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#### ABSTRACT

# MECHANICAL PROPERTIES OF SAND-ICE MATERIALS

Ву

#### Bernard D. Alkire

Experimental shear strength and creep data obtained for confining pressures up to 1000 psi are presented for sand-ice materials. To investigate factors that affect the strength of the material, constant axial strain rate tests were conducted on samples with various void ratios, strain rates, and ice contents. Uniaxial, confined and step-stress creep tests were conducted to determine the effect of confining pressure on sand-ice materials and to develop an expression that would be descriptive of the creep behavior for confining pressures up to 1000 psi.

The granular part of the samples consisted of Ottawa sand sized between the number 20 (0.84mm) and 30 (0.59mm) U. S. Standard sieve sizes. The ice was prepared from deaired, deionized and distilled water with sample ice contents ranging from 33 to 100 percent of the sand void volume. Samples prepared in a split aluminum mold were 1.13 inches in diameter by 2.26 inches in height. All tests were conducted in a high pressure

triaxial cell with temperature controlled by submersion in a low-temperature bath maintained very close to -12.0° C.

The constant strain rate tests showed that high confining pressure causes a distinctive stress-strain curve. This curve has an initial linear portion, up to approximately two percent strain, followed by a near linear increase in stress up to failure of the sample. Strains at failure increased with confining pressure and were six to seven percent for samples tested with 700 psi confining pressure.

Results from the constant axial strain rate tests are presented in terms of the Mohr-Coulomb theory where the factors that affect the frictional and cohesive components of strength are identified. It is shown that the cohesive component of strength is due to the response of the ice matrix to test conditions. The cohesion is dependent on strain rate and ice content for constant temperature. The frictional component is shown to be dependent on the void ratio and the confining pressure. It is shown that the frictional behavior of the sand-ice material is very similar to the frictional characteristics of unfrozen sand tested at high confining pressure.

Uniaxial creep tests conducted at various levels of constant axial stress were used to obtain the general creep behavior of the sand-ice materials. With these

tests as a basis for comparison, the effects of confining pressure were determined from step-stress and confined triaxial creep tests. The results show that increases in the confining pressure reduce the strain rate. An expression for calculating the strain rate as a function of deviator stress and confining pressure was developed. This expression indicates that creep decreases exponentially with increasing confining pressure. Confining pressure below 200 psi has the greatest effect on the strain rate, and two regions of definition are necessary to totally describe the effects of confining pressures up to 1000 psi.

Results from the creep tests with reduced ice content samples are used to show the influence of relative ice content by a term called the percent of maximum deviator stress. The term, regardless of ice content, is defined as the applied creep deviator stress divided by a peak deviator stress. The peak deviator stress is obtained from a constant axial strain rate test conducted at a confining pressure equal to the confining pressure used in the creep test. All creep tests performed at the same percent of maximum deviator stress produced the same strain rates. Using this fact the equation developed for high ice content samples may be used for the reduced ice content if the deviator stress is modified to include the effect of ice content.

## MECHANICAL PROPERTIES OF

SAND-ICE MATERIALS

Ву

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#### NOTATIONS

 $A_{HT}$  = Area of ice, high ice content

A<sub>HC</sub> = Area of sand, high ice content

 $A_{T,T}$  = Area of ice, low ice content

 $A_{T,S}$  = Area of sand, low ice content

c = Cohesion

D =  $\sigma_1 - \sigma_3$  = Axial stress difference = Deviator stress

D<sub>a</sub> = Dilatancy component

 $D_r$  = Relative density

E = Modulus of elasticity

e = Void ratio

f = Shear force acting on a flow unit

 $\Delta F$  = Free energy of activation, calories per mole

 $\Delta F_{O}$  = Activation energy required to overcome cohesion

g = Particle gradation

h = Planck's constant =  $6.624 \times 10^{-27} \text{erg-sec}^{-1}$ 

H = Mineral type

I = Interparticle forces

j = Ice content

K = Slope factor

K<sub>f</sub> = Frictional constant

 $k = Boltzmann's constant = 1.38 \times 10^{-16} erg {}^{\circ}K^{-1}$ 

M = Percent of maximum deviator stress

m, b, C, A, N, G = creep parameters

n = Exponent in creep equation

 $N_C$  = Flow value =  $\frac{1 + \sin \phi}{1 - \sin \phi}$ 

 $p = (\sigma_1 + \sigma_3)/2$ 

P = Particle shape

P<sub>H</sub> = Force causing shear, high ice content

 $P_r$  = Force causing shear, low ice content

 $q = (\sigma_1 - \sigma_3)/2$ 

R = Universal gas constant = 1.98 calories  $^{\circ}K^{-1}$  mole  $^{-1}$ 

t = Time

T = Temperature

v = Frequency of activation, sec<sup>-1</sup>

X = Parameter, a function of the number of flow units

 $\varepsilon$  = True axial strain, in/in

 $\dot{\varepsilon}$  = True axial strain rate, min<sup>-1</sup>

 $\dot{\epsilon}_{C}$  = Arbitrary strain rate in creep

 $\lambda$  = Distance between equilibrium positions of flow units

 $\Sigma$  = Stress factor = D- $\sigma_m$ 

σ = Uniaxial stress

 $\sigma_c$  = Proof stress in creep equation

 $\sigma_{m}$  = Mean normal stress

 $\tau$  = Shear stress

 $\tau_{\rm H}$  = Shear stress, high ice content

 $\tau_{\text{T.}}$  = Shear stress, low ice content

 $\phi$  = Angle of internal friction

 $\sigma_1$  = Major principle stress

 $\sigma_3$  = Minor principle stress = confining pressure

#### CHAPTER I

#### INTRODUCTION

The mechanical properties of sand-ice are studied to determine the strength and creep behavior of the material. Originally the strength of frozen soils was determined as for an undrained clay, with strength being stated in terms of cohesion (Vialov, 1965a). As more elaborate testing equipment became available, and strength was determined to be time dependent (Tystovich, 1960), creep testing was used to study the nature of this time dependency and its relationship to strength. Presently, many testing techniques are used to study the mechanical properties of frozen soils. Tension tests (Vialov, 1965b), shear tests (Vialov, 1965b), uniaxial compression tests (Goughnour and Andersland, 1968), confined compression (Andersland and AlNouri, 1970) and constant axial stress tests (Andersland and AlNouri, 1970; Sayles, 1968) have been conducted on frozen soils. These tests have resulted in various empirical formulations that describe the time dependent mechanical properties of frozen soils.

One of the most common methods used to describe the strength of frozen soil is the Mohr-Coulomb failure

theory. This theory has been used by Vialov (1965b);

Tystovich (1960); and Andersland and AlNouri (1970) to

describe the time dependent behavior of sand-ice materials.

The basic problem in this approach to shear strength is

determining the interrelationship of the cohesive and

frictional components of strength for given test conditions.

Assuming that the Mohr-Coulomb theory is valid for frozen soils, a portion of this study is concerned with identifying factors that affect the frictional and cohesive components of strength. The basic factors that influence strength of sand-ice materials include temperature, strain rate, ice content and the percent of sand in the system. These factors have been discussed by other investigators of sand-ice materials (Vialov, 1965b; Kaplar, 1971; Goughnour and Andersland, 1968). However, the effect of these factors when the sand-ice is subjected to high confining pressures is not known. One of the main objectives of this study is to use the results of tests conducted at high confining pressures as a means of identifying frictional and cohesive components of strength. By using triaxial testing techniques and confining pressures up to 1000 psi, the effects of strain rate, ice content and void ratio on the strength of sand-ice are determined. In order to eliminate the effect of

temperature on the results, all constant strain rate tests were conducted at a temperature of -12.0° C.

From the results of the experimental portion, the Mohr-Coulomb theory is applied for the entire range of confining pressures and an effective angle of friction is determined. It is shown that the angle of friction is independent of ice content and is related to the angle of friction for unfrozen sands tested at high confining pressures.

The second part of this study describes the effect of confining pressure on the creep of sand-ice materials. Andersland and AlNouri (1970) have indicated that the steady state creep rate can be estimated using the rate process theory. For confining pressures up to 150 psi, the steady state creep was determined to be a function of deviator stress and the mean stress. In order to verify this result and to extend the range of mean stresses used, creep tests were conducted at confining pressures up to 1000 psi. From the results of these tests an expression for creep in terms of deviator stress and confining pressure is developed for the entire range of confining pressures.

A problem in determining the time dependent behavior of sand-ice is the identification of the active component of creep. By using samples with reduced ice content, it can be shown that the ice matrix is the primary agent of creep. Further, it is noted that there is a relationship between the peak deviator stress as determined in a constant strain rate test, and the creep behavior of a sand-ice sample tested at a deviator stress less than the peak value.

Constant deviator stress testing was used to obtain the creep behavior of the sand-ice material. The effect of confining pressure was obtained using step-stress testing techniques where the deviator stress is held constant and the confining pressure is increased in steps as the tests progress. These tests covered a range of confining pressures from 0 to 1000 psi. Uniaxial creep tests were conducted to obtain the general creep characteristics of the material and to verify the effect of confining pressure on creep. Reduced ice content samples were also tested using uniaxial and step-stress techniques.

#### CHAPTER II

#### LITERATURE REVIEW

### 2.1 Frozen Soil Structure

In order to understand the shear strength and creep characteristics of a sand-ice material, it is useful to describe the various components that make up the system. Frozen soils, in general, can be considered to be multi-phase systems made up of an assemblage of soil particles, unfrozen pore water, polycrystalline ice and entrapped air. The relative proportions of each of these components will have substantial effects on the mechanical behavior of the material. Some of the phases are interrelated, such as the amount of unfrozen pore water and the type of soil particles. Others are directly affected by ambient conditions and testing techniques. Overall, the picture obtained is a complicated system responsive to numerous changes in conditions. The discussion to follow will emphasize sand-ice materials, but other types of frozen soil will be included to give a better idea of the available theories used to determine the strength characteristics of sand-ice materials.

Vialov (1965b), Scott (1969) and Tsytovich (1960) have shown that variations in mechanical properties of frozen soils can be related to the amount of unfrozen pore water in the soil-ice system. There are two phases of unfrozen water in frozen soil: water vapor having a variable composition, and water that is strongly attracted to the soil particles by intermolecular forces.

Water vapor is a gaseous phase found in the void spaces. At temperatures below freezing its properties remain the same until frozen. Water vapor has been found in polar ice at temperatures as low as -40.0°C (Tsytovich, 1960). Water vapor transport may contribute substantially to the formation of ice lenses in soil systems where the freezing front is isolated from the source of the water. In this process, moisture is transported by vapor diffusion from the warmer source to the colder freezing front (Jumikis, 1966). For soils that were saturated before freezing this phenomenon does not occur.

The other type of unfrozen water that may be present in a frozen soil can be explained using the "diffuse double layer" concept. According to this theory the layer of water molecules closest to the soil particles are attracted to the surface molecules and have higher energy states and different characteristics than water which is located at some distance from the particle surface. The

amount of water in the bound layer that will freeze is dependent upon the interaction of the forces of crystallization and the forces of attraction to the particle surface. The forces of attraction are dependent on the mineralogical composition of the particles and will be influenced by the specific surface of the particles while the forces of ice crystallization are dependent to a large degree on the temperature. For any given temperature, the larger the specific surface area of the mineral, the larger the amount of unfrozen water. Tsytovich (1960) showed that unfrozen water was present in clays even at temperatures below -30.0° C. Anderson (1967) verifies this fact and states,

It seems beyond a doubt that in frozen silicate mineralwater systems, the ice crystals are separated from the substrate surface by an unfrozen fluid-like interfacial zone of water.

Some of the differences in behavior between frozen sands and clays can be explained when it is known that the sands with their round large sized particles have low specific area as compared to clay particles. Because sands have low specific surface, and unfrozen water contents are directly related to these surface areas, nearly all available water in sand is frozen at temperatures slightly below  $0.0^{\circ}$  C (Scott, 1969).

# 2.2 Freezing Process

Since all frozen soils are at some time unfrozen, it is necessary to understand the mechanism of freezing.

Basically, freezing is a thermodynamic process. By sufficiently lowering the temperature, molecules in a higher state of energy--the liquid state--change to molecules in a lower state of energy--the solid state. It is possible (Scott, 1969) to visualize the liquid state as consisting of aggregates of liquid molecules, which for a given temperature will have an equilibrium size that is determined by the ambient conditions. From quantum mechanics it is known that other aggregates of molecules will exist that are both larger and smaller than the equilibrium size. The larger aggregates will grow to form 'nuclei' of solidification. The formation of ice crystals depends upon the existence of these nuclei in the water as distinct starting points for crystallization of ice (Jumikis, 1966). The actual temperature at which crystallization will take place is a function of the grain size.

When a soil freezes, the soil structure may be considerably altered by the formation of ice lenses. In addition, the soil may be consolidated by the development of negative pore pressures developed below or adjacent to the ice/water interface. The degree of this alteration depends primarily on the mineralogical composition of the soil, grain size, freezing history and saturation. For large grained sand or gravel the soil structure is unaltered

(Vialov, 1965b) as freezing occurs with void spaces being filled with randomly oriented crystals of ice.

It was noted that the unfrozen water may have two different phases: water vapor and water attached to or adsorbed on the soil particles. For sand-ice materials these types of water are not present in any great amount. At temperatures slightly below 0°C all water freezes directly in the pore spaces forming a massive structure (Vialov, 1965b) with little sensitivity to freezing history (Scott, 1969; Sayles, 1968).

Another factor in the freezing of a soil is the change in volume of water as freezing takes place. This factor may have considerable importance in the laboratory if samples of constant void ratio are to be prepared. The amount of soil volume increase (frost heave) is dependent upon the amount of water available and the grain size of the material. When water freezes there is an increase in volume of approximately nine percent. The change in volume may or may not affect the soil structure depending on the drainage conditions. Tsytovich (1960), states that under the conditions of free drainage, no changes in soil volume for sand will occur because the excess water resulting from freezing will be squeezed out. This will not be the case for fine grained soils since their low permeability will inhibit drainage of the excess

water resulting in expansion of the soil system as volume change occurs during freezing.

## 2.3 Cohesion

Unfrozen sand has no unconfined shear strength. When sand is saturated and frozen, there will be a substantial unconfined strength. The increase in strength due to the confinement of the ice matrix is called cohesion. In general, cohesion may result from three causes (Vialov, 1965b): (1) intermolecular cohesion due to forces of attraction between particles, (2) structural cohesion resulting from the process of formation and (3) cohesion due to confinement of the ice matrix (ice cementation). Depending on the type of soil, any or all of these components may be present. For sand-ice materials it is reasonable to assume that the first two components of cohesion are negligible and consider only the cohesion due to confinement of the ice matrix.

Cohesion due to the ice matrix is very responsive to temperature change and is a function of time, moisture content, plastic strain, load, and strain energy. One theory used to explain cohesion is based on variations and movement of unfrozen water in the soil-ice structure (Scott, 1969; Vialov, 1965a; Tsytovich, 1960). This theory states that upon application of some stress, high pressures are caused near the points of contact of the grains, resulting

in the melting of the ice in these regions. The melted ice flows to zones of lower stress where it refreezes.

On the macro-scale this may be considered a weakening process followed by a strengthening process. Goughnour (1967), used this basic idea to explain creep characteristics of ice and identified the weakening and strengthening mechanisms.

Vialov (1965a), using rigid ball penetration test techniques, has obtained extensive data for the cohesion of frozen soils. His basic observations are: (1) sandy soils have small rheological response compared to clays; (2) cohesive properties increase up to some maximum as ice content increases; (3) temperature changes are one of the main causes of variations in the cohesive component in frozen soils; and (4) long term cohesion may be significantly less than the instantaneous cohesion (three to nine times). Vialov's tests are the most extensive long term investigations available into the cohesive properties of soils. However, the resulting mathematical formulations may be in question due to the testing technique (Scott, 1969).

# 2.4 Mechanical Properties of Ice

The properties of the pore ice may affect the mechanical behavior of frozen soil. It is know that the direction of the applied loads in relation to the direction of the ice crystal's axis has a definite effect on the

mechanical behavior of the ice (Gold, 1963). However, it is generally assumed that when ice freezes in the pore spaces of a soil-ice material, a polycrystalline structure is formed and there exists no oriented planes of weakness (Goughnour, 1967). It is for this reason that the discussion of the mechanical properties of ice, as they affect sand-ice systems, is limited to polycrystalline ice.

In addition to the orientation of the crystals, the mechanical properties of ice are affected by a substantial number of variables. Among the most important of these are strain rate and temperature. Leonards and Andersland (1960) have shown that unconfined compressive strength increases approximately 15 psi per degree centigrade from 370 psi at -4° C. Their tests were conducted at a strain rate of  $2 \times 10^{-2} \text{min}^{-1}$ ; and results showed considerable scatter due to the random nature of the freezing The strain rate also affects the strength of process. polycrystalline ice. Halbrook (1963) noted both an increase in Young's modulus and ultimate strength with an increase in rate of strain. However, Sanger (1971) in his review of available test results, indicates a decrease in strength of fresh water ice with an increase in strain rate.

Concerning the creep of polycrystalline ice, Gold (1963) noted that slip takes place only along basal planes and the deformation mechanism must be described in ways

which ice grains respond to this constraint. Gold (1963) has identified seven mechanisms which may take part in the response to applied loads. In the central part of the ice grains, slip bands and kink bands develop to conform to imposed deformations. However, for the grain boundary regions; boundary migration, crack formation, and distortion of the boundaries may take place as the grains respond to the applied loads. As a final response, recrystallization may take place, which is usually an indication of tertiary creep. The rate of loads application has a definite effect on which mechanisms predominate. For high loading rates, accommodation cracking and grain boundary migration are the controlling mechanisms.

# 2.5 Shearing Resistance

The shear resistance of sand-ice materials is dependent on a complex interaction of the ice matrix and the granular portion of the system. The Mohr-Coulomb theory is most frequently used to describe the shear strength of soils. It is a summation of the cohesive component and a frictional component. The cohesive component of frozen soils was discussed in section 2.3. The frictional component is best understood by examining the frictional characteristics of unfrozen sands.

# 2.5.1 Sand (Unfrozen)

In a sand-ice system it is apparent that for some conditions the frictional characteristics of the sand will contribute to the shear strength of the sand-ice material. The frictional properties of sands are well known and have been the subject of many articles. A good basic discussion of the many factors that affect the frictional behavior of single mineral sand was prepared by Koerner (1970). More important in relation to frozen sand is the frictional behavior of sand at high confining pressure. Several investigators have considered this problem (Hirschfeld and Poulous, 1963; Hall and Gordon, 1963; Vesic and Clough, 1968, Lee and Seed, 1967). The basic conclusions from their work that may be applied to sand-ice materials are:

- 1. Shearing resistance is made up of three components; sliding friction, dilatancy, and particle crushing and rearranging.
- 2. The dilatancy component of strength becomes small at high confining pressures.
- 3. The angle of friction decreases as confining pressure increases.
- 4. The strain at failure increases with increased confining pressure.
- 5. At high confining pressure sands exhibit a plastic stress-strain relationship.

# 2.5.2 Sand-Ice Materials

Shear strength of soil has traditionally been determined by the Coulomb equation which divides the shear strength into a frictional and cohesive component. The equation,

$$\tau = c + \sigma_n \tan \phi \tag{2-1}$$

may be used for soil-ice materials if the coefficients are adequately descriptive of the behavior of the frozen soil system. It is known that shear strength in frozen soils is time dependent (Vialov, 1965a) making it necessary to include the time factor in the defining equation.

Considering the Coulomb equation term by term, the frictional component may be expressed as:

$$\tau_f = \sigma_n \tan \phi = \sigma_n K_f$$

and (2-2)

$$K_f = f(\sigma_3, I, e, \hat{\epsilon}, P_s, g, H)$$

where  $\sigma_3$  = confining pressure

I = interparticle attractive or repulsive forces

e = void ratio

 $\varepsilon$  = strain rate

P<sub>s</sub> = particle shape

q = particle gradation

H = mineral type

It is usually assumed that the interparticle forces are insignificant for sand, and for a given type of sand the particle shape, gradation and mineral type can be held constant. Then for a given soil:

$$\tau_{f} = f(\sigma_{3}, e, \dot{e}) \tag{2-3}$$

The strain rate dependency is small for granular soils and for tests of short duration may be considered constant (Whitman, 1957). Thus, the functional relationship is usually interpreted as being related to initial void ratio and the applied confining pressure. Then,  $K_f = f(\sigma_3, e) = \tan \phi$  where  $\tan \phi$  may be defined at failure or at intermediate points along the stress path (Schmertmann and Osterberg, 1960).

The cohesive component in equation 2-1 representing a frozen soil is a function of three components (Vialov, 1965a). For sand-ice materials the interparticle and structural cohesion are negligible in magnitude and it is the confinement due to the ice matrix which controls cohesion. The component of shear strength contributed by the ice may be defined as:

$$c_i = f(\varepsilon, T, \dot{\varepsilon}, j, t)$$
 (2-4)

where  $\varepsilon = strain$ 

 $\dot{\varepsilon}$  = strain rate

T = temperature

j = ice content

t = time

The composite soil shear strength is:

$$\tau = c_i + \sigma_n K_f \tag{2-5}$$

Although the equation indicates a summation, it is possible that  $c_i$  and  $K_f$  do not reach their maximum at the same time. In fact, experimental evidence for clays (Schmertmann and Osterberg, 1960) indicates they do not. Further, if the cohesive component due to the ice is time dependent, eventually reducing to zero, then the shear strength will be a purely frictional phenomenon. It is doubtful that this is ever completely true; however, the contribution to shear strength due to the ice may approach a constant as this component is fully mobilized.

Other attempts have been made at defining the shear strength of frozen soils using the Mohr-Coulomb failure theory (Tsytovich, 1960; Vialov, 1965b). However, the fact that the strength of frozen soils is time dependent requires the modification of the usual form of equations to include the time factor. Tsytovich (1960) indicated that the shear strength of frozen soil is a function of at least three factors:

$$\tau = f(T, \sigma_3, t) \tag{2-6}$$

T = temperature of the soil below freezing

 $\sigma_3$  = confining pressure

t = time of action of the load

Thus, the shear strength for frozen soils can be determined by the equation

$$\tau = c_{T} + P \tan \phi_{T}$$
 (2-7)

where both  $c_T$  and  $\phi_T$  are functions of temperature and time. For a given time and stress the angle of friction increases as the temperature increases until at  $0^{\circ}$  C the value is equal to the value for unfrozen soils. The above relationship does not necessarily hold for all types of soils. Vialov (1965b) showed that the frictional component tan  $\phi_T$ , is not time dependent for frozen sands, sandy loams and dense clays. Other tests from the same study showed that for sands, the angle of friction at failure was constant for times to failure of 1 to 24 hours. The difference in the time factor, as it affects the friction term for various types of soil makes it very difficult to express the strength characteristics of clays and sands with one all inclusive equation.

Andersland and AlNouri (1970) have also used the Coulomb expression to evaluate the time dependent strength characteristics of frozen sands. They obtained a constant value of C and tan  $\phi$  when the factors affecting the cohesive component were held constant. In their study the

cohesion and angle of friction were determined from both constant strain rate and differential creep tests.

Another approach to the determination of the shear strength of sand-ice is to relate the strength of the sand-ice material to the strength of ice by a stress factor (Goughnour and Andersland, 1968). In this procedure the strength of a sand-ice material is obtained by multiplying the strength of ice at various strains by a stress factor. The stress factor is the ratio of sand-ice strength to the strength of ice obtained from samples tested at similar conditions. For this type of presentation it was noted that for strains less than approximately two percent, the stress factor is constant. Above this amount the stress factor is no longer constant, but increases in a linear manner up to a maximum value. After the peak strength of the sand-ice is reached the stress factor is again constant. Using the results from stress factor versus strain graphs, Goughnour (1967), identified the three stages of strengthening in a sand-ice system as follows:

> 1. The initial strengthening occurs at low values of strain where the characteristics of the ice predominate. In this stage the strength of sand-ice materials is a linear function of the strength of ice.

- The second stage occurs where solid to solid contact becomes apparent. This effect may be mobilized throughout deformation when the volume of sand is greater than 42 percent.
- 3. The third stage, related to dilatancy of the sand occurs as the particles act against the confinement of the ice matrix.

# 2.6 Creep Behavior

Since the strength of frozen soils has a strong time dependence, it is necessary to understand the rheologic behavior of the soil-ice system. One of the manifestations of the rheological characteristics of soil-ice is creep.

