1.721	1.125	0.045	2.300
3.511	0.014	1.481	6.377	0.008	1.727	1.018	0.050	2.401
3.097	0.016	1.502	7.101	0.007	1.735	0.968	0.052	2.513
3.153	0.016	1.518	7.278	0.007	1.742	0.866	0.058	2.640
3.706	0.014	1.534	6.515	0.008	1.749	0.830	0.061	2.743
3.575	0.014	1.548	6.378	0.008	1.756	0.717	0.071	2.883
3.851	0.013	1.562	6.596	0.008	1.762	0.771	0.066	2.983
4.050	0.012	1.575	8.035	0.006	1.768	0.639	0.079	3.128
4.618	0.011	1.586	7.365	0.007	1.774	0.599	0.084	3.266
3.580	0.014	1.599	8.273	0.006	1.779	0.549	0.092	3.470
4.597	0.011	1.611	5.239	0.010	1.786	0.544	0.093	3.623
4.518	0.011	1.621	3.222	0.016	1.797	0.699	0.072	3.722
4.756	0.011	1.630	2.746	0.018	1.812	0.487	0.104	3.821
4.870	0.010	1.641	2.321	0.022	1.832	0.479	0.106	3.904
4.722	0.011	1.651	2.315	0.022	1.854			

<u>Table 27</u>. The Temperature Changes from an Adiabatic Magnetization Experiment on Sample 1, Orientation C, April 21, 1967.

T(0)	T(3500)	T(6050)	T(8400)	T(8900)
1.282	1.244	1.196	1.161	1.154
1.311	1.256	1.202	1.164	1.156
1.298	1.263	1.209	1.166	1.156
1.514	1.471	1.402	1.345	1.330
1.519	1.474	1.406	1.346	1.331
1.516	1.473	1.402	1.345	1.330
1.519	1.477	1.405	1.345	1.330
1.607	1.565	1.485	1.412	1.393
1.607	1.566	1.488	1.413	1.393
1.607	1.561	1.486	1.412	1.392
1.607	1.565	1.489	1.412	1.392
1.729	1.685	1.601	1.485	1.449
1.728	1.687	1.602	1.486	1.449
1.727	1.671	1.602	1.485	1.447
1.726	1.671	1.603	1.485	1.447
1.798	1.757	1.672	1.573	1.550
1.798	1.756	1.669	1.572	1.550

T(0)	T(3500)	T(6050)	T(8400)	T(8900)	
1 857	1 8 7 7	1 702	1 755	1 7/7	
1.057	1.033	1./92	1./33	1./4/	
1.852	1.828	1.788	1.753	1.747	
1.903	1.884	1.853	1.830	1.827	
1.894	1.877	1.848	1.828	1.827	
1.920	1.902	1.873	1.855	1.853	
1.913	1.896	1.870	1.853	1.853	
2.068	2.063	2.061	2.076	2.086	
2,066	2.059	2.058	2.074	2.086	
2.165	2.165	2.176	2.208	2.221	
2.156	2.157	2.168	2.203	2.221	
2.432	2.449	2.490	2.570	2.595	
2.417	2.434	2.478	2 560	2 595	
2.117		2.470	2.000		
3.028	3.081	3.182	3.313	3.333	
2 960	2 003	3 0 9 3	3 255	7 777	
2.900	2.995	5.085	5.255	3.333	
3 322	3 386	3 5 3 1	3 717	3 762	
	5.000	J.JJI	5.111	5.702	
3.224	3.284	3.424	3.660	3.762	