It has been demonstrated by several investigators (Vialov, 1965b; Sayles, 1968; Goughnour and Andersland, 1968) that soil-ice systems when subject to constant stress will develop what is considered to be a "classic" creep curve. Figure 2-1 shows this curve as a strain-time relationship for damped and undamped creep. Damped creep is defined as creep in which the strain approaches a limit as time increases. It is characterized by an instantaneous elastic strain and a region of decreasing strain rate approaching a constant strain. The undamped creep does not approach a constant strain and is typically divided into four sections: (1) instantaneous elastic strain resulting

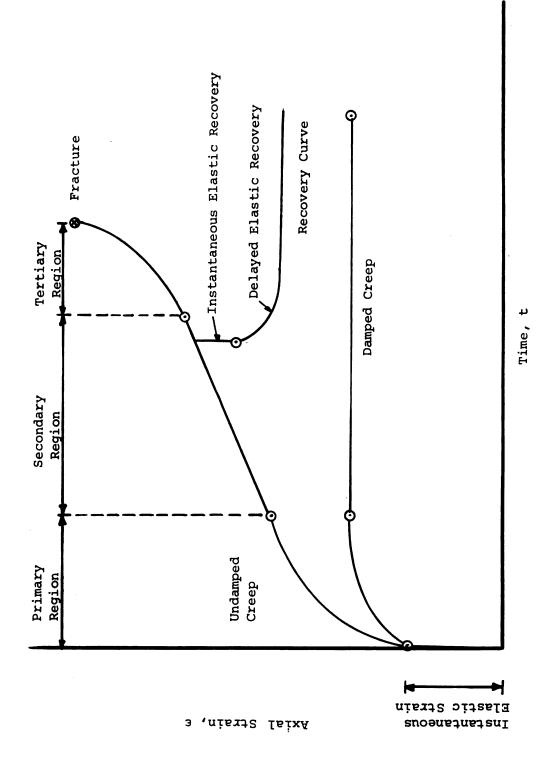


Figure 2-1.--Typical constant axial stress creep curves.

from the application of the load, (2) primary creep with a decreasing rate of strain, (3) a secondary region of constant or minimum strain rate and (4) the tertiary region in which strain rates increase to failure. Vialov (1965b), identifies these regions in terms of deformation processes. The region of instantaneous deformation is termed elastoplastic since not all of the deformation is recoverable. The primary region is the region of plastic deformation if irreversible deformation takes place. The secondary region is termed plastic-viscous since the constant deformation with time is comparable to the flow of a viscous fluid. Finally, the tertiary region is the region of progressive flow leading to a viscous failure. The division between damped and undamped creep is somewhat arbitrary since what at first glance is considered to be damped creep could be the secondary region of creep leading to failure if long term readings were obtained. It has been suggested (Scott, 1969) that the maximum load that can be applied and still produce damped creep is related to the unfrozen strength of the soil system. Any load which exceeds the ultimate strength of the soil structure alone will eventually lead to a creep failure.

If the undamped sample had been unloaded during the test a recovery curve similar to the one shown in Figure 2-1 would have resulted. Recovery is broken into two sections:

the instantaneous elastic recovery and the delayed elastic recovery. Not all of the strain that accumulated up to the time of removal of the load will be recovered, and most of the deformation remains permanently (Scott, 1969).

# 2.6.1 Theory

Various methods have been used to describe the behavior of a material as it deforms under a constant load. The most common methods include power law relationships, hyperbolic relationships and the hereditary creep theory as proposed by Vialov (1965a).

The hereditary creep theory is based on the assumption that the deformation at any time depends not only on the level of stress applied, but also on the history of prior deformations (Vialov, 1965b). The theory is straight forward mathematically and reduces to an equation for strain as a function of time as follows:

$$\varepsilon(t) = \frac{\sigma(t)}{E_o} + [K(t-t_o)\sigma(t_o)\Delta t]$$
 (2-8)

where the various components may be identified. The first term on the right,  $\frac{\sigma(t)}{E_O}$ , is the instantaneous deformation which takes place after the application of the load  $\sigma(t)$  at the present time t.  $E_O$  is the instantaneous modulus of elasticity. The second term is the result of previous loading and is the history dependent term.  $K(t-t_O)$  is a relaxation term, where K is a coefficient and  $(t-t_O)$  is the

time of relaxation.  $\sigma(t_0)$  is the previous load applied to the system at time  $t_0$  and  $\Delta t$  is the duration of the previous loads. Using this equation and the principle of superposition, all possible loading histories may be considered. In this equation the temperature dependency appears in the evaluation of the coefficient K and has a very strong influence on the developed strains. The hereditary creep theory has been used extensively by various Russian investigators to describe the rheological properties of both frozen and unfrozen soils (Vialov, 1965b).

The most recent theory to be used extensively to explain the creep characteristics of frozen soil is the rate process theory. This theory, as proposed by Gladstone, Laidler, and Eyring (1941), has its basis in statistical and quantum mechanics, and its application has been discussed by a number of investigators (Abdel-Hady, 1964; Dillon and Andersland, 1967; Mitchell, 1964) for various types of materials.

The rate process theory treats creep as a thermally activated process in which flow units of atoms, molecules or groups of molecules move across an energy barrier from one equilibrium position to another. The movement across the energy barrier is determined on a statistical basis and requires a flow unit to obtain sufficient energy  $\Delta F$ ,

termed the free energy of activation to surmount the barrier. For equilibrium conditions the movement is entirely random and the flow units cross the energy barrier equally in all directions resulting in no net flow of the material. If a directed potential is applied to the system, such as an axial stress, then the energy barrier becomes distorted in the direction of the applied potential and more flow units have sufficient energy to move in the direction of the potential than in the direction opposing the potential. The result is a net flow in the direction of the applied potential. Expressed in mathematical terms; the division of thermal energy among flow units is given by the Boltzmann distribution (Mitchell, 1964) and the frequency of activation v may be expressed as:

$$v = \frac{kT}{h} \exp \left[-\Delta F/RT\right]$$
 (2-9)

where  $k = Boltzmann's constant (1.38 x <math>10^{-16} erg K^{-1})$ 

T = absolute temperature, degrees Kelvin

 $h = Planck' constant (6.624 \times 10^{-27} erg-sec^{-1})$ 

 $R = universal gas constant (1.98 cal^{\circ}K^{-1} mole^{-1})$ 

 $\Delta F$  = free energy of activation, Cal/mole With application of the directed potential the energy barrier becomes distorted by an amount  $\frac{f\lambda}{2}$ , where f is the

applied potential and  $\lambda$  is the distance between equilibrium positions. The result is that the energy barrier has a height of  $(\Delta F + \frac{f\lambda}{2})$  in the direction opposing the potential and  $(\Delta F - \frac{f\lambda}{2})$  in the direction of the potential. Substituting these values into equation 2-9 and subtracting, results in an expression for the net increase in frequency of movement in the direction of the applied potential. If both sides of the expression are then multiplied by a parameter X, a function of the number of flow units, an expression for strain rate is obtained as:

$$\dot{\hat{\epsilon}} = \frac{2XkT}{h} \exp[-\Delta F/RT] \sinh [f\lambda/2kT] \qquad (2-10)$$

If the applied stress is large enough, the expression reduces to

$$\dot{\varepsilon} = \frac{XkT}{h} \exp \left[-\Delta F/RT\right] \exp \left[f\lambda/2kT\right] \qquad (2-11)$$

This is the form of the equation that is most frequently used in describing creep.

Using equation 2-11, some insight into factors that affect the frictional component of a sand-ice material can be shown. Mitchell (1964) proposed that

$$\Delta F = \Delta F_{o} + P(\phi + D_{a})$$
 (2-12)

in which  $\Delta F_{o}$  is the activation energy required to overcome the cohesive component of strength and P is the interparticle

component of activation energy composed of a frictional part  $\phi$  and a dilatancy part  $D_a$ . Then, substituting into equation 2-11

$$\dot{\varepsilon} = \frac{XkT}{h} \exp\left[\frac{-\Delta F_0 - P(\phi + D_a)}{kT}\right] \exp\left[\frac{f\lambda}{2kT}\right]$$
 (2-13)

If logarithms of both sides are taken, the result is

$$\ln \dot{\varepsilon} = \ln \frac{XkT}{h} - \frac{\Delta F_0}{kT} - \frac{P(\phi + D_a)}{kT} + \frac{f\lambda}{2kT}$$
 (2-14)

The shear force f is equal to the applied stress difference  $(\sigma_1^{-}\sigma_3)$  divided by a structural factor S, and solving for the stress difference:

$$(\sigma_1 - \sigma_3)$$
 = constant + constant + p  $(\phi + D_a)$  (2-15)

This equation separates the deviator stress into various components and can be used to study the factors that affect these components. For example, the frictional component is shown to be independent of both temperature and strain rate. In addition, the equation can be related to the Mohr-Coulomb equation if it is assumed that the test results were obtained at constant strain rate, temperature and structure. This result is particularly interesting since constant strain rate tests can be used to define an effective angle of friction that is independent of the ice properties.

Ladanyi (1972) has discussed the creep characteristics of frozen soils using a power law relationship.

In this discussion of creep behavior the steady state strain rate is determined to be some power of the applied uniaxial stress.

$$\dot{\varepsilon} = \dot{\varepsilon}_{\rm C} \left[ \frac{\sigma}{\sigma_{\rm C}({\rm T})} \right]^{\rm n} \qquad {\rm T = Constant} \qquad (2-16)$$

In this equation,  $\dot{\epsilon}_{\rm C}$  is a small normalizing strain rate,  $\sigma_{\rm C}({\bf T})$  is the uniaxial stress that causes  $\dot{\epsilon}_{\rm C}$ , and n is an experimentally determined power.

Using the basic power law formulation in equation 2-16, it is possible to obtain a relationship between the strain rate equation and the constant strain rate test results predicted by the Mohr-Coulomb equation. Starting with the expression:

$$\tau = C(t,T) + \sigma \tan \phi \qquad (2-17)$$

the equation can be rewritten in terms of the maximum stress difference as:

$$(\sigma_1 - \sigma_3)_f = \sigma_{fu}(t,T) + \sigma_3(N_c - 1)$$
 (2-18)

where  $(\sigma_1 - \sigma_3)_f$  = deviator stress at failure  $\sigma_{fu} = \text{unconfined compressive strength at time}$  t and temperature T  $N_C = \text{flow value} = (1 + \sin \phi) / (1 - \sin \phi)$ 

solving equation 2-16 in terms of the unconfined strength and substituting into equation 2-18 results in an expression for the deviator stress in terms of the confining pressure.

$$\sigma_{1} - \sigma_{3} = \sigma_{cuo} \left[ \frac{\varepsilon}{\varepsilon} \right]^{n} f(T) + \sigma_{3} (N_{c} - 1)$$
 (2-19)

where  $\sigma_{\text{cuo}}$  = unconfined compression strength for temperatures near  $0^{\circ}$  C.

 $\dot{\epsilon}^{c}$  = constant strain rate of the test

 $\dot{\varepsilon}_{c}$  = normalizing strain rate

f(T) = temperature term

This equation shows the shear strength as being dependent upon a cohesive term and a frictional term. The frictional term is dependent only on the angle of friction of the material and the confining pressures.

It is interesting to note that both the power law relationships and the rate process equations can be reduced to the form of the Mohr-Coulomb equation. In this form both contain a frictional component that is independent of strain rate and temperature.

# 2.6.2 Application of the Rate Process Theory

The most extensive investigation into the creep behavior of sand-ice using ideas from the rate process theory was reported by Andersland and AlNouri (1970). In determining the effect of mean stress, the logarithm of

the secondary creep rate was plotted against a stress factor  $\Sigma$  which is a function of the deviator stress and the mean stress. The resulting curve was linear and could be expressed as:

$$\dot{\varepsilon} = b \exp(m\Sigma)$$
 (2-20)

where b and m are experimentally determined parameters. The b term was found to be an exponential function of the deviator stress and the resulting equation took the form:

$$\dot{\varepsilon} = C \exp (ND) \exp (-m \sigma_m)$$
 (2-21)

where C and N are constants, D is equal to the deviator stress and  $\sigma_m$  is equal to the mean stress. This equation is in the form of the equations from rate process theory at large stresses and indicates an exponential increase in strain rate with increasing stress difference and an exponential decrease in strain rate with increasing mean stress.

In the same investigation (Andersland and AlNouri, 1970) the effect of temperature on the creep of sand-ice was determined using differential creep testing techniques and was found to be in the form

$$\dot{\epsilon} = A \exp \left(\frac{-L}{T}\right)$$
 (2-22)

where A is an experimentally determined parameter that includes the effects of the applied stress. This equation predicts creep to be an exponential function of the temperature. Ladanyi (1972) has noted that this is not descriptive of experimental work conducted over a wide range of temperatures, and suggests that there is evidence of a near linear temperature dependence for sand-ice down to -20.0° C.

#### CHAPTER III

#### MATERIALS AND SAMPLE PREPARATION

To eliminate the variables caused by particle composition and gradation, standard Ottawa sand, obtained from Soiltest Incorporated, was used in all sand-ice samples. The sand was composed of uniform sub-angular quartz particles with a specific gravity of 2.65. To insure uniform gradation only particles between the number 20 (0.84mm) and 30 (0.59mm) U. S. Standard sieve sizes were used. A sand volume of 64 percent was selected to obtain a dense soil structure. This volume of sand was well above the critical volume of 42 percent determined by Goughnour (1968) to be the point where intergranular friction is a major factor in the development of strength in sand-ice materials. Actual values of the percent of sand varied between 61.6 and 64.3 as noted in the test data shown in the Appendix. A sand volume of 64 percent produces a sample with a void ratio of 0.562.

The ice matrix was formed from deaired, deionized, distilled water. Using techniques outlined below, polycrystalline ice with densities of 0.918 to 0.854 gm/cm<sup>3</sup>

were obtained. The density of ice at -12.0°C is 0.91848 gm/cm<sup>3</sup> (Pounder, 1967). The difference between the actual and the test ice densities was due to small air bubbles trapped in the sample voids as the sample was saturated. If the voids had been completely saturated with ice, an ice content of 100 percent would have been obtained. Actual ice content for the high ice content samples ranges from 92.5 to 99.0 percent. Some special tests were made with ice contents of approximately 55 and 35 percent. These tests are noted in later sections.

Sample size and sample preparation were essentially the same as that used by Goughnour (1967) and AlNouri (1969). The sample size, 1.13 inches in diameter by 2.26 inches in height, was selected to yield a one square inch end area and a volume of 2.26 cubic inches. Knowing the specific gravity of the sand and the percent sand by volume the correct amount of oven dried sand could be predetermined.

The samples were prepared by pouring the predetermined amount of sand into a split aluminum mold that had been lightly greased with silicone vacuum grease to reduce adhesion between the mold and the sample. The mold was filled half full of sand and tamped 25 times with a rubber hammer. The remaining portion of the sand was poured into the mold and tamped just enough to bring the level of sand to the top of the mold.

Initial tests exhibited a tendency to flare at the top of the sample. It was believed that this was caused by local variations in density near the top of the sample. To eliminate this tendency, the mold was built up 0.3 inches and the top part of the sample was trimmed off to the correct height of 2.26 inches. This method eliminated the problem with flaring and the samples exhibited a more uniform cross section after testing.

After the sand had been poured into the mold, deaired, deionized, and precooled water was added to the sample until it appeared at the top of the mold. The mold was then tapped lightly to remove air bubbles that may have been trapped in the sample. This procedure was only partially successful since all samples contained less than 100 percent ice content. The sample was then placed in a cold box maintained at -18.0° C, and allowed to freeze for approximately 24 hours. After this period of time essentially all water was frozen and additional freezing time would not affect the strength of the sample (Sayles, 1968). Prior to mounting the sample in the triaxial cell, one sample end was trimmed with a sharpened paint scrapper to permit uniform seating with the loading cap.

The sample was then removed from the mold and transferred to another cold box for future mounting on the triaxial cell's pedestal. Here, the sample was

weighed both in air and immersed in fuel oil having a specific gravity of 0.832. The sample weight, volume, and ice content were obtained from these measurements.

To reduce end effects, friction reducers made of a sandwich of two layers of polyethelene and a greased aluminum disk were placed on each end of the sample. Next the sample was placed on top of the pedestal and capped with a lucite cap. A protective membrane was placed over the sample and fastened with rubber bands. The sample was then transferred to another cold box where it was mounted on the triaxial cell base plate. additional light membranes and one heavy membrane were placed over the sample. The triaxial cell's cover was placed over the sample and bolted to the base plate. The loading ram was brought into contact with the sample and the entire cell assembly was transferred to a work bench and the confining pressure gauge was attached. Finally, the cell and appurtenances were transferred to the cold bath and the cell was filled with coolant. Before testing, the triaxial cell and sample were allowed to stabilize in the cold bath for 12 hours at -12.0° C. This complicated mounting procedure was necessary to insure that the sample was never exposed to an environment that had any contact with the ethylene glycol coolant used in the cold bath since this could cause disintegration of the ice. This procedure took about 20 minutes and resulted

in an unusual temperature history for the samples. However, the samples were exposed to temperatures greater than -10.0° C for only a few seconds, and for sand-ice materials at temperatures less than -10.0° C, history has little effect on the strength of the materials (Scott, 1969).

After the sample had been tested the triaxial cell was removed from the cold bath and disassembled. The sample was inspected for membrane leaks and for indications of failure planes. The sample was weighed and the final volume obtained using the procedure described above. The entire sample was placed in a drying oven and the dry weight of sand and moisture content were obtained.

The sample preparation for the reduced ice content samples was the same, except a known volume of water was added to the sand instead of completely saturating the sample. The amounts of water used were 10, 8, and 4.5 ml, which resulted in ice contents of approximately 75, 55 and 35 percent, respectively.

In preparing reduced ice content samples there was some question as to the actual distribution of ice in the pore spaces. It is doubtful that the procedure described will result in a completely uniform distribution of water, and the ice contents indicated are nominal, based on the moisture content of the entire sample. The actual ice content distribution was higher

than the nominal at the bottom of the sample and lower than the nominal at the top. Use of snow or fine ice particles mixed with the sand was not attempted because of anticipated compaction problems for the desired high sand density. The results from reduced ice content samples did give a fairly reasonable indication of general magnitudes of strength.

#### CHAPTER IV

#### EQUIPMENT AND TEST PROCEDURES

Since triaxial tests covering a range of confining pressures from 0 psi to 1000 psi were conducted, the triaxial cell had to be constructed of a material that would withstand this range of pressures. The type of cell used was a special high pressure triaxial cell. The cell was a stainless steel Wykeham-Farrance triaxial cell constructed for a maximum working pressure of 1500 psi and tested to 2250 psi. The cell had a stainless steel hardened ram and adequate valves to provide for drainage and pressure control. Two base plates for the cell were specially designed and constructed at Michigan State University to provide for a 15,000 pound or a 5,000 pound capacity stud transducer. For the constant strain rate tests the base plate with the 15,000 pound capacity transducer was used. The creep and stepstress tests were performed using the base plate with the 5,000 pound capacity transducer.

In order to conduct the triaxial tests at pressures up to 1000 psi a pressure transmitting system was used similar to that described by Warder (1969). This system used pressurized nitrogen gas as the activating

source. The gas was transmitted from the nitrogen tanks through a regulating valve to a high pressure cell. In this cell the gas was brought into contact with the coolant liquid which transmitted the pressure to the triaxial cell. The high pressure cell also kept the coolant from backing up the line into the nitrogen tank during depressurizing. Gages were placed at various locations to monitor the pressure. A master gage attached to the triaxial cell was used to read the confining pressure in the triaxial cell. This gage had a 5 psi increment with an accuracy of 1/2 percent. The constant pressure regulator and the system described held the pressure constant during the tests with very little variation.

The other part of the system consisted of the refrigerator unit and its appurtenances which controlled the test temperature of the coolant. A micro-regulated portable refrigerating unit was used to control the temperature of the coolant. The coolant was circulated from the refrigerating unit to a cold bath in which the tri-axial cell was immersed. This system provided very good temperature control. Goughnour (1967) using a similar system determined, by using a thermocouple attached inside the triaxial cell, that temperature varied by not more than 0.05° C from the temperature of the coolant liquid in the cold bath. Temperature at the cold bath was monitored using a thermometer with scale divisions

of 0.1° C from which the temperature could be estimated to  $\pm$  0.01° C. The coolant used in the refrigerating unit was a mixture of about 1/2 ethylene glycol and 1/2 water. Figure 4-1 shows a schematic layout of the testing equipment.

Various types of transducers were used to measure the axial force and displacements during a test. The transducer used to measure the loads during the constant axial strain rate tests was a Strainsert model Q-1096 stud transducer with a 15,000 pound capacity. Loads measured with this transducer were accurate to ± 10 pounds. This unit had no provision for pressure equalization, and when the confining pressure was applied the transducer would indicate a negative load. The value for the negative load was set equal to zero and increases in load were measured from this value.

For the constant strain rate tests (samples 77-89) and the creep tests a Strainsert flat load cell type FL5U-2SP with 5,000 psi capacity was used. This load cell had an accuracy of  $\pm$  5 pounds.

To measure the axial displacement, a Sanborn Linearsyn differential transformer was used. The transformer was attached to the triaxial cell with the core element bearing on a collar plate fixed to the cell's loading ram. This allowed measurement of axial displacement within the cell and eliminated all other

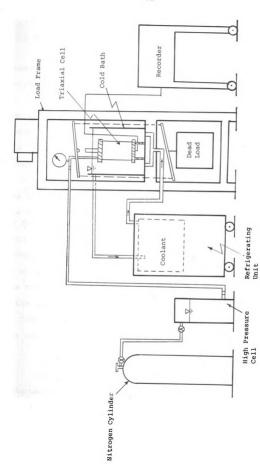


Figure 4-1.--Layout showing test equipment.

displacement measurements. The accuracy of measurements was + 0.0004 inches.

The force transducer and the differential transformer were connected to a Sanborn 150 4-channel recorder for permanent display of the results.

Two different load frames were used for the test series. The constant strain rate tests (samples 77-89) and the creep tests were performed on a Soiltest load frame Model T-118-X with a Graham variable speed transmission. The transmission was of the screw type and allowed displacement rates to be changed while tests were in progress. All other constant strain rate tests were conducted on a Wykeham-Farrance variable speed load-This frame had a 30 speed gear box with ing frame. speed selections from 0.225 to 0.000024 inches per minute. The machine performed satisfactorily, but there was no provision for changing the rate of displacement once the machine had started. The results indicate that as the load was applied, the displacement rate dropped off from the selected rate and did not return to this rate until after the peak load had been reached.

# 4.1 Triaxial Tests

Triaxial tests with constant strain rates were conducted on both confined and unconfined sand-ice samples. After the sample and triaxial cell had been

in the cold bath for about 12 hours, the test procedure outlined below was followed:

- The temperature of the cold bath was observed and recorded.
- 2. The force transducer and the displacement transformer were connected to the Sanborn recorder which was allowed to warm up. After an adequate warm up period both transducers were brought to a zero reading.
- 3. The load frame ram was lowered until it was just in contact with the triaxial cell's ram, with no load applied.
- 4. If the test was to be confined, the appropriate level of pressure was applied to the triaxial cell. If the test was unconfined, this step was omitted.
- 5. The drive mechanism was set at the desired speed (usually 0.006 in/min) and the loading ram was activated.
- 6. The trace of the load and deflection readings were observed on the recorder output charts. As the trace approached the top of the graph, the stylus was turned back using the zero suppression capability of the recorder.
- 7. After the peak load was observed on the recorder the driving mechanism was stopped

and the confining pressure, if any, was removed.

8. The temperature of the cold bath was recorded and the triaxial cell was removed from the cold bath.

Most of the constant strain rate triaxial tests were conducted on the Wykeham-Farrance load frame. However, 15 tests were conducted using the Soiltest apparatus. In these tests the procedure was as noted above with the exception of step six in which the trace of the displacement curve was observed and adjustments of the strain rate were made as the test progressed.

# 4.2 Creep Tests

All creep tests were conducted on the Soiltest load frame. Loads were applied by a loading yoke supporting a dead weight of lead bricks. The yoke was lowered by the drive motor of the load frame. When loads were applied to the sample, the drive was lowered at the fastest rate possible. Loading time was approximately five seconds.

## 4.2.1 Uniaxial

The procedure for conducting a uniaxial creep test was basically the same as the triaxial tests. The preliminary steps were the same as steps 1-4 listed in section 4.1. After the load was applied the trace of the

deflection curve was observed and at predetermined intervals small increments of weight were added to the sample to compensate for the increase in cross sectional area and to maintain a constant stress. The increments of weight were noted and used to check the load readings obtained from the recorder. The tests were allowed to run for approximately six hours before the load was removed. The samples were allowed to recover for one hour, then the triaxial cell was removed from the cold bath and disassembled.

## 4.2.2 Step-Stress

In step-stress testing the deviator stress was held constant and the confining pressure applied to a sample was changed by increments or steps. Except for the loading stage, the step-stress tests were conducted in the same manner as the uniaxial creep tests. During loading the selected level of stress was applied to the sample which was permitted to deform in the uniaxial state of stress for 60 minutes. At the end of this time an initial increment of confining pressure of 100 psi was applied to the sample. After the confining pressure was applied it was necessary to add weight to the dead load to retain the selected level of deviator stress. This was accomplished by observing the load trace on the recorder and adding weight until it returned to the

initial value. Additional increments of confining pressure were added at 120, 180, 240, 300 and 360 minutes. The total confining pressure after each of these increments was 200, 400, 600, 800 and 1000 psi, respectively. When operating at elevated confining pressure, the membranes were easily ruptured causing several of the step-stress tests to be terminated.

#### CHAPTER V

#### EXPERIMENTAL RESULTS

# 5.1 Constant Axial Strain Rate Tests

The mechanical properties of soils are usually measured using triaxial compression tests. More recently the effect of strain rate has been recognized as one of the many variables that affect the stress-strain relationships. As a consequence, constant axial strain rate testing was used to eliminate this potential variable. This section presents the results from constant axial strain rate tests on unfrozen sands, sand-ice with high ice content and sand-ice with reduced ice content.

# 5.1.1 Drained Tests

characteristics of frozen and unfrozen sands, the frictional behavior of the unfrozen sand was obtained for the same test conditions as the frozen sands. A series of drained triaxial tests were conducted on unfrozen Ottawa sand at a strain rate of 2.66 x 10<sup>-3</sup>min<sup>-1</sup> and a void ratio of 0.58. These tests were conducted in a standard perspex triaxial cell and were limited to 110 psi confining pressure. The frictional

characteristics for unfrozen sand at higher confining pressures were obtained from data presented by Lee and Seed (1967) and Vesic and Clough (1968).

Typical results of drained triaxial tests on unfrozen sand are shown in Figures 5-1 and 5-2. An angle of internal friction equal to 37° was obtained from the Mohr diagram shown in Figure 5-2. This value is typical for Ottawa sand with a void ratio of 0.58. Figure 5-1 shows the stress-strain and volume changes characteristic of the Ottawa sand. The curves indicate: (1) Volume change is negative (increases) for all tests with little variation between the tests at different confining pressures. At higher confining pressures the amount of volumetric strain decreases but will remain negative for pressures through 1000 psi (Lee and Seed, 1967); (2) Strain at failure ranges from four to six percent for all tests and (3) The peak strength increases as confining pressure increases. These results are in agreement with expected behavior.

## 5.1.2 High Ice Content

The effect of confining pressure on the strength of sand-ice materials tested at confining pressures from 0 to 1000 psi and a strain rate of  $2.66 \times 10^{-3} \text{min}^{-1}$  are shown in Figure 5.3. This rate of strain is fairly fast and resulted in failure times of 10-30 minutes, depending

on the confining pressures. In this figure it is apparent that strains at failure and peak strength of the sand-ice samples increase with confining pressures. This is also typical of results for unfrozen sand at high confining pressures (Lee and Seed, 1967). However, the curves for sand-ice materials show two yield points depending on the amount of confining pressure. For confining pressures in excess of 100 psi the curves have an initial yield point followed by a fairly linear increase in strength up to a second yield point that progresses to failure. This behavior is typical of all the samples tested at higher confining pressures. There is no indication that confining pressure greatly alters the value of the Young's modulus for the initial portion of the curves and except for the sample 44, there was little variation in the value of the initial yield point.

Figure 5-3 includes a plot of strain versus time for the various tests. The fact that this curve has a slight curvature indicates that the actual strain rate varies only slightly from the nominal strain rate of  $2.66 \times 10^{-3} \text{min}^{-1}$ . The variation is due to the test apparatus and appears to be typical of all the tests conducted on the Wykeham-Farrance loading frame.

Volume of sand, or void ratio is an important factor in determining the strength of sand-ice materials. To obtain the effect of confining pressure on this

variable, tests were conducted at various void ratios and confining pressures. Figure 5-4 and 5-5 show that void ratio affects strength through the entire range of confining pressures tested.

The initial yield for these tests is approximately 1200 psi and appears to be independent of the volume of sand. This value is greater than the maximum shear strength of ice tested under similar conditions, indicating some reinforcing effect due to the sand. The spread of the curves above the initial yield is the result of variations in the development of the frictional component resulting from the different volumes of sand. These figures show that the ice matrix does not appear to affect the basic frictional mechanism of a sand.

An additional factor which may affect the strength of a sand-ice sample is the strain rate. It is generally considered that increasing the strain rate will increase the strength of frozen soils (Kaplar, 1970). The results of uniaxial constant strain rate tests performed at three different strain rates are shown in Figure 5-6. These tests show an increase in peak strength as strain rate increases; however, the magnitude of the increase is only 250 psi for a ten-fold increase in the strain rate. What is more interesting is the trace of the curves. For the slowest strain rate there is a low initial yield followed by a non-linear increase of stress progressing to failure.

The faster strain rates have higher values for the initial yield point, and then progress much more rapidly to failure. Since the soil structure and volume of sand for the samples are constant, this indicates that the strain rate primarily affects the ice matrix. The difference in peak strength noted is approximately equal to the difference in the initial yield values.

To investigate the effect strain rate has on confined samples, a series of tests were conducted at 700 psi confining pressure for various strain rates. The strain rates varied from  $7.07 \times 10^{-5} \text{min}^{-1}$  to  $5.3 \times 10^{-3} \text{min}^{-1}$  or a factor of 75 when compared to the lower rate. Figure 5-7 shows the results of this test series. As is typical for confined samples, there is an initial yield followed by a linear increase of stress leading ultimately to failure. The initial yield is shown to be dependent upon strain rate, although the peak stresses for the samples varies by only a small amount. If the samples with constant strain rates are corrected for variations in percent of sand to a constant 63 percent, the peak strengths are as follows: sample 50, 2750 psi; sample 38, 2745 psi; and sample 48, 2450 psi. The differences noted are of the same magnitude as noted for the unconfined tests and are only a small percent of the peak stress.

Of particular interest in this test series are the results for sample 19 where three values of

strain-rate were used. For each increase in strain rate there is a corresponding linear increase in the stress followed by another yield point. As the strain rates increase, Young's modulus also increases. This implies that the ice matrix is responsive to the strain rate, and any change in test conditions will interrupt the existing equilibrium relationship and cause a new relationship to form.

The results of the constant axial strain rate tests on high ice content samples are summarized in Table 5-1.

# 5.1.3 Reduced Ice Content

To determine the effects of ice content and confining pressure, a series of tests were conducted on samples with ice contents of approximately 55 percent. The confining pressures were the same as used for the samples with high ice contents. The results for this test series are shown in Figure 5-8. The stress-strain behavior for samples with reduced ice contents was about the same as for the high ice contents, except that the peak strength was lower for all confining pressures. These curves also show that confining pressure does not increase the Young's modulus to any great extent, but the initial yield value does increase with increasing confining pressure. For the reduced ice content sample,

the initial yield that was so prominent for the high ice content samples was almost completely obscured until a confining pressure of 700 psi was applied. This suggests that the initial yield is related to the ice matrix and as the ice content is reduced, the behavior becomes more frictional in nature.

A better indication of the effect of reduced ice content on the stress-strain characteristics is shown in Figure 5-9. In this figure the results of both high and low ice content tests for typical unconfined and confined conditions are shown. It can be seen that for reduced ice content: (1) the strains at failure are slightly less than for the high ice content and (2) the difference in peak strength between high and low ice content is greatest for the unconfined samples.

To obtain a wider range of reduced ice contents, additional tests were conducted with an ice content of approximately 35 percent. Figure 5-10 shows that results of samples with four different ice contents and 100 psi confining pressure. These curves clearly show a small increase in Young's modulus as the ice content increases. One anomaly in the results of these tests is the strain at failure. As the ice content decreases, the strains at failure decrease. However, for the sample with zero ice content the strain at peak strength was larger than for any of the other tests.

The results obtained for all samples with reduced ice content emphasize the nonfrictional behavior of the initial portion of the stress-strain curve and the dominance of the frictional components as soon as adequate yielding has taken place. The results for the reduced ice content tests are summarized in Table 5-2.

Two samples of polycrystalline ice were prepared (as suggested by Goughnour (1967)), and tested at 0 and 685 psi confining pressure to verify the fact that ice is not appreciably affected by confining pressure. The results from these tests are shown in Figure 5-11 and indicate the effect of confining pressure is not very great. The small increases in strength may be due to confining pressures tending to prevent cracking of the ice as failure is approached. However, these tests may be inconclusive since only two samples were tested.

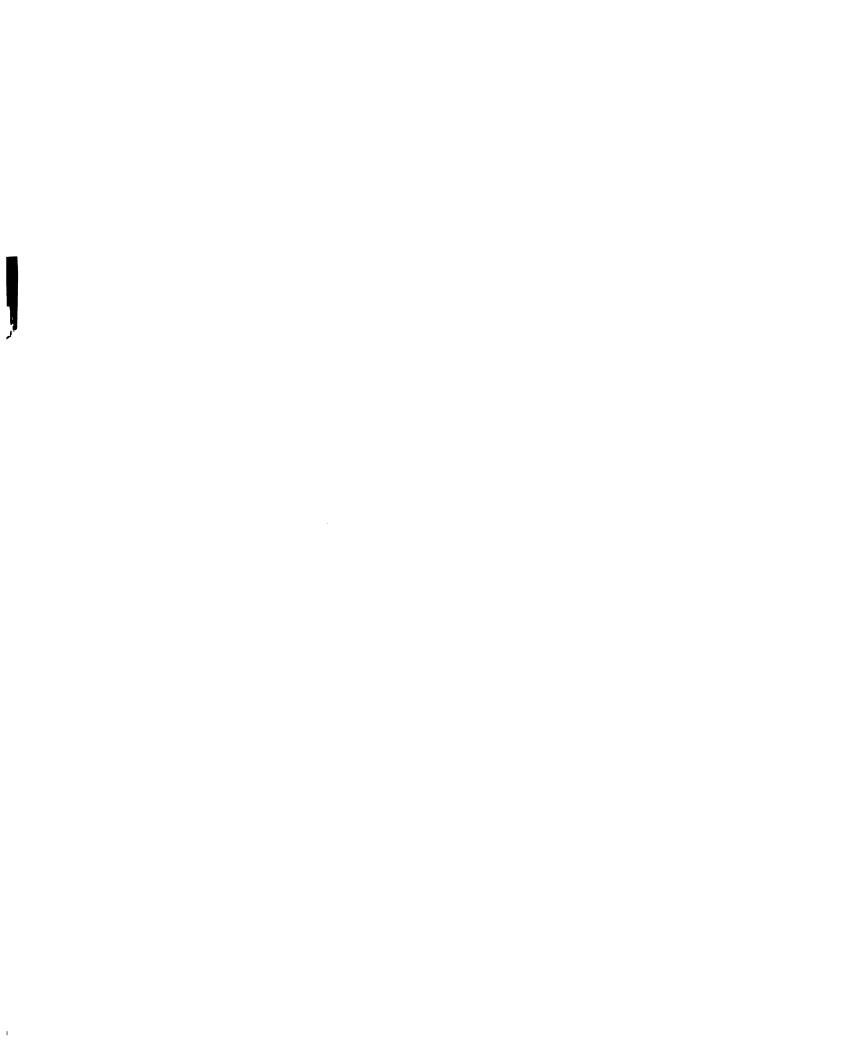
## 5.2 Creep Tests

It is known that the strength of frozen materials are highly dependent upon the time of load application and their behavior can be studied using creep testing techniques. In the following section the results of creep tests on sand-ice materials will be presented.

## 5.2.1 High Ice Content

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The creep behavior of sand-ice materials and relationships that are descriptive of their behavior



were studied using creep tests conducted in three different ways: uniaxial, confined and step-stress. Temperature was held constant at -12.0° C for all tests and selected constant deviator stresses of 400, 640, 750 and 1070 psi were used to give a wide range of creep behavior.

5.2.1.1 Uniaxial.—The main objective of the uniaxial tests on the sand-ice was to obtain the general creep behavior of the material and the magnitude of strains that result for a test time of approximately six hours. Typical results for the selected levels of stress are shown in Figure 5-12. Each of the curves show an instantaneous strain immediately after the application of the load followed by a region of decreasing strain rate. In sample 90 the region of noticeable decreasing strain rate was up to 200 minutes. Beyond this time the curves approach linearity.

The initial instantaneous deformation does not exhibit any clear trend because of slight variations in friction reducers and sample seating. To eliminate these variables, the strains for all the tests have been corrected by subtracting the strain at one minute. Figure 5-13 shows the corrected results for the four levels of axial stress. This curve gives a much clearer picture of the variations in strain between the stress levels.

- 5.2.1.2 Confined.--Before conducting step-stress creep tests where the confining pressure was varied at selected time intervals, it was necessary to observe the creep response of sand-ice under continuous confining pressure. The results of two tests conducted at a constant deviator stress and constant confining pressure are plotted in Figure 5-14. Shown for comparison are the results of a uniaxial test at the same stress level. If the test results are corrected as described in section 5.2.1.1, and replotted as in Figure 5-15, the effect of confining pressure is more apparent. As the confining pressures increase, the strains and strain rates decrease for any selected time. It is noted that the effect of confining pressure is greatest at low values since the original 200 psi increase in confining pressure had more than twice the effect of the 390 psi increment between the 210 psi and 600 psi level.
- 5.2.1.3 Step-Stress.--The effect of confining pressure on creep rate is shown by step-stress creep tests conducted at 400, 640 and 750 psi levels of constant deviator stress. Test results are shown in Figure 5-16 for confining pressures added at one hour intervals in the sequence 100, 200, 400, 600, 800 and 1000 psi. As each increment of confining pressure was applied, a rapid increase in strain took place due primarily to expansion

of the triaxial cell. Following this increase in strain due to cell expansion there was a region of fairly rapid increase in strain with time which quickly decreased, resulting in a strain rate less than the minimum for the preceding increment.

One additional test conducted to observe the step-stress characteristics at a constant deviator stress of 1070 psi is shown in Figure 5-17. A uniaxial creep test at the same level of stress has been shown for comparison. The increase in strain due to cell expansion followed by the region of decreasing strain with time, demonstrates that there was no basic difference between the step-stress test shown here and those discussed above. The region of decreasing strain and dampening effect of the confining pressure are more noticeable here than for the samples tested at lower levels of deviator stress.

Table 5.3 contains a summary of the experimental results for the creep tests on high ice content samples.

## 5.2.2 Reduced Ice Content

The creep behavior of frozen sand at reduced ice contents was studied by using constant deviator stresses of 400, 640 and 750 psi. These constant stresses were the same as for the high ice content samples. Sand volume and temperature (-12.0° C) were held as constant as possible. It was expected that reduced ice contents

would increase the frictional characteristics of creep and lead to a better identification of the processes involved in sand-ice materials.

5.2.2.1 Uniaxial. -- The results of uniaxial creep tests on reduced ice samples are shown in Figure 5-18. The curves illustrate the changes in creep behavior as axial stress increases. The curves all have the characteristic chape of "classical" creep curves, and one has progressed into the tertiary region and is in the process of failing. When compared to the high ice content samples with equal axial stresses, shown in Figure 5-12, the reduced ice content greatly accelerates the strain rates for any given axial stress.

The change in creep behavior for reduced ice content is shown by samples with three ice contents and a constant axial stress of 750 psi in Figure 5-19. As the ice content decreases, the strains at a constant time increase substantially, indicating a close relationship between the ice matrix and the creep behavior.

5.2.2.2 Confined. -- The results of a uniaxial creep test and a constant deviator stress creep test with continuous confining pressure on reduced ice content samples are plotted in Figure 5-20. When compared to the uniaxial test, the effect of the confining pressure is to dampen the response of the sample to the applied

stress. The same effect was noted for the high ice content samples, but the magnitude of the change of strain rates was not nearly as great.

5.2.2.3 Step-Stress.--Step-stress tests for the reduced ice content samples illustrated in Figure 5-21 include two levels of constant deviator stress. The sample tested at 640 psi developed a leak after the third increment of confining pressure was applied and the test was terminated after 180 minutes. The effect of confining pressure and development of the strain versus time curves are similar to the high ice content samples presented in section 5.2.1.3.

Uniaxial tests showed that a reduced ice content sample tested at an axial stress of 750 psi would progress to failure within one hour. Therefore, the time increments for applying confining pressure in the step-stress tests were decreased. The results of a step-stress test at a constant deviator stress of 750 psi is shown in Figure 5-22. For this test the confining pressure decreased strain rates significantly. Even at 90 minutes, the test did not progress into the tertiary region and strain rates were still decreasing. This test indicated that creep of a sand-ice material will be greatly decreased or prevented as confining pressures are increased.

TABLE 5-1.--Experimental results for constant axial strain rate tests, high ice content.

Sample No.	Percent Sand	Strain Rate	Strain at Failure	Peak Strength	Confining Pressure	Percent Ice	Total Volume Change	Remarks
	ою	min <sup>-1</sup>	in/in	psi	psi	o40	cm <sub>3</sub>	
1	-	2.66×10 <sup>-3</sup>		36	0		NA	
7	2		7	46	0	2	NA	
4	63.5	=	2	3	0	97.4	NA	
2	2.	=	$\mathcal{C}$	48	0		NA	
7	2.		Н	33	0		NA	
8	2.	.33x1	$\mathbf{c}$	47	0		NA	
	3.		2	90	S		NA	
	2	=	2	64	0		NA	
	2.	<b>E</b>	2	54	S		NA	
	2.		$\infty$	50	0		NA	
	2.	걲	Н	60	200	97.0	.19	
	2.	ies	7	9/	0		+0.332	
	3.	<b>8</b>	7	84	2		99.	
	2	2	S	78	S		NA	
	3.	=	9	13	S			rder
	2.	=	~	43	0		ဖ	Possible leak
	3.	£	4	97	350	9	+0.403	
	2.	=	7	99			.48	
	62.4	=	S	51	0	NA	NA	
	7	=	4	64	0	NA	+0.282	
	2.6es	=	7	61	0	NA	NA	
	3	=	$\infty$	74		NA	NA	
	3.	=	9	73	0	7	.55	
	3.	=	S	24	9		969.0+	
40	63.0	=	.036	7	100	NA	NA	
	62.9	=	$\sim$	7	0	0.96	+0.246	

								-1			: <del>:</del>				; ; ;	5			
.24	.42	.45	+0.100	.49	.74	NA	.60	+0.890	.18	.17	NA	NA	NA	NA	NA			-0.403	.29
9	9	9	96.5	9	9	Z	9	5.	5.	9	97.0	9	ъ.	œ	7			0.86	8
0	0	200	700	200	069	099	640	1000	200	1000	200	0	100	100	100		Samples	685	0
43	61	87	85	84	91	47	64	83	81	90	1956	56	64	61	50		Ice (	735	9
~	2	05	S	9	9	マ	ဖ	9	$\sim$	~	.032	$\overline{}$	$\overline{}$	$\overline{}$	$\vdash$			,030	.022
$2.66 \times 10^{-3}$		=	.33x		.33×10_	.66×10	=	=	=	=	=	=	=	=	2,66x10 <sup>-3</sup>			2.66×10 <sup>-3</sup>	=
2	س	<del>.</del>		٠ س		2	3	2	3	2	62.8	3	3	4.	ش			0	0
											82							20	

All tests:

-12.0° C Wykcham-Farrance Loading Frame unless noted

NA = Not Available

TABLE 5-2.--F.xperimental results for constant axial strain rate tests, reduced ice content.

ng Percent e Ice Remarks	ονo	57.0	53,6	55,8	58.2	55.0	59.4	32.9
Confining Pressure	psi	0	350	1000	700	100	0	100
Peak Strength	psi	885	1636	2584	2325	1029	834	817
Strain at Failure	in/in	.023	.040	.057	.052	.026	.022	.022
Strain Rate	min <sup>-1</sup>	$4.42 \times 10^{-3}$	2.66x10 <sup>-3</sup>	=	=	=	z	2.66×10 <sup>-3</sup>
Percent Sand	₩	62.7	63.0	62.5	63.4	62.9	63.7	63.2
Sample		72	73	74	92	78	79	87

All tests:

-12.0° C

Soiltest Loading Frame

TABLE 5-3.--Experimental results for creep tests, high ice content.

Percent Sand	o40	۳.	∞.	6.	6.	<b>۳</b>	.7	2.	.7
II.		63.3	63.8	63.9	62.	63.	63.7	63.2	62.7
Percent	∞	94.7	95.2	95.1	95.7	95.8	95.2	95.9	94.7
ll Minimum Strain Rate	min-1	3.0×10 <sup>-5</sup>	4.5×10 <sup>-6</sup>	1.0×10 <sup>-5</sup>	0.9×10 <sup>-5</sup>	2.5×10 <sup>-5</sup>	1.0×10 <sup>-5</sup>	1.2×10 <sup>-5</sup>	1.2×10 <sup>-5</sup>
Total Test Time	min	320	320	240	350	290	290	300	270
Total Volume Change	cm <sup>3</sup>	+0.228	-0.078	-0.078	-0.012	+0.144	-0.054	-0.012	-0.216
Confining Pressure	psi	0	0	0	0	0	0	205	009
Maximum Percent d Deviator of Maximum or Stress Deviator s Fig. 6-3 Stress	oγo	70.5	26.0	41.0	42.5	70.5	49.0	38.0	30.5
Maximum Deviator r Stress Fig. 6-3	psi	1520	1540	1550	1500	1520	1540	1994	2465
Applie Deviato Stress	psì	1070	400	640	640	1070	750	750	750
Sample I		06	96	66	101	102	108	115	118

63.6	63.8	63.1	62.3
95.1	95.5	95. 5	95.5
4.3x10 <sup>-5</sup> 1.8x10 <sup>-5</sup>	4.0x10-5 1.9x10-5 1.3x10-5 1.2x10-5 1.1x10-5 0.9x10-5	1.5x10-5 1.2x10-5 1.0x10-5 7.8x10-6 8.0x10-6 8.0x10-6	4.4×10-5 2.7×10-5 1.8×10-5 1.5×10-5 1.2×10-5 1.1×10-5
180	120 120 180 340 400	120 120 180 240 360 400	60 120 180 240 300 360
+0.108	-0.078	-0.072	-0.048
350	100 200 400 600 800 1000	100 200 200 400 600 800	100 200 400 600 800
69.5 45.5	41.5 36.0 31.5 25.5 20.5	26.5 23.0 21.0 17.5 14.0	51.0 45.0 37.5 32.0 29.0
1540	1540 1770 2030 2500 2840 3120 3350	1510 1720 1900 2270 2600 2880 3100	1470 1660 1760 1990 2340 2600
1070	640	400	.750
91	100	109	121

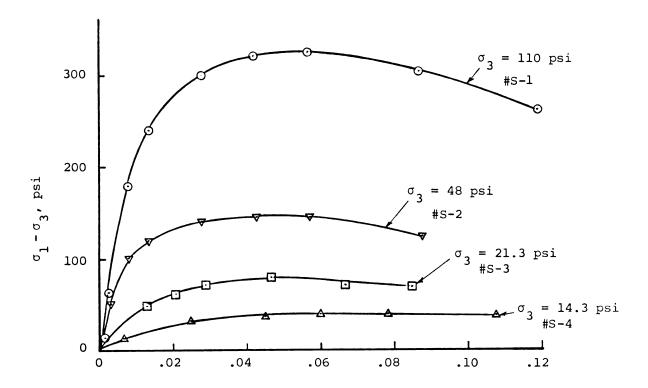
All tests: -12.0° C

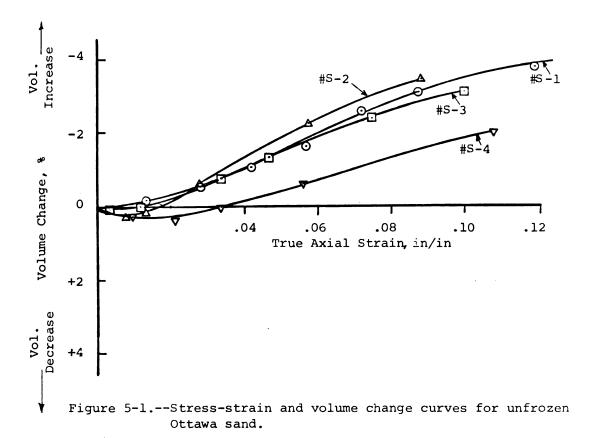
TABLE 5-4.--Experimental results for creep tests, reduced ice content.

Remarks							Leak@30 min		
Percent Sand	96	63.8	63.3	63.5	63.4	64.2	63.6	63.9	63.8
Percent Ice	0/0	8.09	58.8	59.6	69.5	70.7	62.5	64.6	59.4
Minimum Strain Rate	min <sup>-1</sup>	9.0x10 <sup>-6</sup>	3.7×10 <sup>-5</sup>	5.0x10 <sup>-4</sup>	1.1x10 <sup>-5</sup>	4.1x10 <sup>-5</sup>	NA	0.9×10 <sup>-5</sup>	4.5×10 <sup>-5</sup> 2.5×10 <sup>-5</sup>
Total Test Time	min	350	365	46	510	240	150	260	60
Confining Pressure	psi	0	0	0	0	0	205	009	100
Percent of Maximum Deviator Stress	₩	42.5	71.5	83,5	70.5	68.5	52.4	34.5	43.5 38.0
Maximum Deviator Stress Fig. 6-3	psi	937	895	895	1060	1100	1210	1860	915
	psi	400	640	750	750	750	640	640	400
Sample Applied No. Deviator Stress		93	97	107	111	114	119	120	94

	Leak @180 min	Leak@ 28 min	Leak@180 min	Leak@120 min	
	63.6	64.0	64.0	63.1	63.6
	60.0est	60.0est	60.0est	60.0est	60.5
1.8×10-5 1.5×10-5 1.3×10-5 1.2×10-5 0.9×10-5	9.0x10 <sup>-5</sup> 5.4x10 <sup>-5</sup> 2.7x10	1.1x10 <sup>-3</sup> 3.0x10 <sup>-4</sup> 3.0x10 <sup>-4</sup>	8.0x10 <sup>-5</sup> 4.0x10 <sup>-5</sup> 1.8x10 <sup>-5</sup>	6.5x10 <sup>-5</sup> 2.5x10 <sup>-5</sup>	6.4×10 <sup>4</sup> 3.2×10 <sup>4</sup> 1.4×10 <sup>6</sup> 9.0×10 <sup>6</sup> 5.0×10 <sup>6</sup> 2.0×10 <sup>6</sup>
180 240 300 400	60 120 180	13 28 28	60 120 180	60	15 26 40 60 95
200 400 600 800 1000	100 200	200 400	100 200	100	100 200 400 800
33.0 27.0 23.7 21.5	70.0 60.5 53.5	81.0 60.5 49.0	69.0 60.0 51.5	44.5 39.0	81.0 70.0 62.0 51.0 45.0
1210 1480 1690 1860 1990	920 1060 1200	930 1240 1540	930 1070 1240	905	925 1070 1210 1470 1670 1850
	640	750	640	400	750
	8	104	112	113	117

All tests: -12.0° C





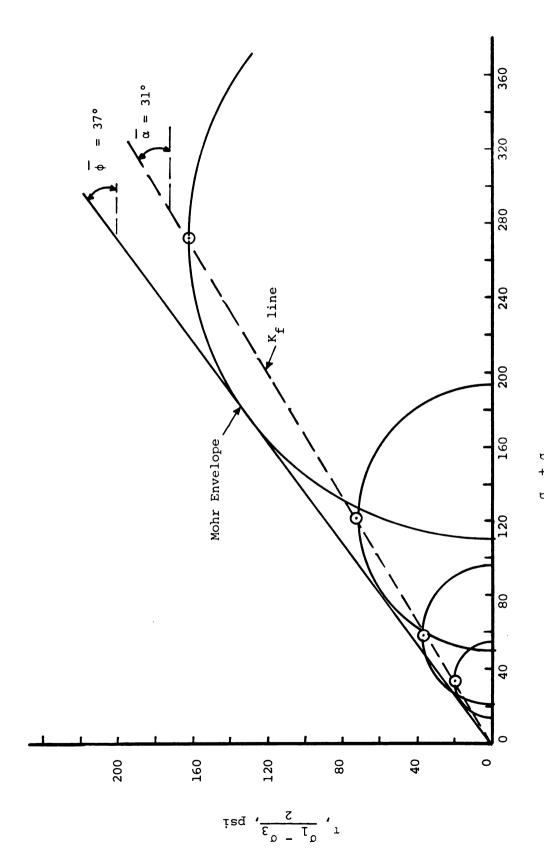
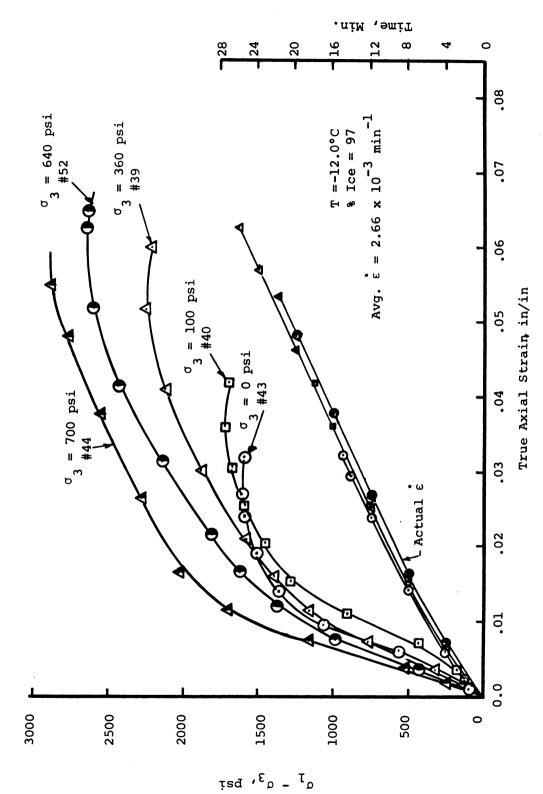
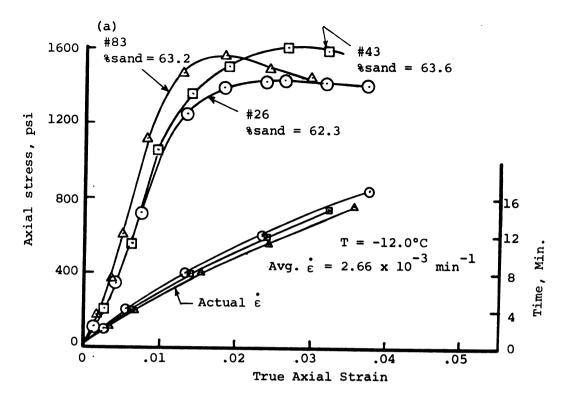


Figure 5-2. -- Drained test results on unfrozen Ottawa sand.



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Figure 5-3. -- Effect of confining pressure on the stress-strain behavior of sand ice materials.



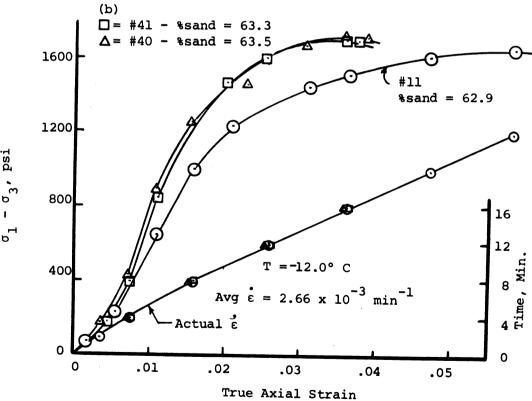


Figure 5-4.--Effect of volume of sand on strength.

- (a) Unconfined
- (b) Confining pressure 100 psi.

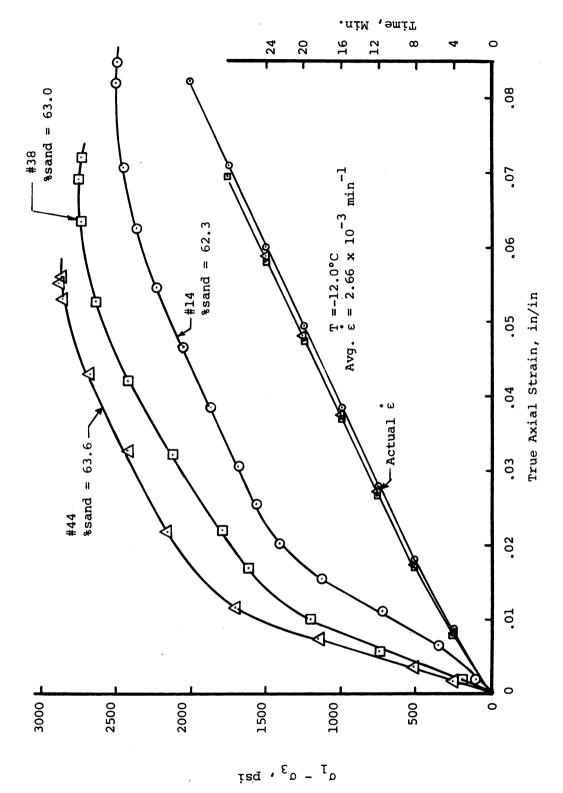


Figure 5-5. -- Effect of volume of sand on strength for a confining pressure of 700 psi.

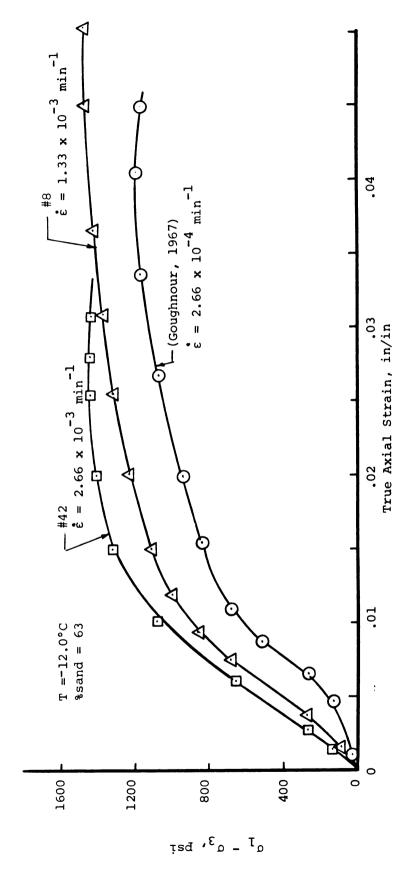


Figure 5-6.--Effect of strain rate on strength for unconfined tests.

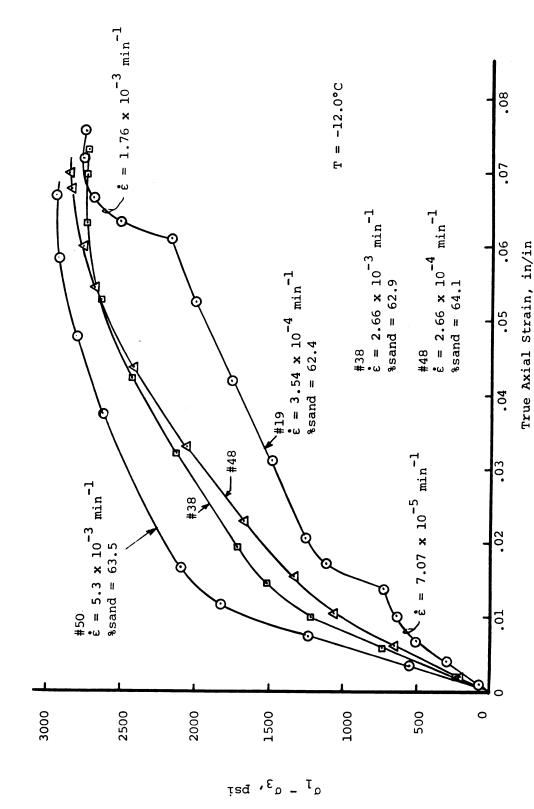


Figure 5-7.--Effect of strain rate on strength for confining pressure equal to 700 psi.

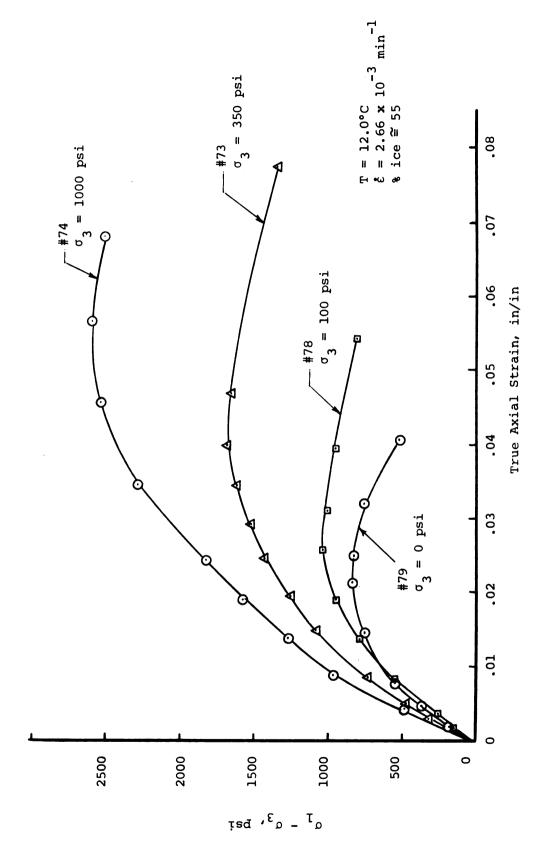


Figure 5-8.--Effect of confining pressure on strength for reduced ice contents.

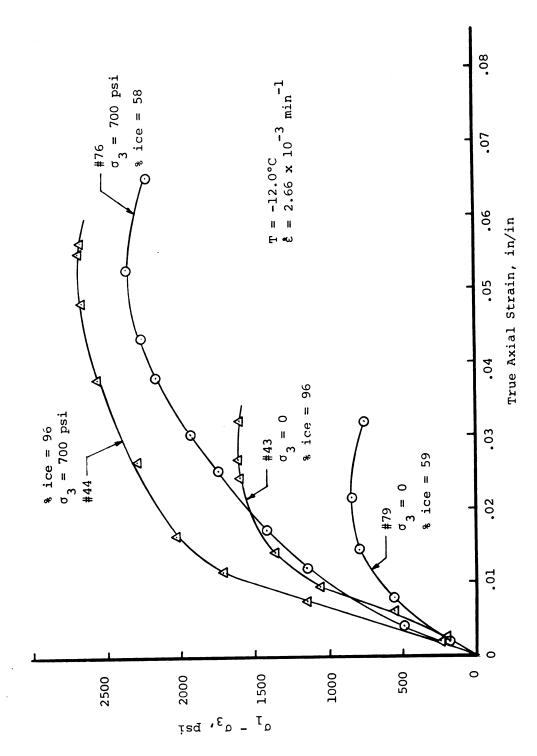


Figure 5-9. -- Stress-strain curves for high and reduced ice contents.

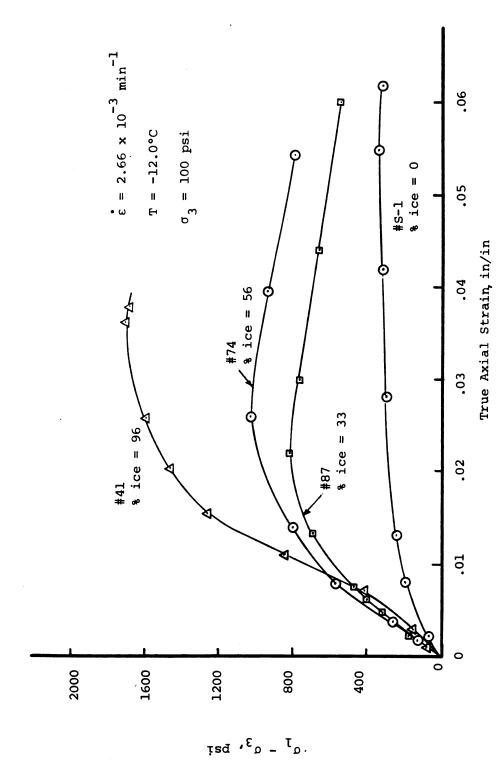


Figure 5-10. -- Stress-strain curves for various ice contents.

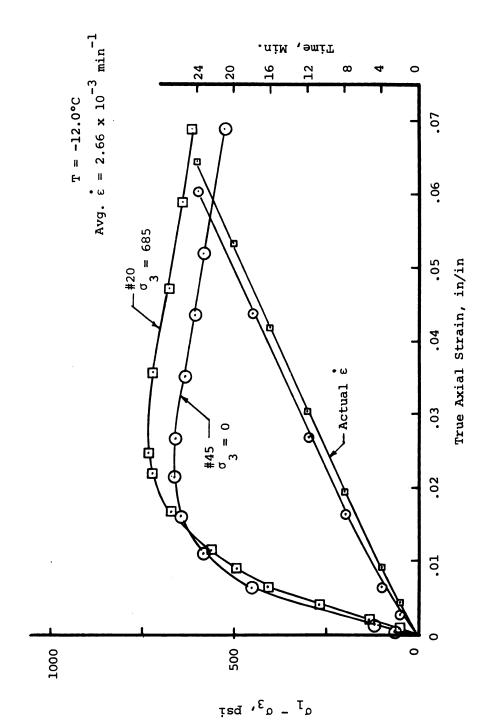


Figure 5-11. -- Stress-strain curves for polycrystalline ice samples.

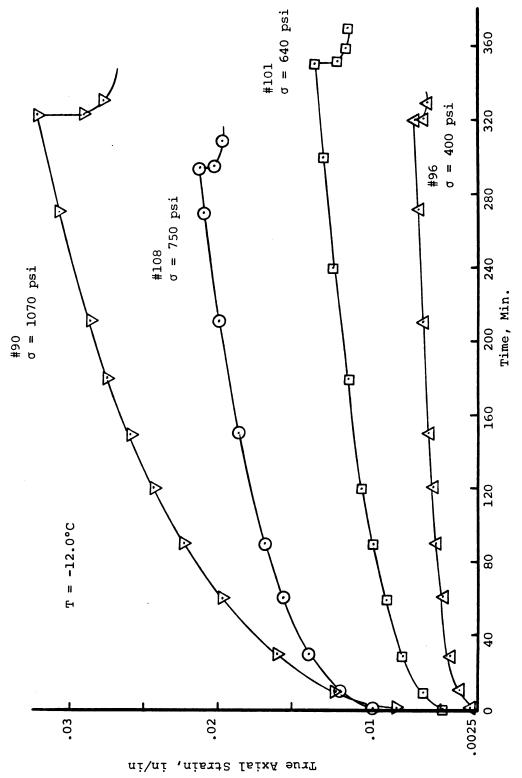


Figure 5-12. -- Uniaxial stress creep curves for high ice contents.

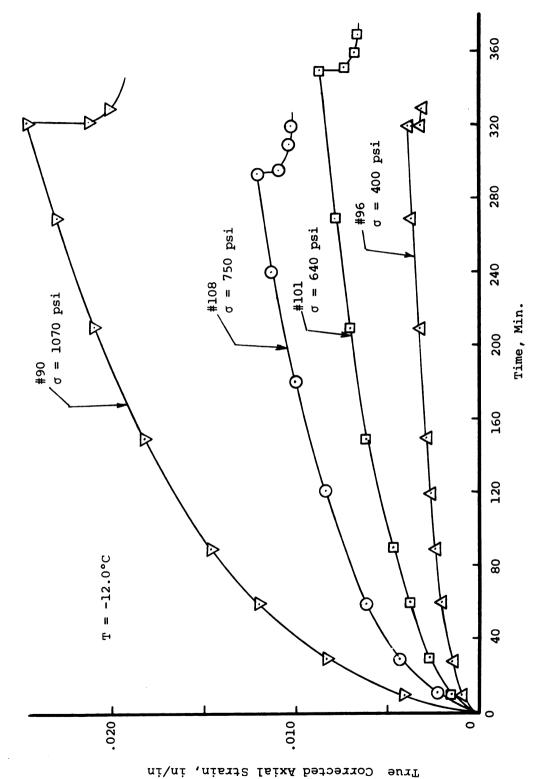


Figure 5-13.--Corrected uniaxial stress creep curves for high ice contents.

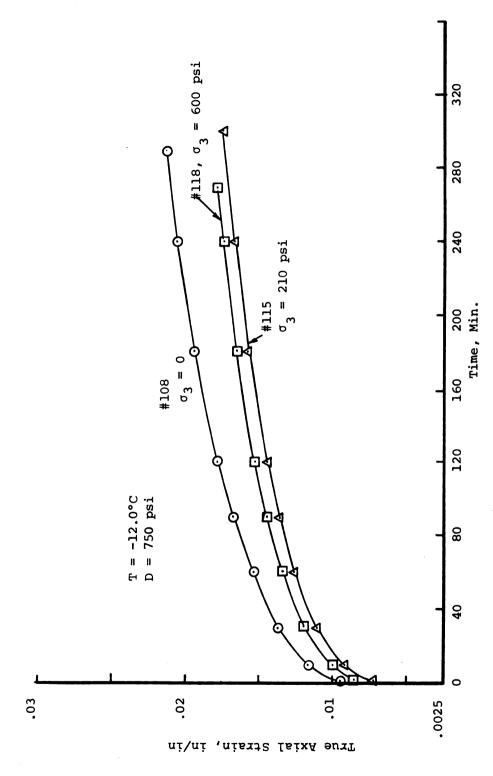


Figure 5-14. -- Constant axial load creep with constant confining pressure.

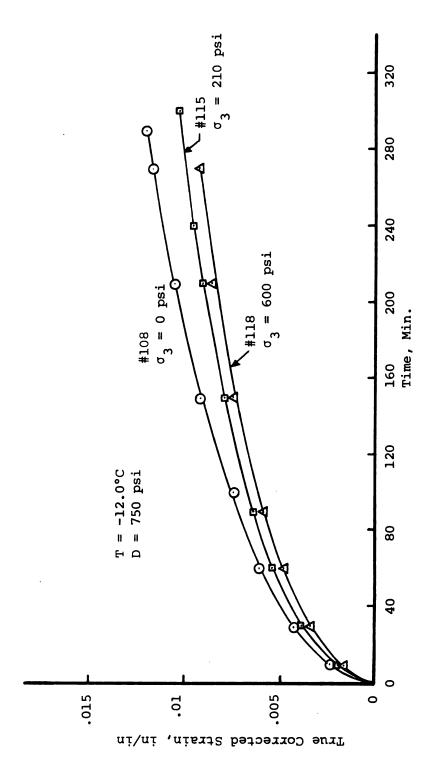


Figure 5-15. -- Corrected constant axial load creep with constant confining pressure.

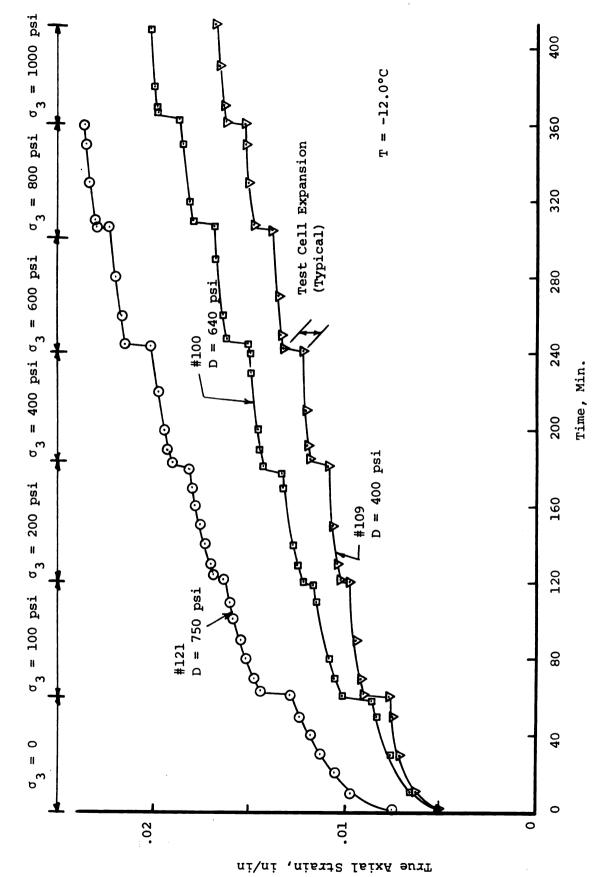


Figure 5-16.--Step-stress creep for high ice content.

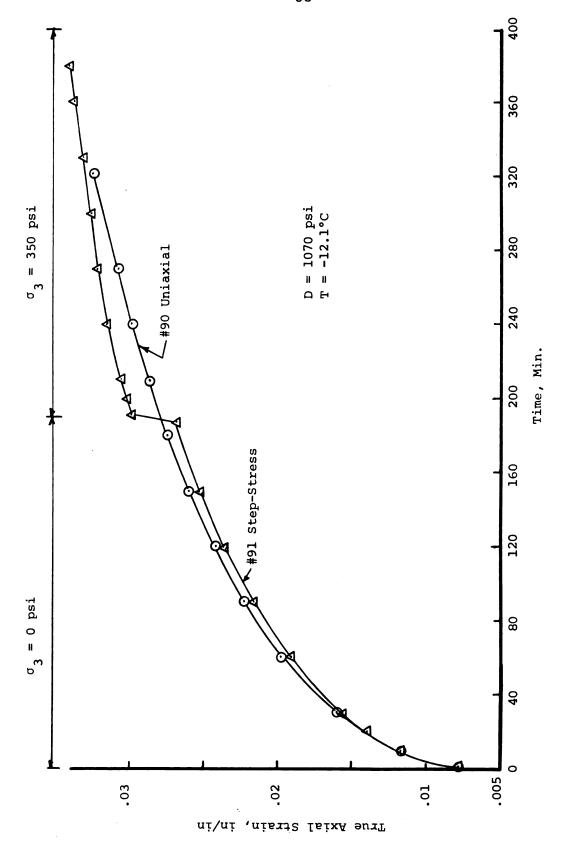


Figure 5-17. -- Uniaxial and step stress creep for high ice content.

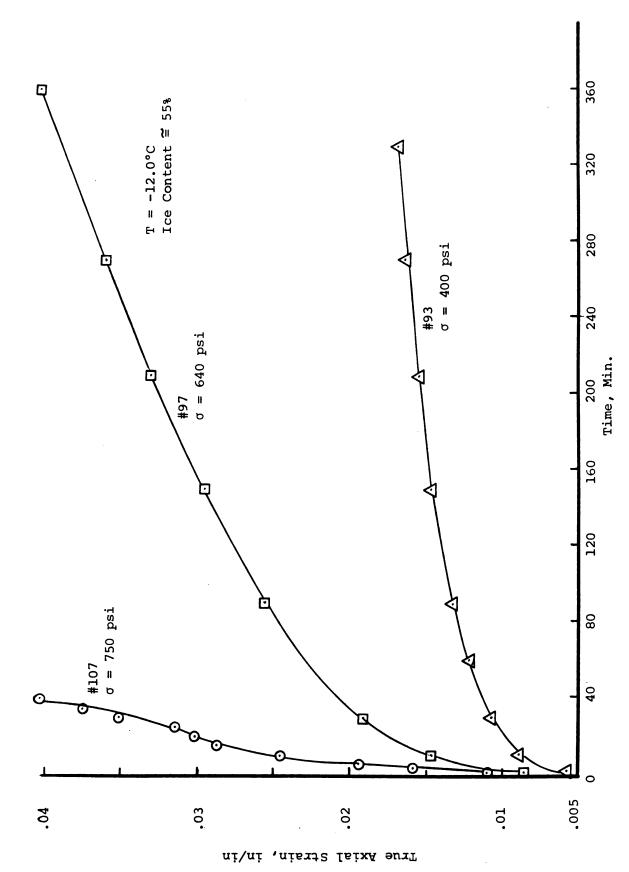


Figure 5-18.--Uniaxial stress creep for reduced ice content.

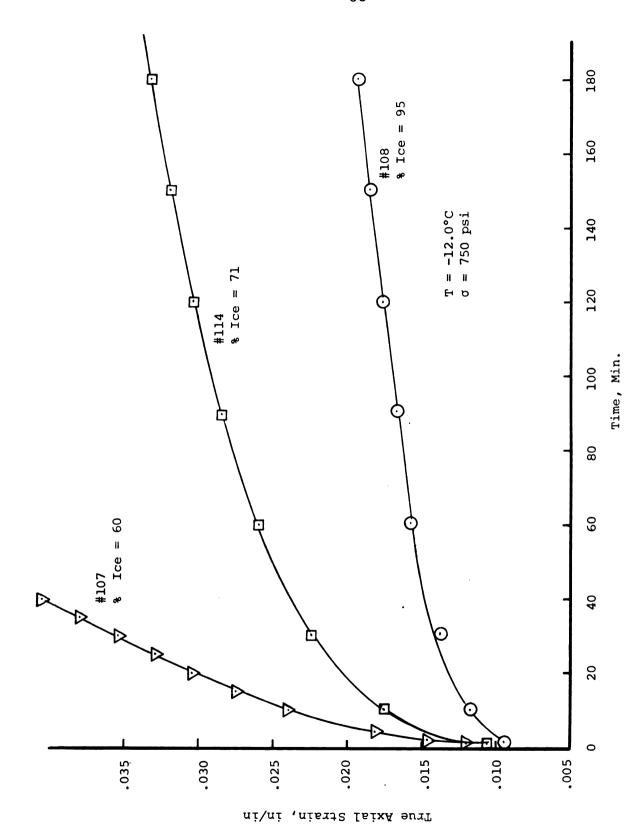


Figure 5-19. -- Effect of ice content on uniaxial stress creep.

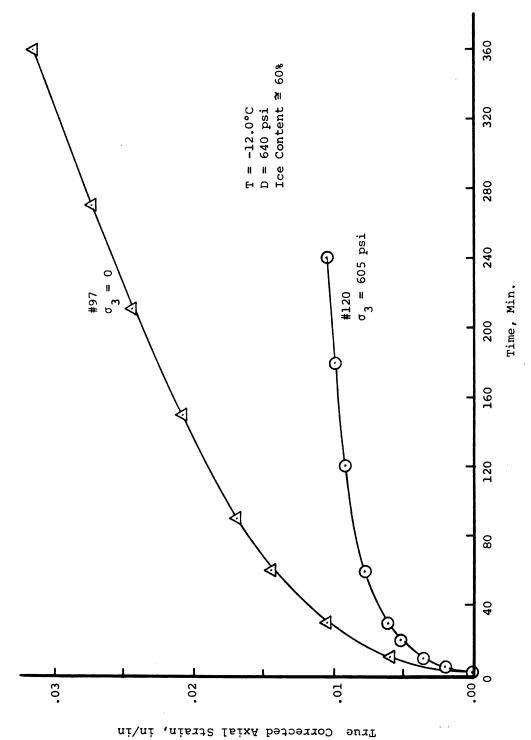


Figure 5-20. -- Corrected constant axial load creep with constant confining pressure and reduced ice content.

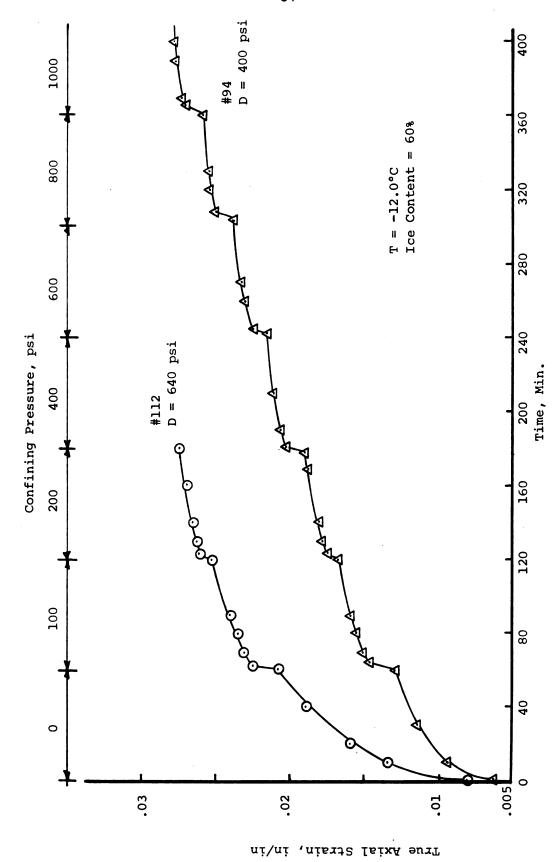


Figure 5-21. -- Step-stress creep for reduced ice content, D = 400 and 640 psi.

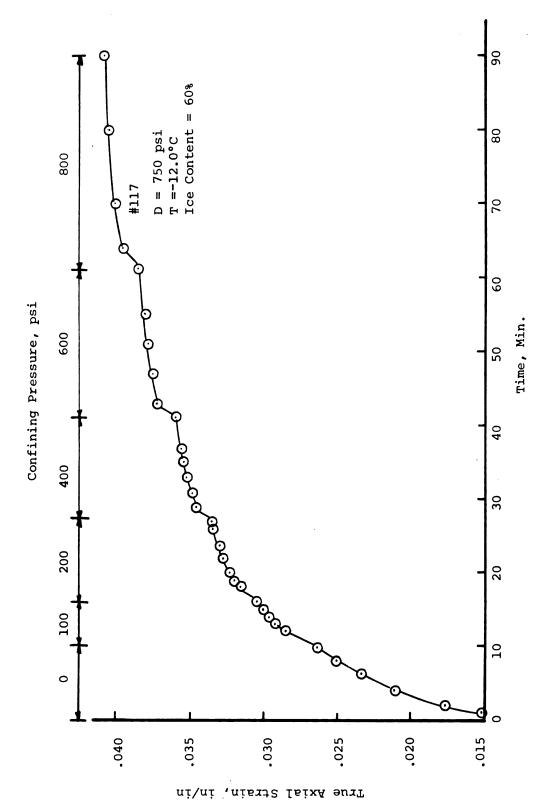


Figure 5-22.--Step-stress creep for reduced ice content, D = 750 psi.

#### CHAPTER VI

#### DISCUSSION OF RESULTS

#### 6.1 Factors Controlling Shear Strength

Assuming that shear strength of a sand-ice material is composed of cohesive and frictional components which may be identified and isolated, the effect of various factors on these components can be shown. Vialov (1965b) has shown that the cohesive component of sand-ice is due primarily to confinement by the ice matrix and factors that alter the ice matrix will change the shear strength proportionately. The major cause for variations in the cohesion of the ice matrix is temperature (Vialov, 1965b), with strain rate and ice content having effects that are less well understood. By holding temperature constant, while changing the strain rate or ice content, the effect of these factors was observed.

The frictional component of strength for dense sand-ice materials tested to failure is independent of time, strain rate and ice content, and dependent on the void ratio and confining pressure. The effects of these factors were obtained by testing samples at constant strain rates and various void ratios over a large range of confining pressure.

In the following sections each of the factors which affect the frictional and cohesive component of strength will be discussed. The effect of confining pressure on the various factors will be discussed as it occurs.

## 6.1.1 Frictional Component

The frictional component of strength for sand-ice materials is dependent on the frictional characteristic of the sand material. Koerner (1970) has identified particle size, shape and gradation as factors which may affect the frictional behavior of single mineral soils. By using only Ottawa sand between the number 20 (0.84mm) and 30 (0.59mm) U. S. Standard sieve size, these factors were minimized. Once these factors have been eliminated, the frictional characteristics of the single mineral sand is dependent on sliding friction, dilatancy, and particle crushing and rearranging. Because of the high volume of sand in the sand-ice samples tested herein, particle to particle contact is likely to occur and sliding friction will develop with deformation. This will be true even if it is assumed that each grain of sand is surrounded by a layer of ice, since the contact pressures that develop will be high enough to cause pressure melting and migration of moisture at contact points. Particle crushing is known (Lee and Seed, 1967) to be small for Ottawa sand tested up to 1000 psi confining pressure and will not contribute

significantly to the frictional component of strength. Thus, the only unaccounted-for component of frictional strength is dilatancy. As the confining pressure increases, the volume changes associated with dilatancy are resisted by the confining pressure resulting in a lower component of strength due to dilatancy, and a lower angle of friction. For sand-ice materials both the applied confining pressure and the confinement due to the ice matrix retard volume changes resulting in a low component of strength due to dilatancy. As a result, the angle of friction for sand-ice materials will be lower than those obtained from unfrozen sands at similar confining pressures.

To verify these observations, volume measurements were taken both before and after testing selected samples. Since the equipment did not allow the measurment of volume changes during the test, total volumetric strain per test was divided by the unit strain at the end of the test to obtain an average change per unit of strain. The results of this procedure, shown in Figure 6-1, permit several observations to be made: (1) volume changes are small and are all negative (increase) for the sand densities tested; (2) volumetric strain per unit strain decrease as confining pressure increases; and (3) volume changes are less for sand-ice materials than for unfrozen sand at equal confining pressures. These observations verify the original assumption that dilatancy must contribute to the strength of sand-ice

materials. However, the fact that the values of volumetric strains are small implies that the contribution to strength will be small. The resulting angle of friction obtained for sand-ice materials should be comparable to those obtained for dense sands at high confining pressures where dilatancy has also been reduced.

# 6.1.2 Void Ratio (Density)

One of the variables that affects the peak strength is the variation of void ratio between sand-ice samples.

This factor has been reported by other investigators
(Kapler, 1971; Goughnour, 1967; and Yong, 1963) for sand-ice materials and is an indication that the material retains some of the frictional characteristics of unfrozen sand.

A decrease in void ratio for unfrozen sand tends to increase the maximum deviator stress at failure (Koerner, 1970; Lee and Seed, 1967). This is due to dilatancy and particle rearranging and crushing. For sand-ice materials the actual magnitude of the strength increase appears to be dependent upon the confining pressure in addition to the void ratio.

Using uniaxial compression tests, Goughnour and Andersland (1968) showed a bilinear relationship between the volume of sand and peak strength. A similar presentation is shown in Figure 6-2. The majority of the data for this graph was obtained from Goughnour (1967) with additional points added from the tests conducted in this study. The

test procedures and sample preparation were the same for all tests. This figure also shows an increase in peak strength due to changes in temperature and strain rate.

It is interesting to note that above a sand volume of approximately 42 percent the change in slope of the curves at the different temperatures appears related to the ability of the ice matrix to exert various effective stresses in the sample. If the ability of the ice matrix to apply confining pressure is the requirement for increasing the slope of the curves, it would be expected that other factors which increase the cohesive component of strength may also increase the slope of the line. There is an indication in Figure 6-2 that this is the case. The tests conducted at a strain rate of  $2.66 \times 10^{-3} \text{min}^{-1}$ have a slightly greater slope than the tests conducted at  $2.66 \times 10^{-4} \text{min}^{-1}$ . There is a limitation for which this will occur, since there is a confining pressure at which dilatancy will be prevented and the friction angle will become constant.

The results of increased confining pressure and volume of sand on the peak deviator stress are shown in Figure 6-3. Increased confining pressures serve to increase the maximum deviator stress per unit increase in sand volume. Above 350 psi the increase in maximum deviator stress per unit increase in sand volume appears to be constant, nearly parallel curves. These results reinforce

the previous discussion concerning a limiting value of confining pressure that can cause an increase in the slope of the strength versus percent of sand curves. Lee and Seed (1967) showed that as the confining pressure on unfrozen sand samples increased, the difference in failure stresses between a loose and a dense sample increases up to a maximum value and then remains essentially constant. The same behavior is shown in Figure 6-3 for the sand-ice material. Thus, for sand-ice at low confining pressures, dilatancy contributes to the variations in strength between samples with different void ratios. At high confining pressures the dilatancy component of strength is reduced, producing a fairly constant difference in deviator stress between dense and loose sand-ice samples. This explanation implies that the response of the ice matrix can be considered analogous to higher effective stresses, and variations in sand volume do not increase or decrease that response.

Since the effect of void ratio is influenced by the confining pressure applied to the sample, it is necessary to account for all pressures. For a sand-ice system, there is not only the externally applied confining pressure but an internal increase in effective stresses provided by the ice matrix. If the internal and external pressures are added, it is apparent that the frictional component of strength in sand-ice systems can be compared to unfrozen

sands only if the unfrozen materials are tested at higher confining pressures.

Another indication of the interrelationship of confining pressure and percent of sand by volume can be obtained by plotting the peak stresses in terms of the principal stress ratio. In Figure 6-4 the principal stress ratio versus the percent of sand by volume is shown for various confining pressures. This graph shows that the lower the confining pressure, the more sensitive the principal stress ratio is to changes in sand volume. In fact, at high confining pressure the principal stress ratio is quite insensitive to changes in the sand volume and approaches a constant level. This type of behavior is also typical of unfrozen sands at high confining pressure (Lee and Seed, 1967).

### 6.1.3 Relative Ice Content

In order to magnify the frictional characteristics of a sand-ice material, tests on samples with reduced ice content were conducted. To relate strength to a function of ice content, the term "percent of ice" is used. The percent of ice is defined as the volume of ice divided by the volume of voids multiplied by 100. The calculation of the volume of ice is determined by dividing the weight of water in a sample by the density of ice at  $-12.0^{\circ}$  C  $(0.91848 \text{ gm/cm}^3)$ .

Kaplar (1971), Vialov (1965b), and Yong (1963) have shown that strength of sand-ice materials decrease approximately linearly with a decrease in the percent of ice in the sample. These results were obtained for unconfined tests with no indication of the effects of confining pressure. The results of confined compression tests on samples with different ice contents are shown in Figure 6-5. Values for the high percent of ice were obtained from Figure 6-3 using the same volumes of sand as contained in the reduced ice samples. This figure indicates a linear and constant decrease in deviator stress with reduced ice content for all confining pressures. Since each line of equal confining pressure has a different volume of sand, the reduction in strength due to changes in the ice content is independent of both confining pressure and volume of sand. From this result it can be concluded that the reduction in strength is due entirely to a loss of cohesion and samples at reduced ice content will have the same frictional characteristics as samples at high ice contents.

To compare the significance of the percent of ice for various confining pressures a plot of reduction in strength versus confining pressure is shown in Figure 6-6. The reduction in strength is calculated as follows:

$$\frac{D_{H} - D_{L}}{D_{H}} \times 100$$

where

D<sub>H</sub> = Maximum deviator stress for high percent ice.

 $D_{\tau}$  = Maximum deviator stress for low percent ice.

This figure indicates that the reduction of strength decreases as the confining pressure increases. This is another indication that strength at high confining pressure is less dependent on the ice matrix and becomes primarily frictional in nature.

#### 6.1.4 Confining Pressure

Previous investigations into the strength behavior of frozen soils have been primarily conducted on samples that were unconfined or at low confining pressures. Yong (1963), Goughnour (1967), and AlNouri (1969) have conducted tests on sand-ice materials at confining pressures up to 150 psi. In order to extend the data of these investigators confining pressures up to 1000 psi were used to determine the effect on the strength of sand-ice materials. This range of pressures has been used on unfrozen sand by Lee and Seed (1967). The data from this study was used to interpret the results for frozen sand.

Typical stress-strain behavior for unconfined and confined tests is shown in Figure 6-7. These tests indicate that for low confining pressures the curves progress through an initial period of high stress increase per unit strain

followed by partial yielding leading ultimately to failure. The sample with the higher confining pressure behaves in a similar fashion up through the initial yield point. However, after this point additional strengthening due to dilatancy and sliding friction takes place and there is a long, fairly linear increase in stress, progressing eventually to failure. Similar results have been observed in unfrozen materials with a cohesive matrix (Schmertmann and Osterberg, 1960) where the initial yield point is identified as matrix yield.

An indication of the relative magnitudes of the proportions of shear strength due to cohesion and friction is given, by a graph of principal stress ratio versus confining pressure in Figure 6-8. When compared to unfrozen Ottawa sand values obtained from Lee and Seed (1967) it is apparent that for low values of confining pressure, the shear strength of frozen sand is primarily nonfrictional and dependent on the strength of the ice matrix. As the confining pressure increases, the principal stress ratio for sand-ice decreases and approaches the value for unfrozen sand. However, even at high confining pressure, there is a small component of strength due to the ice matrix. This plot also gives an indication of the shape of the failure envelope since decreasing values of the principal stress ratio with increasing confining pressure correspond to a progressive flatting of Mohr's envelope.

If the same results are plotted on logarithmic scales as shown in Figure 6-9, a bilinear relationship occurs with the area of transition in the region between 100-200 psi confining pressure. Later sections show that creep test results give a similar change in behavior for these pressure ranges.

Another effect of confining pressure on the stress-strain characteristics of a sand-ice sample is an increase in axial strain at failure. Axial strain at failure is plotted against the confining pressure in Figure 6-10. The data shows that as confining pressure increases the strain at failure also increases. This behavior is similar to sands as reported by Vesic and Clough (1968), and Lee and Seed (1967). However, when compared to unfrozen sands, the strains at failure are substantially less for sand-ice materials. For reduced ice content samples, there is also an increase in strain at failure with increasing confining pressure, but the strain at failure has decreased compared to the results for high ice content samples.

# 6.1.5 Failure Criteria

Using the Mohr-Coulomb theory to describe the time dependent strength of sand-ice materials, the results of the constant strain rate tests are summarized by the p-q diagram shown in Figure 6-11. Data for unfrozen sand (Lee

and Seed, 1967) are also plotted as an aid in comparing the results and identifying the components of strength. the ordinate to the unfrozen  $K_f$  failure line is considered to be caused by sliding friction, dilatancy, and particle crushing; the remaining distance to the sand-ice failure line must be attributed to the ice matrix. What is of interest is the consistency of this value regardless of the value of the normal stress. Over the entire range of confining pressure this component varies from only 330-260 psi. This implies that confining pressure has no significant effect on the component of strength due to the ice matrix. If the results of the constant axial strain rate tests on polycrystalline ice are used, the values of calculated q are nearly the same as the value of the cohesive component shown in the p-q diagram for the sand-ice material. Since the value of the cohesive component is nearly constant, it may be concluded that the ice matrix applies a pseudoconfining pressure analogous to a higher effective stress that is also nearly constant. The magnitude of this pressure may be obtained by evaluating the horizontal stress increment obtained by projecting a line from a point on the sand-ice  $K_f$  failure line to a point on the unfrozen sand K<sub>f</sub> failure line. For high ice content samples this value is approximately 600 psi.

When the angle of inclination of the  $\mathrm{K}_\mathrm{f}$  failure line in the p-q diagram is measured, it decreases slightly with increasing values of normal stress but is approximately 26 degrees. This gives an angle of 29.2 degrees on the failure plane. This value is low when compared to the friction angle for unfrozen sands, which are typically 37-45 degrees depending on the initial void ratio. However, the friction angle for unfrozen sands at high confining pressures is less than the value at low confining pressures. Lee and Seed (1967) obtained a value of approximately 30 degrees for high confining pressure tests on Ottawa sand with an initial void ratio of 0.49. For unfrozen sands the reduction in the angle of friction is due to a decrease in the dilatancy component of strength as confining pressure increases. The same effect is produced in sand-ice materials by the combination of the applied confining pressure and the pseudo-confining pressure caused by the ice matrix. If sand-ice samples with a different initial void ratio were plotted, the result would be a downward displacement of the failure envelope as the void ratio increased. This does not mean that the cohesive component will decrease, since the failure plane for unfrozen sand will also be displaced. The result shown previously on the effect of void ratio indicated that at high confining pressures, the change in strength per increase in void ratio is constant and not dependent on the ice matrix.

Also shown on the p-q diagram (Figure 6-11) are the results of the constant strain rate tests on reduced ice content samples. The observations for these samples are similar to those for the high ice content discussed above. Again it is apparent that at failure a full frictional component is mobilized and the reduction in strength is due entirely to a reduction in the cohesive component.

The net result is that sand-ice materials tested to failure has strength characteristics that can be divided into a cohesive component due to the ice matrix and a component due to friction. It has been shown that the frictional component can be related to the behavior of unfrozen sands at high confining pressure. The cohesive component is the part of strength which will be most responsive to variable test conditions and controls the time dependent characteristics of the shear strength. In addition, the cohesive component of strength is dependent on the percent of ice in the sample and for given conditions of temperature and strain rate is nearly constant at failure.

### 6.2 Creep Behavior

In order to describe the creep behavior of sandice materials for various stress levels, it is necessary to determine the effect of confining pressure on creep. This section presents the results of uniaxial, confined and step-stress creep tests on high and reduced ice content samples for confining pressures up to 1000 psi.

Throughout this section constant deviator stress will be shown as a function of the peak deviator stress obtained from the constant axial strain rate tests. The term M will be used to describe this relationship, where M is equal to the ratio of constant deviator stress for the creep test divided by the peak deviator stress from the constant strain rate test conducted at a similar confining pressure. For example if the creep test conditions are:

constant deviator stress,  $(\sigma_1^{-\sigma_3}) = 1070$  psi confining pressure,  $\sigma_3 = 350$  psi volume of sand, = 63.6% ice content, = 100%

Then from Figure 6-3 the maximum deviator stress would be equal to 2360 psi and

$$M = \frac{1070}{2360} \text{ psi}_{psi} \times 100 = 45.5\%$$

Values of M for all creep tests have been calculated and are shown in Table 5-3 and 5-4.

## 6.2.1 High Ice Content

To show the effect of applied stress on the creep behavior of sand-ice materials at high ice contents, the results of uniaxial creep tests conducted at 400, 640, 750 and 1070 psi are plotted as a logarithm of strain rate versus strain in Figure 6-12. The near linear relationship for each stress level indicates that for the time of load application for these tests, the creep strains are small and the strain rates are decreasing at a constant logarithmic These tests have not reached the steady state region of a typical creep curve since this would require a horizontal segment of the strain rate versus time curves. The low values of strain also imply that this should be a region of little volume change. The actual values of volume change that were measured at the end of each test are noted on the figures. Through 750 psi the volume decreased as would be expected for low values of strain. Goughnour (1968) made volumetric measurements during uniaxial creep tests and constant strain rates tests, and demonstrated that an increase in volume will be associated with the matrix yield which is required prior to the mobilization of the dilatancy component of friction. Thus, for the stress levels applied in this series the creep behavior is primarily dependent on the ice matrix and the component of friction associated with solid to solid contacts. Any attempt to

determine an effective angle of friction within this region as proposed by AlNouri (1969) should result in low values since the loads applied are not great enough to mobilize the full frictional value of the sand particles, and the component due to interlocking of the particles.

The effect of confining pressure on a constant deviator stress creep test is to increase the slope of the line of strain rate versus strain as indicated in Figure 6-13. This supports the observation by Andersland and AlNouri (1970) that strain rate decreases with increased mean stress. This may be explained by noting that an increase in confining pressure increases the level of normal stress applied to the sample. Part of this increase is carried directly by particle to particle contact and part is carried by particle to ice contact. When the p-q values for typical sand-ice tests are calculated, the results may be plotted as shown in Figure 6-14. It can be seen that for the unconfined samples, a large portion of the total applied stress must be carried by the ice matrix (F). As confining pressure is applied to the system the stress circle moves to the right and the shear strength required of the ice will be less (G), and the strain rate will decrease, since creep is primarily a function of the shear stress applied to the ice matrix. This mechanistic

picture of creep assumes that the frictional component of strength due to sliding friction is mobilized during the application of the axial stress. For a dense material prepared in the manner described herein, it appears reasonable that this be the case, since the packing is such that grain to grain contact is assured. In order for a sample to proceed to failure, it would be necessary for the Mohr's circle for the test condition to become tangent to the failure plane for the frozen soil. This may occur, since the cohesive component of strength decreases with time causing a downward displacement of the failure envelope. A comparable reduction in strength occurs in overconsolidated clays at large strains. For sand-ice materials time serves the same purpose as the large strains required for the clays.

Step-stress tests have been used (AlNouri, 1969) as a method of determining the steady state creep rate at different levels of confining pressure. When using this method of testing, the axial load is held constant and the major and minor principal stresses are changed by an amount equal to the change in confining pressure. Since the principal stresses are changed by equal amounts, the deviator stress is held constant. With step-stress testing it is assumed that the sample structure remains

the same prior to and immediately after changing the confining pressure and any changes in the creep rate are due only to the change in confining pressure.

The results for step-stress creep tests plotted as logarithm of strain rate versus strain for three levels of constant deviator stress are shown in Figures 6-15 to 6-17. In these tests each new increment of confining pressure causes an increase in the slope of the curves.

As noted in Figure 6-12, a decrease in axial stress produced a similar increase in slope. For the step-stress tests the deviator stress was constant and the confining pressures were altered. Therefore, increasing the confining pressure has the same effect as decreasing the applied stress for a uniaxial test.

As each increment of confining pressure was applied, the strain rate increased. Then follows a period of decreasing strain rate until the next increment of pressure was applied. The initial increase in strain rate was dependent upon the deviator stress and the strain of the sample. At low stresses the samples show the greatest change in strain rates due to confining pressure. This is an indication of the greater structural dependency of the system at lower stresses. At low deviator stress levels the strain that took place during an increment of confining pressure was small and the structure remains nearly constant. When

the next increment of confining pressure was applied, the deviator stress and structure were nearly the same as for the previous increment and the initial response of the material was the same.

The step-stress creep tests involved increments of confining pressures applied at one hour intervals. To give an idea of the time effect on the strain rate, a sample with a constant deviator stress of 1070 psi was tested with zero confining pressure for three hours and then a confining pressure of 350 psi was applied for three hours. The logarithm of strain rate versus strain in Figure 6-18 demonstrates that time does not alter the basic characteristics of the curve and a decrease in strain rate takes place in a manner similar to the tests with confining pressures applied at one hour intervals.

The results of the step-stress creep tests are summarized in Figure 6-19. Andersland and AlNouri (1970) demonstrated that when the logarithm of secondary creep rate was plotted against a stress factor,  $\Sigma$ , a straight line relationship appeared for confining pressures up to 150 psi and time increments of one-half hour. The data summarized in Figure 6-19 indicate that the relationship predicted by Andersland and AlNouri (1970) are correct for low confining pressures. However, for confining pressure in excess of 200 psi the strain rates predicted

by their equation are substantially less than those indicated by the experimental results.

In addition to the increase in strain rate at higher confining pressure, it appears that the equation used by Andersland and AlNouri (1970) is dependent upon the time interval at which the strain rates are obtained. The equation can be changed to reflect this by making the intercept term a function of time as shown below:

$$\dot{\varepsilon} = b(t) \exp(m\Sigma) \tag{6-1}$$

where  $\Sigma$  = stress factor = D- $\sigma_{m}$ 

m = absolute value of the slope of the line

b = time dependent intercept on the Σ axis

Figure 6-19 also indicates that strain rate is most

responsive to changes in confining pressure for the range
of 0-200 psi. Above 200 psi confining pressure, the strain
rate continues to decrease with increased confining
pressure; however, the change per increment is much smaller
and approaches a constant at the higher levels of confining
pressure. This implies that confining pressure changes the
creep characteristics by a mechanism that is mobilized at
low confining pressure. From these results it appears
that in order to adequately predict strain rates using a
stress factor as described by Andersland and AlNouri (1970),
a bilinear relationship that is a function of time and
confining pressure will be required.

When the results of the step-stress creep tests are summarized as shown in Figure 6-20, the interrelationship between stress difference and confining pressure is more clearly shown. To eliminate time dependency in this presentation, time intervals equal to one hour were selected. Changes in slope for lines of equal confining pressures indicate a definite dependency of strain rate upon the confining pressure. For a given deviator stress the strain rates decrease as the confining pressure increases. The exact functional relationship can be derived empirically since a linear relationship on a semi-log plot has the basic form:

$$\dot{\varepsilon} = b(t) \exp(mD)$$
 (6-2)

Taking logarithms of both sides results in the expression

$$\log \dot{\epsilon} = \log b(t) + (m \log e) D$$
 (6-3)

where (m log e) is the absolute value of the slope of the lines of equal confining pressure and b is the intercept on the ordinate. To determine the relationship between the slope, m, and the value of confining pressure, m is plotted against confining pressures as shown in Figure 6-21. The results of this graph exhibit a bilinear relationship of slope versus confining pressure. From this figure the equation for the slope m as a function of confining pressure is:

$$m_i = C_i + G_i \sigma_3 \tag{6-4}$$

where  $m_i$  = value of slope for the line of equal confining pressure.

i = 1, for confining pressure equal to or less than
200 psi.

i = 2, for confining pressure greater than 200 psi.

G<sub>i</sub> = slope of the i<sup>th</sup> segment of the m versus
 confining pressure graph.

Combining this expression with the equation 6-3 results in the following expressions:

$$\log \dot{\varepsilon} = \log b(t) + [(C_i + G_i \sigma_3) \log e D]$$
 (6-5)

$$\dot{\varepsilon} = b(t) \exp \left[ (C_i + G_i \sigma_3) D \right]$$
 (6-6)

$$\dot{\varepsilon} = b(t) \exp (C_i D) \exp (G_i \sigma_3 D)$$
 (6-7)

Equation 6-7 is of the same form as that describing the rate process theory. For the range of confining pressures studied (up to 1000 psi) an equation can be derived to describe the strain rate of a sand-ice sample. Using equation 6-7, the coefficient C<sub>i</sub> and G<sub>i</sub> must be determined for the appropriate ranges of confining pressure. From Figure 6-21, when confining pressure is equal to or less than 200 psi

$$m_1 = C_1 + G_1 \sigma_3 \tag{6-8}$$

where 
$$C_1 = 2.97 \times 10^{-3} \text{ min}^{-1}/\text{psi}$$
  
 $G_1 = -6.04 \times 10^{-6} \text{ min}^{-1}/\text{psi}$ 

likewise for confining pressures greater than 200 psi

$$m_2 = C_2 + G_2 \sigma_3$$
 (6-9)

where 
$$C_2 = 1.98 \times 10^{-3} \text{ min}^{-1}/\text{psi}$$
  
 $G_2 = -1.03 \times 10^{-6} \text{ min}^{-1}/\text{psi}$ 

The resulting equation for the entire range of confining pressures is:

$$\dot{\varepsilon} = b(+) \exp(C_i D) \exp(G_i \sigma_3 D)$$
 (6-10)

when

$$\sigma_3 \le 200 \text{ psi}$$
 b(60) = 4.7 x 10<sup>-6</sup> min<sup>-1</sup>
 $C_1 = 2.97 \text{ x } 10^{-3} \text{ min}^{-1}/\text{psi}$ 
 $G_1 = -6.04 \text{ x } 10^{-6} \text{ min}^{-1}/\text{psi}$ 
 $\sigma_3 > 200$  b(60) = 4.7 x 10<sup>-6</sup> min<sup>-1</sup>
 $C_2 = 1.98 \text{ x } 10^{-3} \text{ min}^{-1}/\text{psi}$ 
 $G_3 = -1.03 \text{ x } 10^{-6} \text{ min}^{-1}/\text{psi}$ 

The bilinear relationship noted for this equation may be explained for a sample at low confining pressures. When the sample is loaded instantaneously, numerous microcracks form at the sand-ice interface because some of the sand grains apply stresses to the ice in excess of the instantaneous ice crystal strength. Increased confining pressure prevents the cracks from forming, resulting in a more homogeneous material with greater strength and lower creep rates. Equation 6-10 shows that strain rates are most responsive to confining pressures below 200 psi. The term b(t) in the equation has no physical significance but is an indication of the minimum strain rate that will be encountered in the range for which the equation is applicable.

The previous discussion has indicated that given the results of step-stress creep tests, a family of curves may be constructed that will allow the calculation of strain rates for various combinations of confining pressures and deviator stress. This method has the disadvantage of being time dependent. It would be much more helpful if the creep characteristics of the sand-ice material could be obtained independent of time.

It was observed that the strain rate decreases in an exponential fashion either after the initial application of the deviator stress (uniaxial tests, Figure 6-12) or

after the application of increments of confining pressure (Figures 6-15, 6-16, and 6-17). If the slopes of these lines are calculated and are plotted versus the percent of maximum deviator stress M as shown in Figure 6-22, a band of points is obtained. Using the results of this graph it is possible to approximate the decrease in strain rate for any test condition as long as the initial elastic strains and the percent of maximum deviator stress are known. The curvature of the graph as M approaches zero is an indication that the response of the sand-ice materials to low levels of applied stress is different and the approximation would not be valid in this region. On the other end of the scale it is expected that the curve would be nonlinear as M approached 100 percent. From the data shown here, a range of 20-75 percent of the maximum deviator stress can be used for the approximation. For samples that progress to failure, the strain rate versus strain graph exhibits an initial linear portion followed by an upward curvature as the sample approaches the beginning of the tertiary region of creep. The results shown in Figure 6-22 can be used only to describe the linear portion of the curve.

#### 6.2.2 Reduced Ice Content

Since creep is related to the strength of a material, it would be expected that for a given constant axial stress

and void ratio, reduced ice content samples would have greater creep response than high ice content samples.

In Figure 6-23, the results of uniaxial creep tests at 400, 640 and 750 psi are shown. It is apparent that these samples, as with the high ice content samples, exhibit typical strain rate versus strain characteristics. For the low level of axial stress (400 psi), the sample exhibits linear characteristic for the entire duration of the test. At higher levels of axial stress (750 psi) the sample has not only an initial linear portion, but also a segment of increasing strain rate. This is the type of behavior that would be expected of a sample that progresses to failure. The intermediate level of axial stress (640 psi) exhibits the initial linear portion and a small region of decreasing strain rate. These curves indicate that reducing the ice content does not alter the basic characteristics of the creep and any differences between high and low ice content samples are in magnitude only.

If the applied deviator stress is related to the maximum shear strength of sand-ice samples for reduced ice content (as was done for the high ice content samples in the previous section) it is possible to define the term M, percent of maximum deviator stress, for the reduced ice content samples. In order to generalize the use of this term, it is necessary to show the relationship between the percent of maximum deviator stress for high and

reduced ice contents. It can be shown intuitively, that for any given percent of maximum deviator stress, the shear stress carried by the ice is constant and the response of the system will be essentially constant.

Considering any failure plane with a shear force resulting from the applied force, then:

$$\tau_{\rm H} = \frac{P_{\rm H}}{A_{\rm HI} + A_{\rm HS}}$$
 and  $\tau_{\rm L} = \frac{P_{\rm L}}{A_{\rm LI} + A_{\rm LS}}$  (6-11)

where  $\tau_{H}^{}$  = shear stress resulting from applied load on high ice content samples

 $\tau_L$  = shear stress resulting from applied load on low ice content samples

 $P_{H}$  = force causing shear for high ice content samples

 $P_{T}$  = force causing shear for low ice content samples

 $A_{HT}$  = area of ice, high ice content

 $A_{T,T}$  = area of ice, low ice content

A<sub>HS</sub> = area of sand, high ice content sample

 $A_{LS}$  = area of sand, low ice content sample

For a constant percent of maximum deviator stress

$$M_{H} = M_{T}$$

where M<sub>H</sub> = percent of maximum deviator stress high ice content sample

Assuming that the shear forces are proportional to the applied loads:

$$P_H = P_{H \text{ max}} \times M_{H} \text{ and } P_L = P_{L \text{ max}} \times M_{L}$$

with P<sub>H max</sub> = maximum shear force resulting from the maximum deviator stress high ice content

P<sub>L max</sub> = maximum shear force resulting from the maximum deviator stress low ice content

For any given sample, let j equal the ice content expressed as a decimal fraction. Then the area of ice is proportional to the ice content in the sample, and

$$A_{HI} = \frac{A_{LI}}{j} \tag{6-12}$$

Since P max is proportional to the maximum applied loads, and the maximum applied loads are proportional to the ice content of the sample, as shown in Figure 6-5

$$P_{H \text{ max}} = \frac{P_{L \text{ max}}}{j}$$

Using the Adhesion Theory of Friction (Lambe and Whitman, 1969), which states that an increase in normal loads must mean a proportional increase in area of contact between two bodies, the area of sand contact is:

$$A_{HS} = \frac{A_{LS}}{j}$$

Substituting these relationships into equation 6-11 and solving:

$$\tau_{H} = \frac{P_{L} \max_{H}^{M}}{(A_{LI} + A_{LS})}$$
 (6-13)

and

$$\tau_{L} = \frac{P_{L} \max^{M} L}{(A_{LI} + A_{LS})}$$
 (6-14)

but,

$$M_{H} = M_{L}$$

and, therefore

$$\tau_{\rm H} = \tau_{\rm L}$$

The above proof obviously is not rigorous because of the assumptions regarding the distribution of forces and the increase in area due to the applied loads. However, the proof is useful for supporting the initial assumption that given a percent of maximum deviator stress, the resulting creep characteristics should be the same. Using this fact, the results from the tests on the reduced ice content samples are presented in a fashion similar to the high ice content samples.

A plot of strain rate versus strain for the various ice contents is shown in Figure 6-24. This figure demonstrates the invariance of creep behavior with respect to ice content. As an additional indication of the effect of various percents of ice, an intermediate percentage of ice of 70 percent has been included. At the applied axial stress of 750 psi the three different ice contents produce curves similar to those obtained by increasing the axial stress and holding the percent ice constant as was shown in Figure 6-23.

As with the high ice content, there was a test in which the sample was subjected to high confining pressure for the entire test period. The results of test plotted as strain rate versus strain in Figure 6-25 shows that the effect of confining pressure is immediately apparent. The confined sample has a steadily decreasing strain rate through the entire test and has undergone much less strain than the unconfined sample. The substantial increase in slope of the curves as the percent of maximum deviator stress was reduced from 71 percent to 34 percent is apparent.

The results of the step-stress creep tests on reduced ice content samples shown in Figures 6-26 to 6-28 include three levels of deviator stress used for the high ice content samples. The increase in slope of the curves with decrease in percent of maximum deviator stress is common to all the step-stress creep tests conducted, and

indicates a definite response to increased confining pressures. Figure 6-28 is particularly interesting in this respect. For the uniaxial test, the sample proceeded into the tertiary range within 45 minutes after application of the axial stress of 750 psi. As the increments of confining pressure were applied, the creep rate decreased and at the end of the test there was no sign of failure, even though the time of the test was 90 minutes. Since the increments of confining pressure were applied at various time intervals, it may be misleading if strain rates obtained from Figure 6-28 are compared to strain rates from the other tests with lower percents of maximum shear stress.

Figure 6-29 is a plot of the stress factor  $\Sigma$  versus strain rate for the reduced ice samples. As with high ice content samples, there is a definite bilinear behavior. Reduced ice content samples are also more responsive to confining pressure in the 0-200 psi range.

In order to describe the creep behavior of reduced ice samples, it is possible to modify equation 6-7 such that the peak deviator stress is a function of the ice content. Therefore, an expression relating the deviator stress for the high and low ice contents can be written:

$$D_{T} = D_{H} f(j)$$
 (6-15)

 $D_{H}$  = Deviator stress high ice content

 $\mbox{\bf D}_{\rm L}$  = Deviator stress low ice content assuming that the function is linear, as shown in Figure 6-5, then:

$$D_{H} = \frac{D_{L}}{J} \qquad \sigma_{3} = constant \qquad (6-16)$$

Substituting this expression into equation 6-7, results in an equation for creep in terms of the applied deviator stress for reduced ice content and the percent of ice.

$$\dot{\varepsilon} = b(t) \exp(C_i \frac{D_L}{j}) \exp(G_i \sigma_3 \frac{D_L}{j})$$
 (6-17)

If the parameters b(t), C<sub>i</sub>, and G<sub>i</sub> are obtained from equation 6-10, it is possible to obtain strain rates for a time interval of one hour. The calculated and experimental results are tabulated in Table 6-1. The data show a good correlation between measured and calculated values and support equation 6-17 for calculating strain rates for reduced ice samples.

Presentation of the creep test results as a function of percent of maximum deviator stress and the slope factor K in Figure 6-30 confirms the trend of increasing K with increasing values of M as was shown for high ice content samples.

content samples it can be stated that the creep characteristics of these samples are essentially the same as for the high ice content samples. If the two test series are related by the factor M, percent of maximum deviator stress, the formulations obtained for high ice content may be used. It is noted that considerable scatter occurs for some of the tests on the reduced ice samples. This scatter was due to difficulty in making duplicate low ice content samples. Even though the same amounts of sand and water were added to each sample, it is probable that the distribution of water in the pore spaces for the unsaturated condition may be different between any two samples, resulting in slightly different ice contents on the plane of maximum shear.

It was originally assumed that a reduction in the percent of ice in a sample would accelerate the creep response so that it would be possible to study a wider range of loading conditions in a shorter amount of time. This has not proven to be the case. Rather, it has been demonstrated that for a given percent of maximum deviator stress the creep characteristics are essentially the same for both the high and low ice content samples. This fact may be useful in conducting experiments on frozen sand-ice materials where limited loading capabilities are available or for the analysis of partially saturated sand-ice systems.

TABLE 6-1.--Calculated versus measured strain rates using Equation 6-17, reduced ice content.

Sample No.	% Ice	DL	Confining Pressure	Calc. Strain Rate Eq 6-17	Measured Strain Rate
	ક	psi	psi	min <sup>-1</sup>	min <sup>-1</sup>
93	60.8	400	0	3.3x10 <sup>-5</sup>	4.2x10 <sup>-5</sup>
97	58.8	640	0	1.10x10 <sup>-5</sup>	1.1x10 <sup>-5</sup>
120	64.6	640	600	$1.7 \times 10^{-5}$	$3.6 \times 10^{-5}$
94	59.4	400	0 100 200 400 600 800 1000	3.5x10 <sup>-5</sup> 2.2x10 <sup>-5</sup> 1.5x10 <sup>-5</sup> 1.3x10 <sup>-5</sup> 1.2x10 <sup>-5</sup> 1.06x10 <sup>-5</sup> .89x10	4.5x10 <sup>-5</sup> 2.5x10 <sup>-5</sup> 1.8x10 <sup>-5</sup> 1.5x10 <sup>-5</sup> 1.3x10 <sup>-5</sup> 1.2x10 <sup>-5</sup> 9x10
98	60.0	640	0 100 200	11.0×10 <sup>-5</sup> 5.7×10 <sup>-5</sup> 3.1×10 <sup>-5</sup>	$9 \times 10^{-5}$ $5.4 \times 10^{-5}$ $2.7 \times 10^{-5}$

Time of Measured Strain Rate = 60 min

Temp. =  $12.0^{\circ}$  C

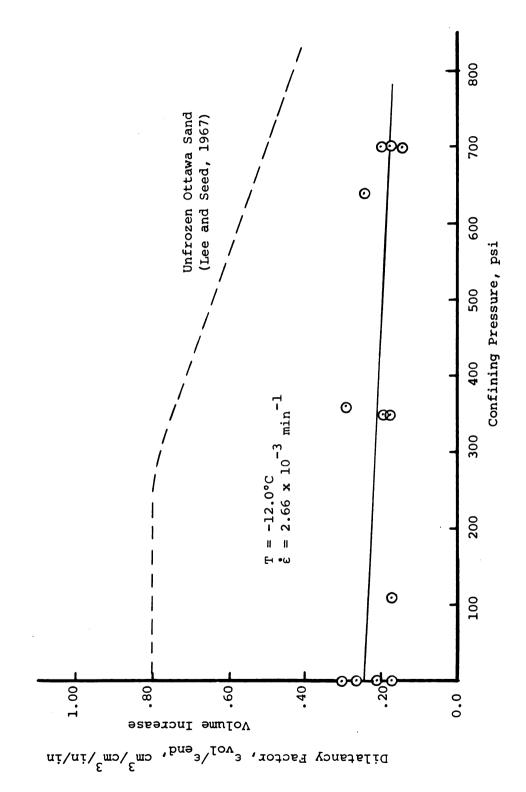


Figure 6-1. -- Effect of confining pressure on volume change.

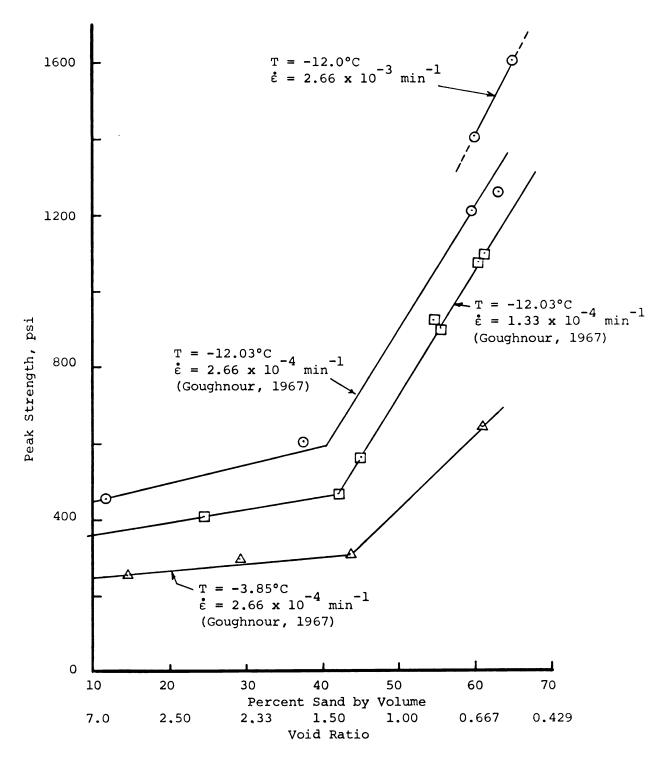


Figure 6-2.--The effect of percent sand, temperature, and strain rate on peak strength.

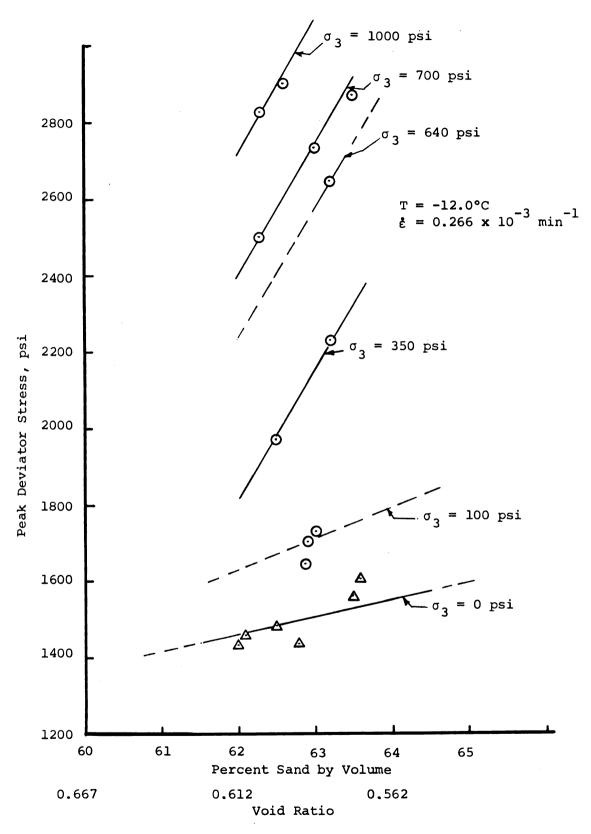


Figure 6-3.--Effect of confining pressure and void ratio on strength

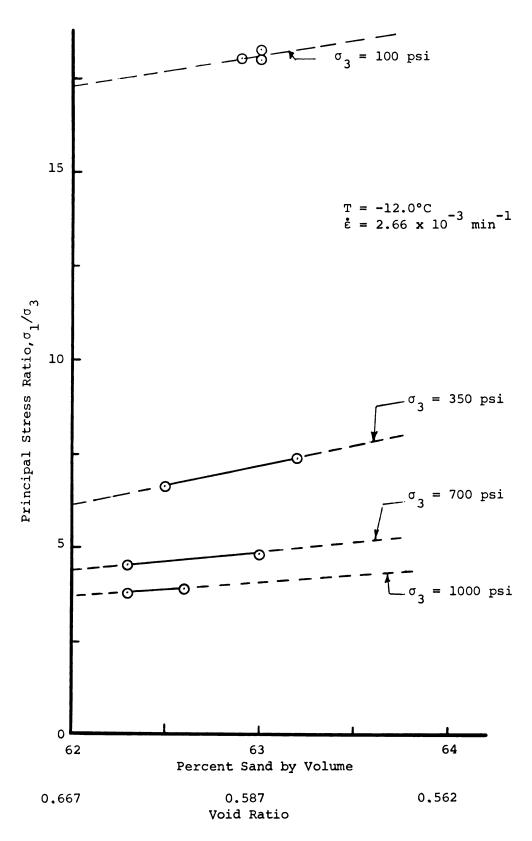


Figure 6-4.--Effect of confining pressure and void ratio on the principal stress ratio

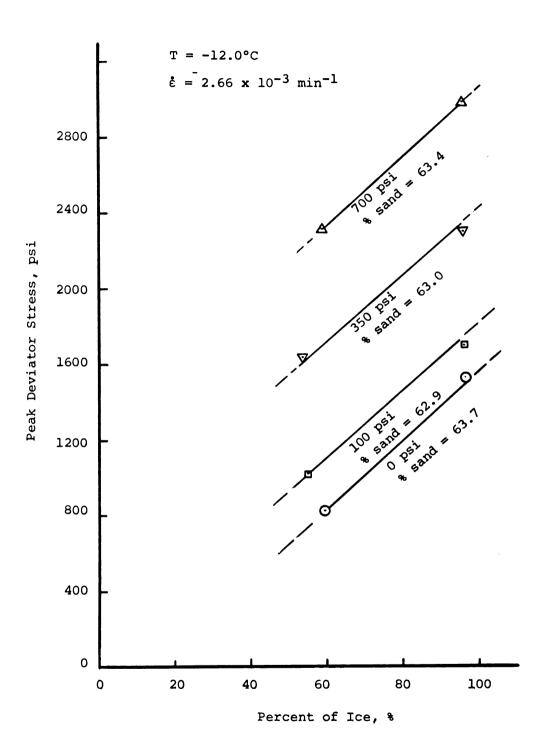


Figure 6-5.--Effect of ice content on strength.

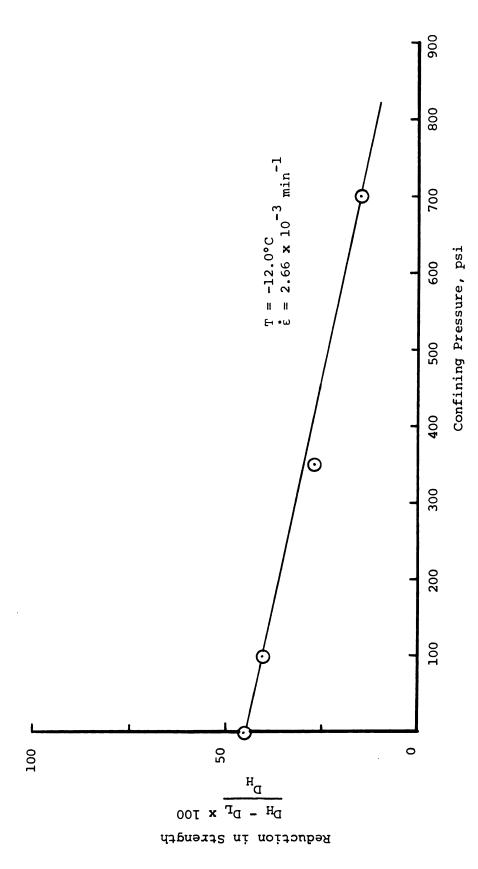


Figure 6-6.--Reduction in strength versus confining pressure.

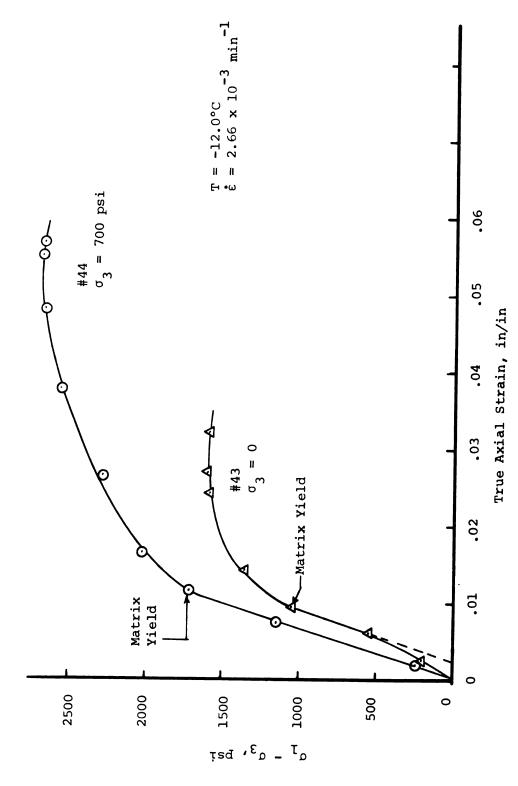


Figure 6-7.--Typical effect of confining pressure on sand-ice.

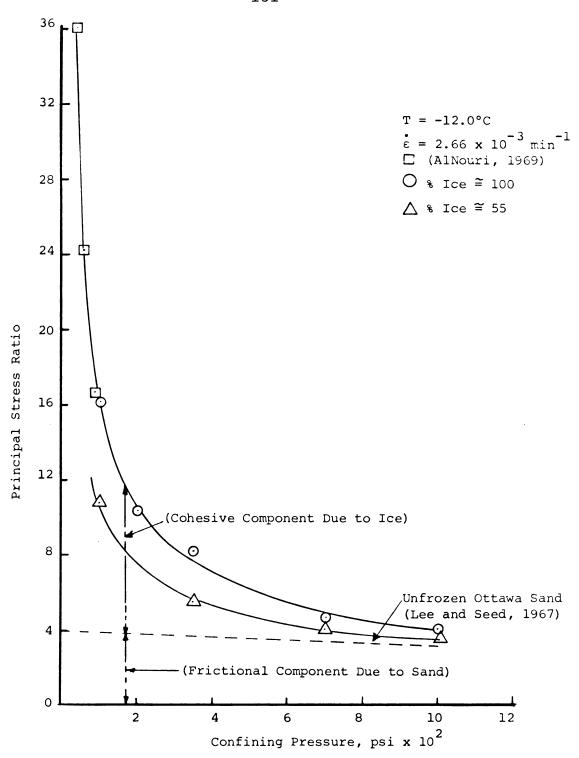


Figure 6-8.--Principal stress ratio versus confining pressure.

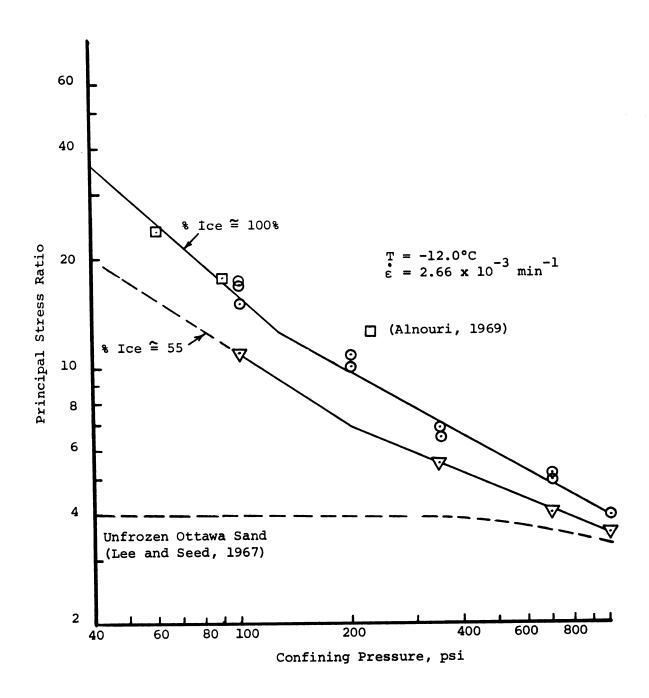


Figure 6-9.--Influence of confining pressure on the principal stress ratio.

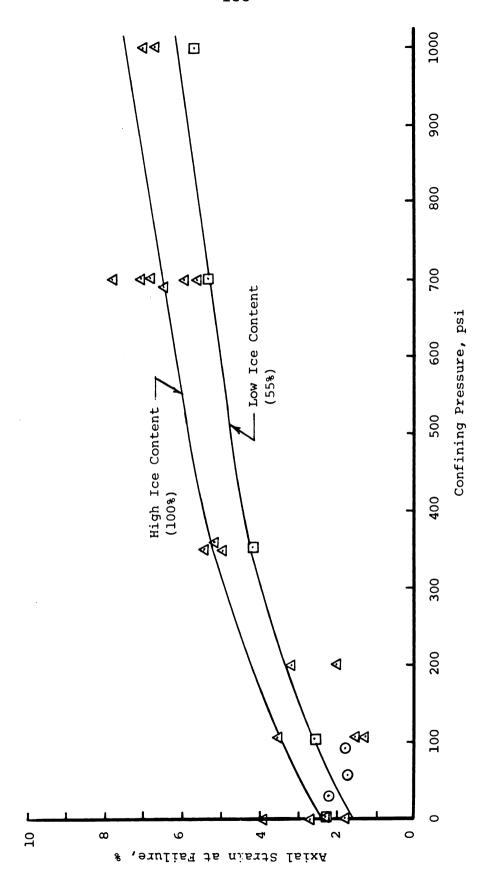


Figure 6-10.--Axial strain at failure for sand-ice samples.

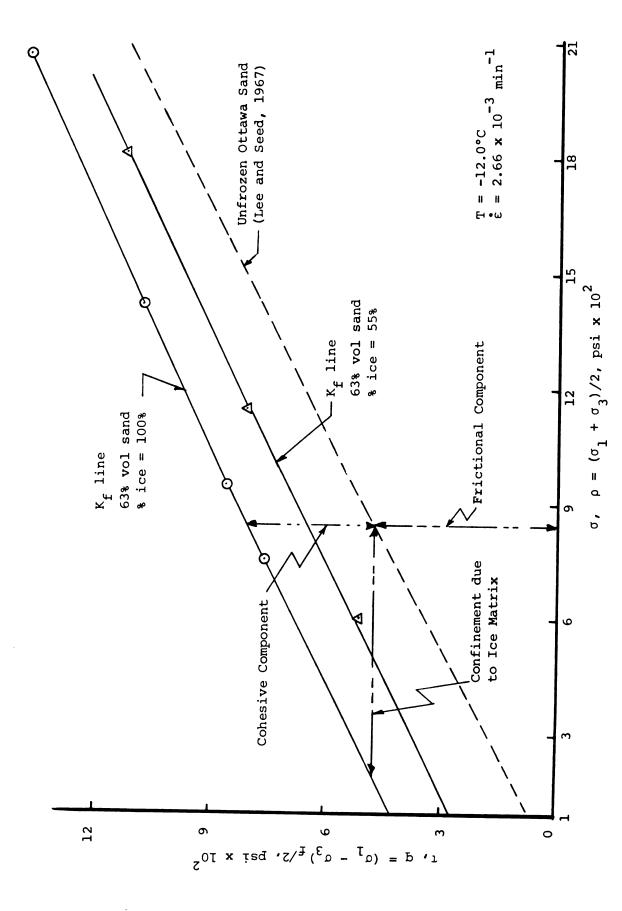


Figure 6-11.--K failure line for sand-ice (typical values).

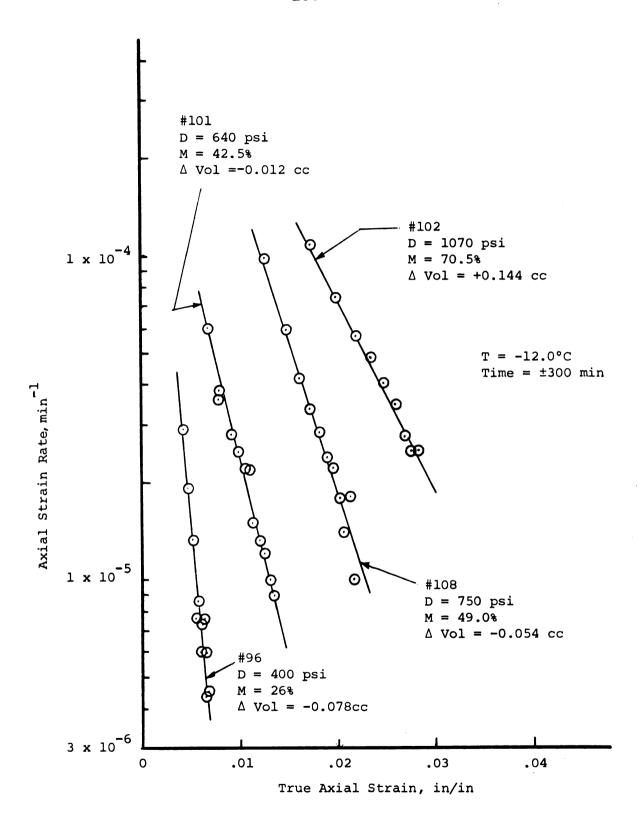


Figure 6-12.--Strain rate versus strain for uniaxial stress creep tests, high ice content.

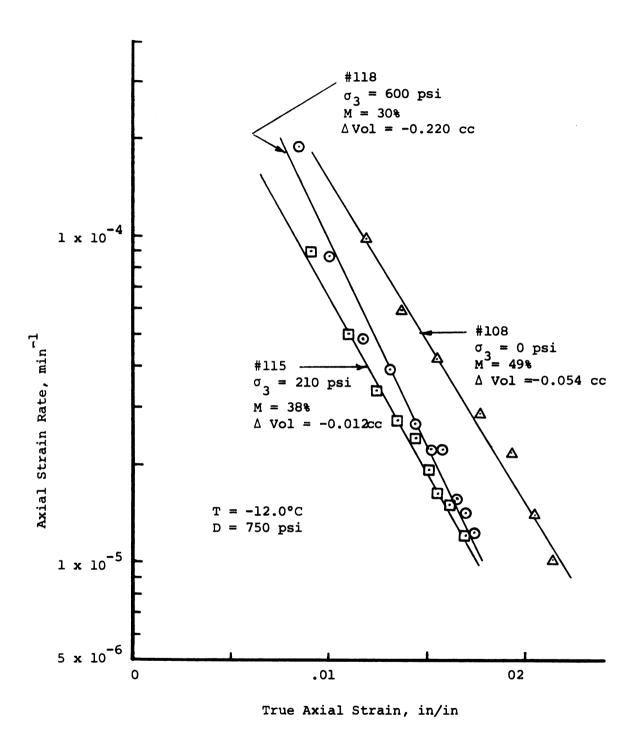


Figure 6-13.--Strain rate versus strain for constant confining pressure test, high ice content.

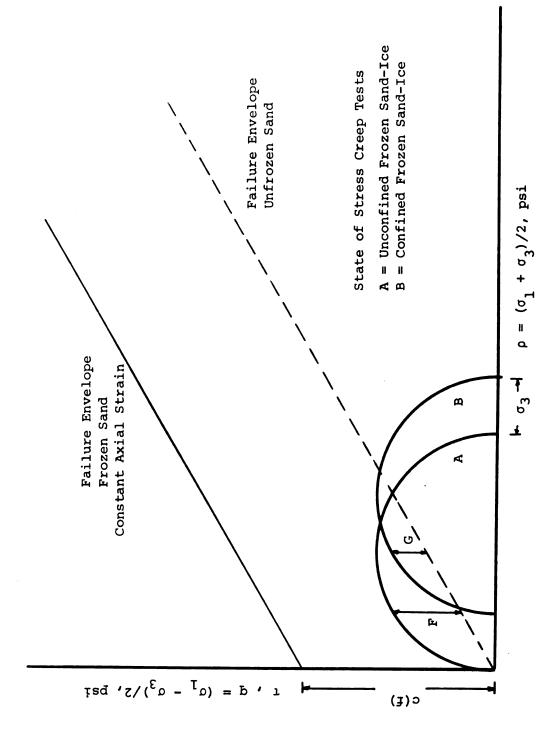


Figure 6-14.--State of stress for uniaxial and confined creep tests.

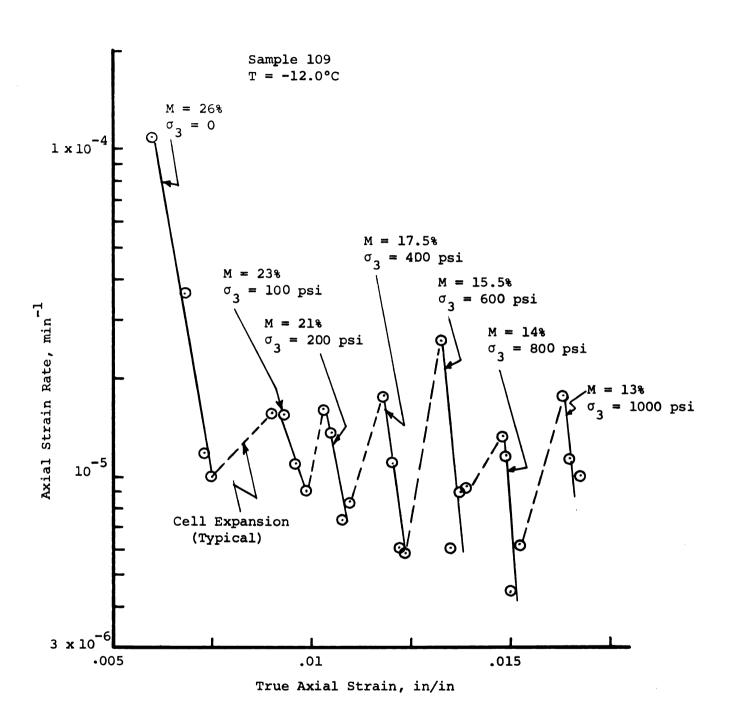


Figure 6-15.--Step-stress creep behavior for a deviator stress of 400 psi, high ice content.

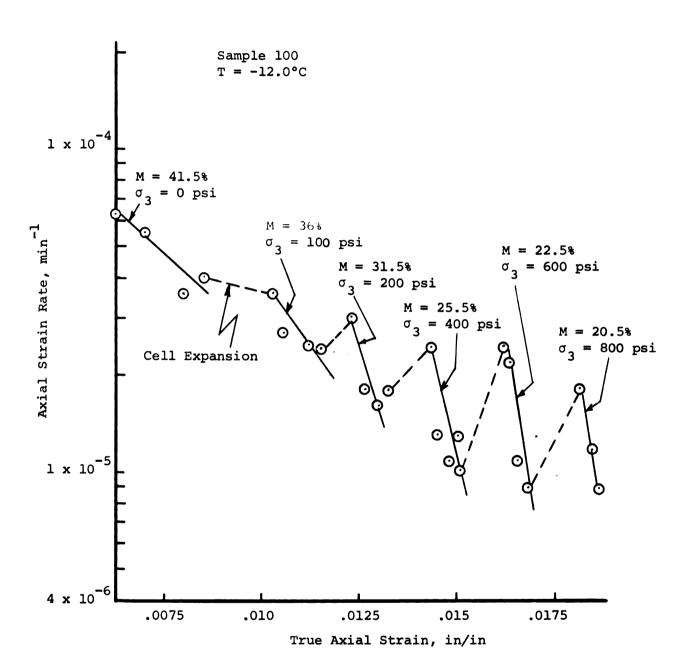


Figure 6-16.--Step-stress creep behavior for a deviator stress of 640 psi, high ice content.

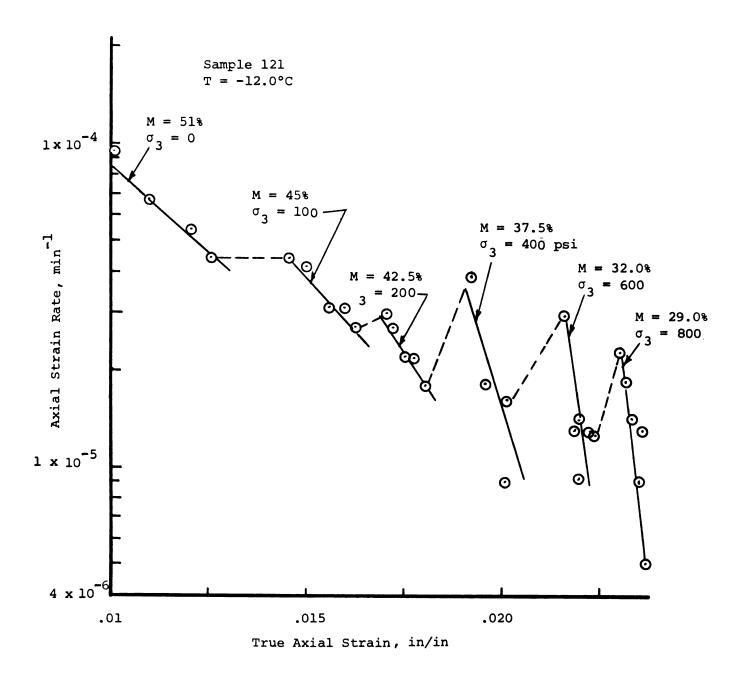


Figure 6-17.--Step-stress creep behavior for a deviator stress of 750 psi, high ice content.

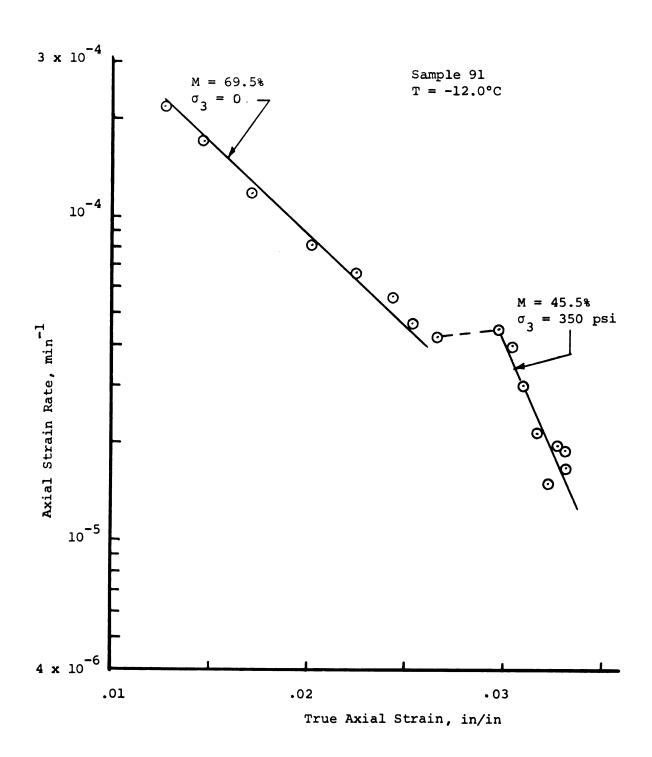


Figure 6-18.--Step-stress creep behavior for a deviator stress of 1070 psi, high ice content.

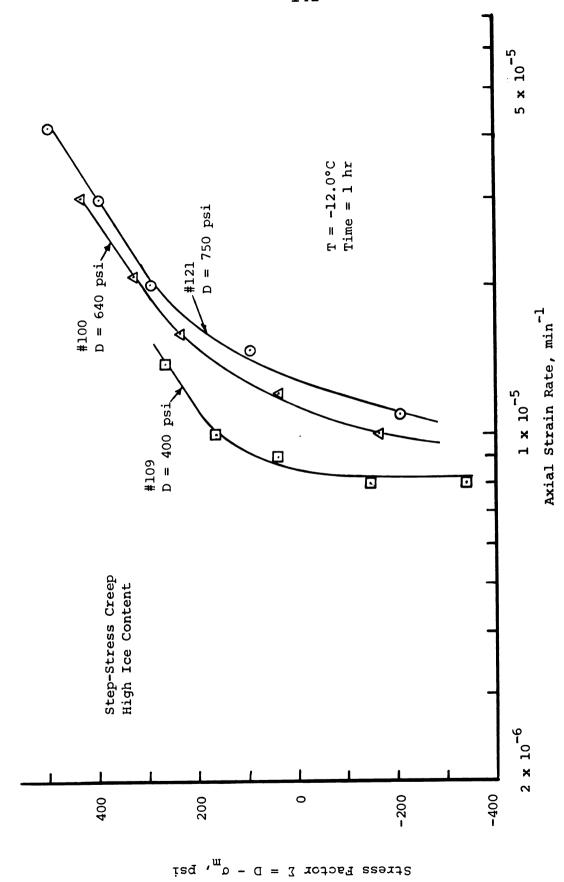


Figure 6-19.--Strain rate versus stress factor  $\Sigma$ .

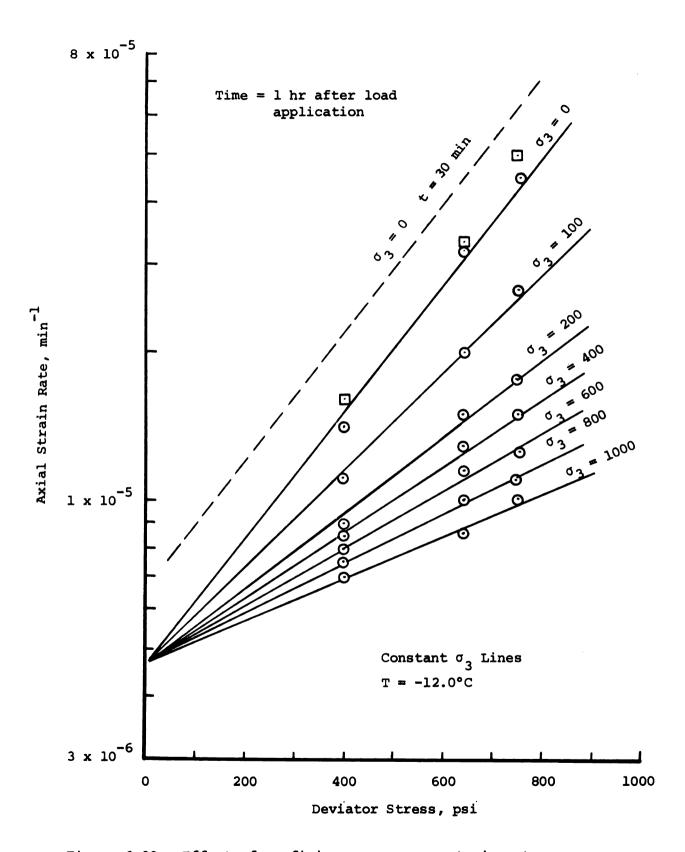


Figure 6-20.--Effect of confining pressure on strain rate.

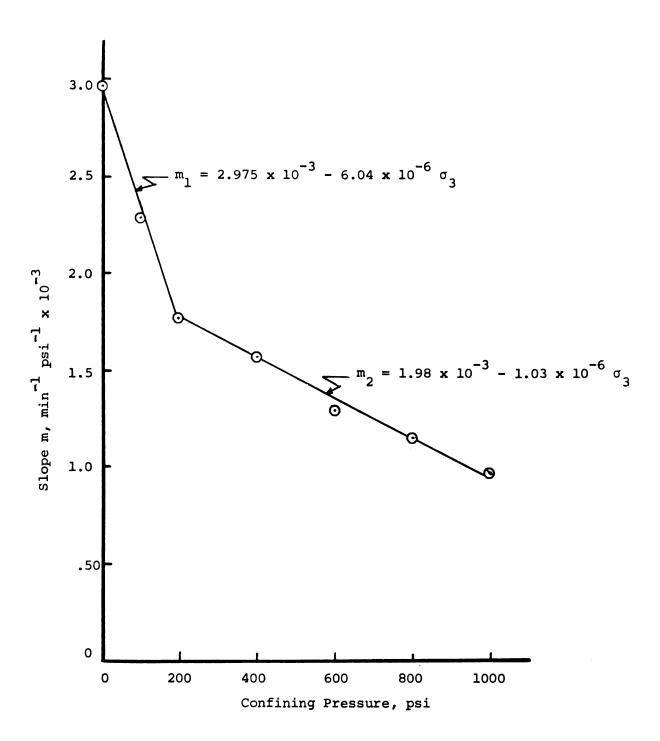


Figure 6-21.--Slope value m versus confining pressure.

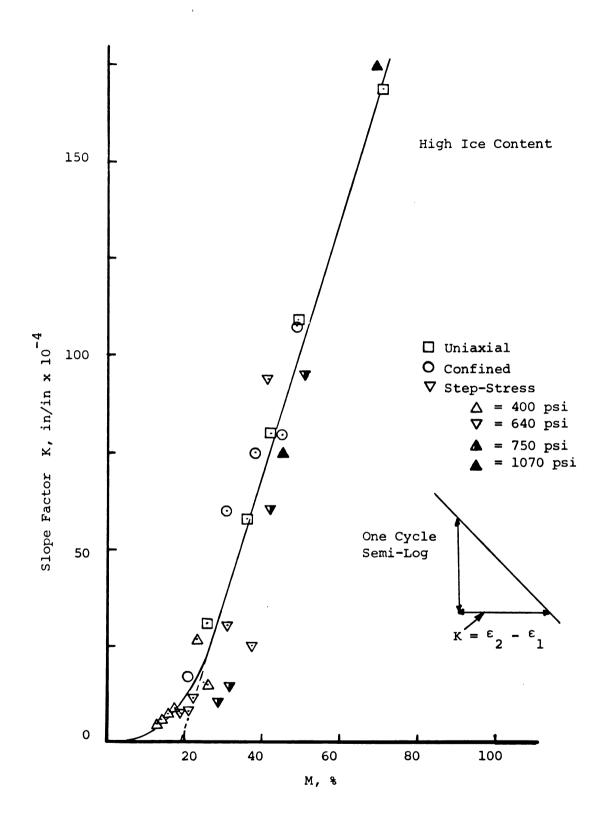


Figure 6-22.--Slope factor K versus percent of maximum deviator stress.

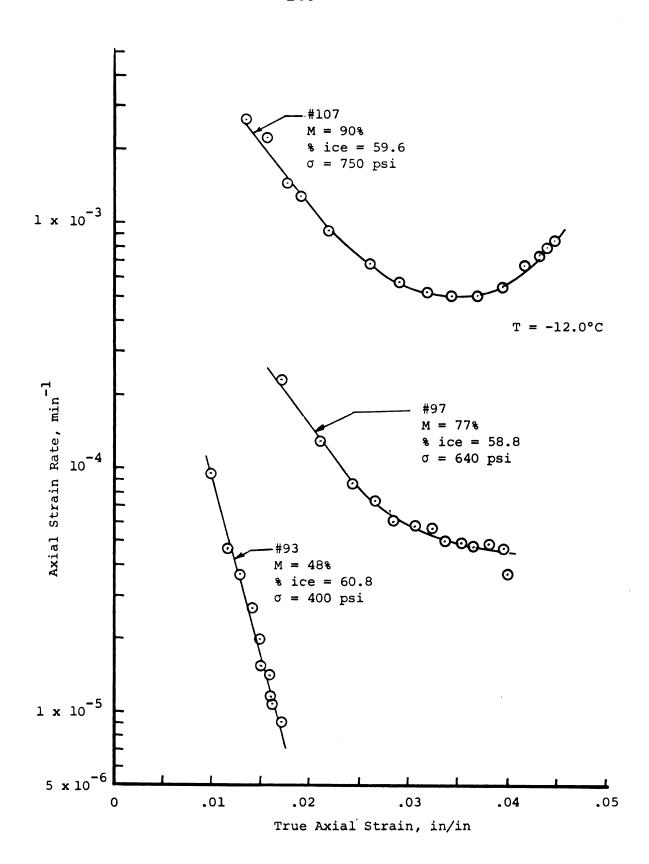


Figure 6-23.--Uniaxial creep test for reduced ice contents.

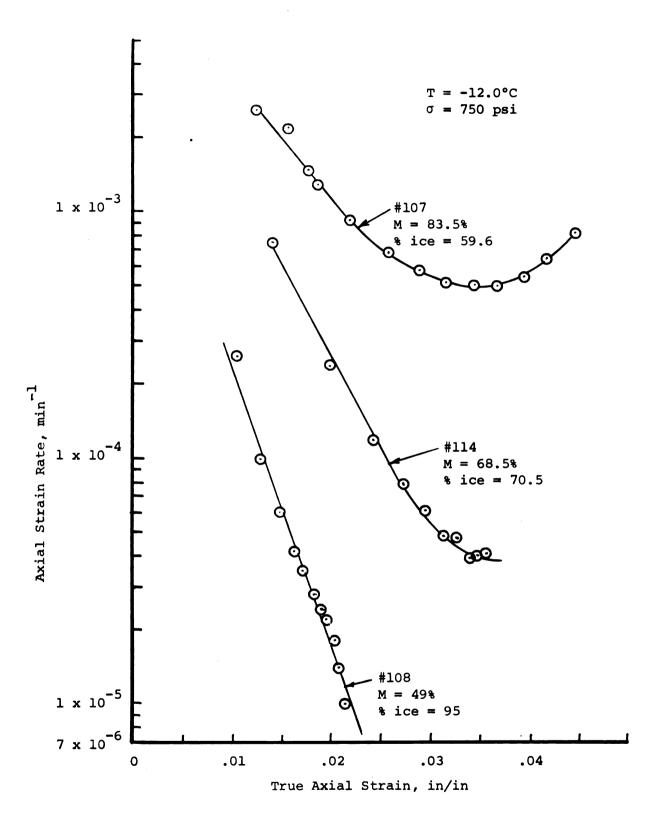


Figure 6-24.--Effect of various levels of ice content on uniaxial creep test behavior.

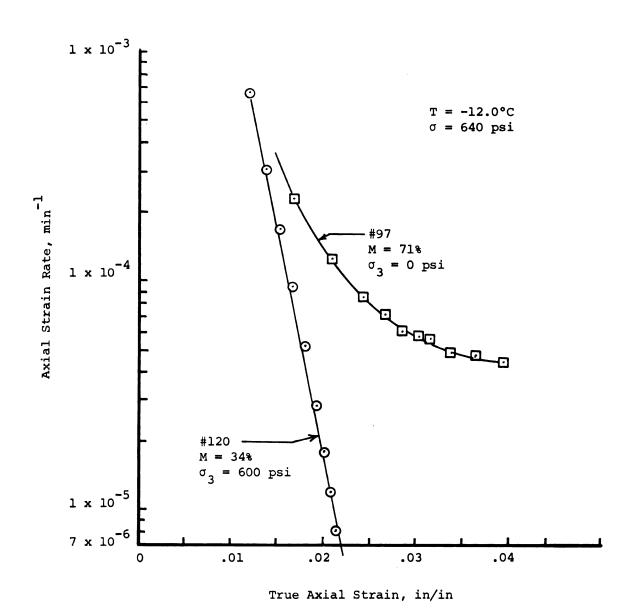


Figure 6-25.--Effect of confining pressure on creep of low ice content samples.

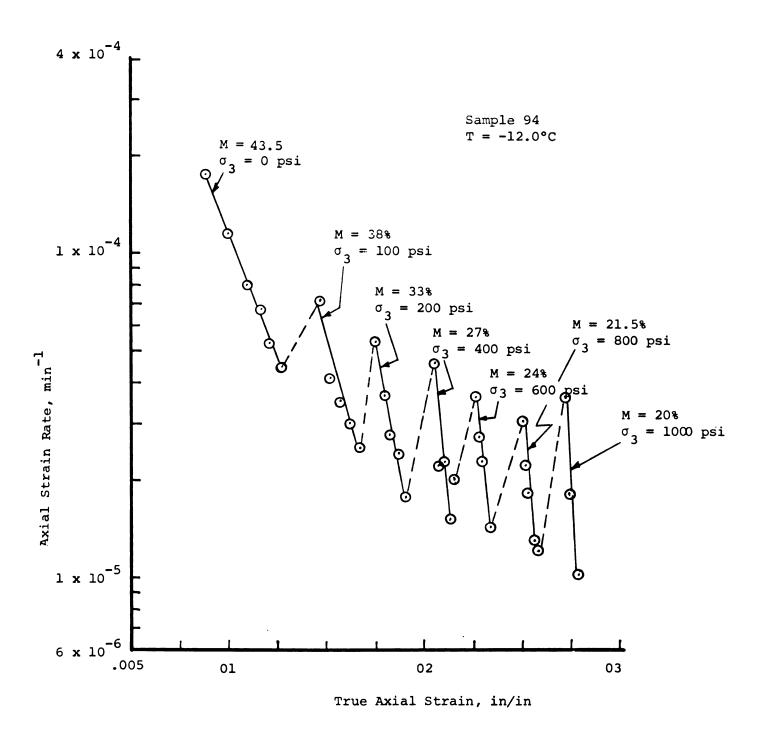


Figure 6-26.--Step-stress creep behavior for deviator stress of 400 psi, low ice content.

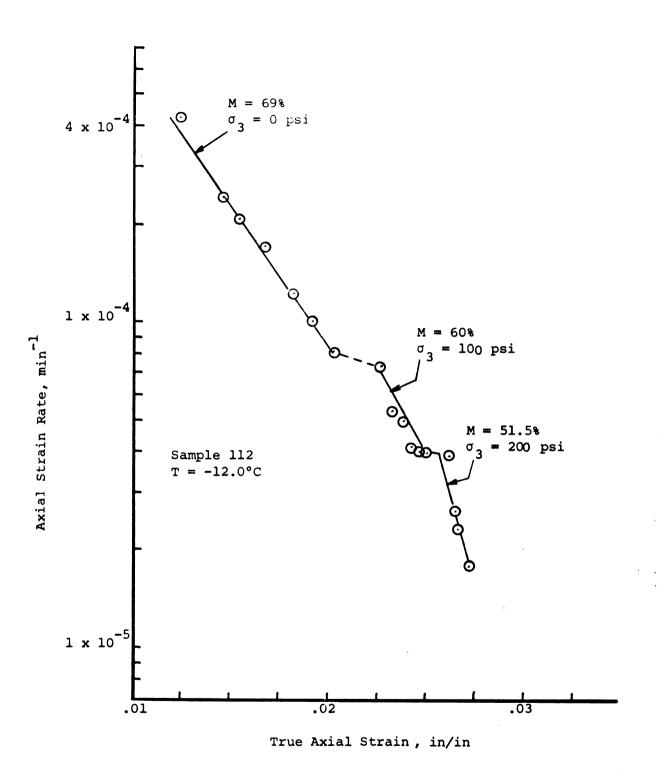


Figure 6-27.--Step-stress creep behavior for a deviator stress of 640 psi, low ice content.

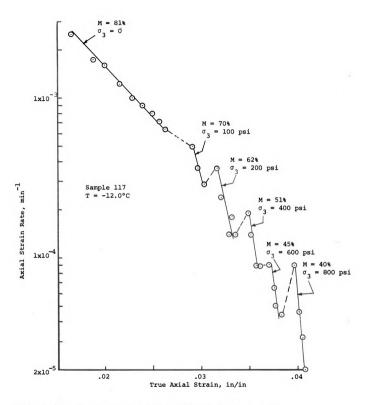


Figure 6-28.--Step-stress creep behavior for a deviator stress of 750 psi, low ice content.

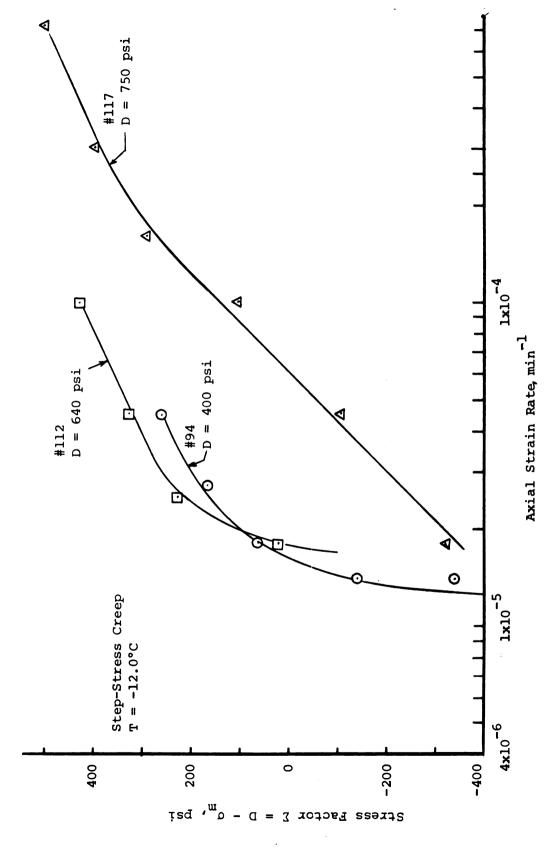


Figure 6-29. -- Strain rate versus stress factor I for low ice content samples.

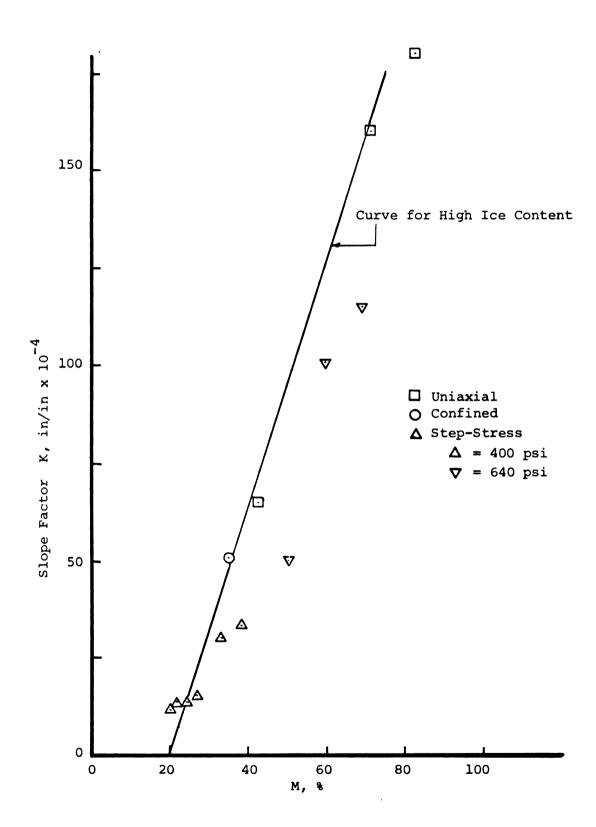


Figure 6-30.--Slope factor K versus percent of maximum deviator stress, low ice content.

### CHAPTER VII

### SUMMARY AND CONCLUSIONS

## 7.1 Shearing Resistance

The shearing resistance of sand-ice materials has been studied in terms of the Mohr-Coulomb failure theory in which the shear strength is a summation of a cohesive term and a frictional term. For a constant temperature, it was shown that the cohesive term is dependent on the ice content and strain rate and is independent of the granular component for the percent sand by volume tested. The frictional component was shown to be dependent upon void ratio and independent of the strain rate and ice content. It was observed that the behavior of a sandice material is dependent on the magnitude of confining pressure applied to the system. For the unconfined test the ice matrix was the primary contributor to the strength of the material and when the ice matrix yielded, the sample progressed to failure. For confining pressures greater than 200 psi the sand-ice samples showed bilinear stressstrain characteristics. The initial portion of the stress-strain curve was attributed to the ice matrix ending at a matrix yield point. The second portion was due to the development of the frictional component of

strength, which was dependent on the void ratio and the amount of confining pressure. It was shown that dilatancy contributes to the frictional strength of the sand-ice samples. When maximum deviator stresses are used to plot Mohr's circles, the failure envelope exhibits a slight curvature as the normal stress increases. Comparisons with unfrozen sand show that the cohesive and frictional components exist over the entire range of applied stresses. The results indicate a system in which the cohesive component depends on the ice matrix and the frictional component has characteristics similar to those for unfrozen sands tested at high confining pressures. The major conclusions regarding the shear resistance of sand-ice materials are as follows:

- 1. Dilatancy occurs in sand-ice samples tested to failure and decreases slightly with increasing confining pressure. The dilatancy of sand-ice is less than for unfrozen sands tested at equal condition.
- 2. A decrease in void ratio (higher density) increases the peak strength for the range of void ratios tested. At higher confining pressures the effect is reduced and the ratio of principal stresses increases only slightly with smaller void ratios.
- 3. Smaller ice contents reduce the peak strength with a linear dependence on the ice content. This relationship is independent of confining pressure.

- 4. High confining pressures produce strength characteristics which are predominantly frictional in nature.
- 5. Failure strains increase as confining pressure increases and decrease slightly with reduced ice content.
- exhibits a slight curvature as normal stress increases, but for engineering design it can be approximated by a straight line. The effective angle of internal friction approximates that for unfrozen sand at high confining pressure. This relationship is independent of the ice content.
- 7. The cohesive component of strength at failure decreased only slightly with increased confining pressure and remains essentially constant for a constant temperature and strain rate.

# 7.2 Creep Behavior

The creep behavior of sand-ice materials was shown to follow "classical" behavior exhibited by other materials such as clays, metals and plastics. By conducting uniaxial creep tests at various levels of constant axial stress, the general creep characteristics of the sand-ice materials were obtained. Using these tests as a basis for comparison, the effects of confining pressure

were obtained using step-stress and confined testing techniques. The experimental results show that increases in confining pressure reduce strain rates. Confining pressures below 200 psi have the greater effect whereas above 200 psi creep rates decreases less rapidly with increased confining pressure. Step-stress testing proved useful in predicting the effects of confining pressure so that creep rate could be calculated as a function of the confining pressure and deviator stress. The expression obtained was defined for regions both above and below 200 psi.

Reduced ice contents have no basic effect on the shape of the creep curves. It was shown that the same equations used for high ice content samples can also be used for the reduced ice content samples when the deviator stress was modified. Finally, it was observed that all creep tests could be related by a term called the percent of maximum deviator stress, M. Tests conducted at equal percents of maximum deviator stress produced similar results and the decrease in strain rate for a particular value of M were the same for both high and reduced ice contents. Conclusions concerning the creep of sand-ice materials include:

1. For a constant deviator stress, strain rate is decreased exponentially by increasing confining

pressure. The high and low stress regions appear to be bounded by the common 200 psi stress level.

- 2. The effect of confining pressure on creep rate is greatest for pressures less than 200 psi.
- 3. Reduced ice content has no basic effect on the creep characteristics of sand-ice material but at equal deviator stresses, higher strain rates occur for the reduced ice samples.
- 4. The applied deviator stress for high and reduced ice content samples can be related to the maximum deviator stress obtained from constant strain rate tests by a term M, percent of maximum deviator stress. Samples tested with the same percent of maximum deviator stress exhibit the same creep behavior and the resulting strain rates are equal.
- 5. The strain rate versus strain curve for sandice materials can be approximated using a constant slope factor K, which describes the decrease in strain rate per increment of strain for any given percent of maximum deviator stress.

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**APPENDICES** 

# TABLE A-1

CONSTANT AXIAL STRAIN RATE TEST DATA

TEMPERATURE = -12.0° C   STRAIN RATE = 2.66 x 10 - 3 min - 1	SAMPLE NUMBER 1	SAMPLE NUMBER 4
2.0 0.003 160.0 1.0 0.0004 20.0 3.0 0.007 250.0 1.0 0.0007 65.0 4.0 0.009 360.0 1.5 0.0039 105.0 5.0 0.012 510.0 2.0 0.0063 135.0 6.0 0.016 725.0 2.5 0.0086 175.0 7.0 0.019 945.0 3.0 0.0116 220.0 8.0 0.024 1125.0 4.0 0.0144 330.0 9.0 0.030 1285.0 5.0 0.0170 475.0 10.0 0.035 1345.0 6.0 0.0210 670.0 11.0 0.035 1345.0 6.0 0.0210 670.0 11.0 0.041 1395.0 7.0 0.0251 875.0 12.0 0.047 1395.0 8.0 0.0290 1100.0 13.0 0.052 1395.0 9.0 0.0343 1265.0 14.0 0.058 1360.0 10.0 0.0394 1360.0 15.0 0.052 1395.0 9.0 0.0343 1265.0 14.0 0.058 1360.0 11.0 0.0452 1400.0 SAMPLE NUMBER 2 12.0 0.0564 1400.0 11.0 0.0564 1400.0 15.0 0.0564 1400.0 17.0 0.0647 1380.0 0.0564 1400.0 0.0571 17.0 0.0614 1230.0 0.0564 1400.0 0.0571 17.0 0.0814 1230.0 0.0564 1400.0 0.0571 17.0 0.0814 1230.0 0.0564 1400.0 0.0571 17.0 0.0814 1230.0 0.0564 1400.0 0.0571 160.0 0.0938 860.0 0.0938	PERCENT SAND = 61.6 PERCENT ICE = 99.8 TOTAL VOLUME CHANGE = NA CONFINING PRESSURE = 0 psi TIME DEFL. LOAD	PERCENT SAND = 63.5 PERCENT ICE = 97.4 TOTAL VOLUME CHANGE = NA CONFINING PRESSURE = 0 psi TIME DEFL. LOAD
15.0 0.0445 0.0	1.0 0.001 95.0 2.0 0.003 160.0 3.0 0.007 250.0 4.0 0.009 360.0 5.0 0.012 510.0 6.0 0.016 725.0 7.0 0.019 945.0 8.0 0.024 1125.0 9.0 0.030 1285.0 10.0 0.035 1345.0 11.0 0.041 1395.0 12.0 0.047 1395.0 13.0 0.052 1395.0 14.0 0.058 1360.0 15.0 0.064 1150.0  SAMPLE NUMBER 2  TEMPERATURE = -12.0° C STRAIN RATE = 2.66 x 10 -3 min -1 PERCENT ICE = 92.8 TOTAL VOLUME CHANGE = NA CONFINING PRESSURE = 0 psi TIME DEFL. LOAD (MIN.) (INS.) (LBS.)  0.0 0.0 0.0 0.0 1.0 0.0048 330.0 4.0 0.0048 330.0 4.0 0.0078 540.0 5.0 0.0110 815.0 6.0 0.0147 1055.0 7.0 0.0190 1245.0 8.0 0.0241 1350.0 9.0 0.0291 1415.0 10.0 0.0346 1455.0 11.0 0.0399 1480.0 12.0 0.0458 1495.0 13.0 0.0508 1495.0	0.0       0.0000       0.0         0.5       0.0004       20.0         1.0       0.0017       65.0         1.5       0.0039       105.0         2.0       0.0063       135.0         2.5       0.0086       175.0         3.0       0.0116       220.0         4.0       0.0144       330.0         5.0       0.0170       475.0         6.0       0.0210       670.0         7.0       0.0251       875.0         8.0       0.0290       1100.0         9.0       0.0343       1265.0         10.0       0.0394       1360.0         11.0       0.0452       1400.0         12.0       0.0508       1400.0         13.0       0.0564       1400.0         14.0       0.0627       1380.0         15.0       0.0686       1345.0         16.0       0.0752       1290.0         17.0       0.0814       1230.0         18.0       0.0870       1160.0         19.0       0.0888       1088.0         20.0       0.0905       810.0         21.0       0.0922       925.0

### TEMPERATURE = $-12.0^{\circ}$ C STRAIN RATE = $2.66 \times 10^{-3}$ min PERCENT SAND = 62.5PERCENT ICE = 94.5 TOTAL VOLUME CHANGE = NA CONFINING PRESSURE = 0 psi DEFL. TIME LOAD (MIN.) (INS.) (LBS.) 0.0 0.0000 0.0 1.0 0.0010 10.0 2.0 0.0043 125.0 3.0 0.0078 240.0 4.0 0.0108 425.0 5.0 0.0146 640.0 6.0 0.0196 830.0 7.0 0.0238 1030.0 8.0 0.0289 1170.0 9.0 0.0344 1255.0 10.0 0.0408 1325.0 11.0 0.0455 1360.0 12.0 0.0509 1400.0 13.0 0.0569 1435.0 14.0 0.0617 1465.0 15.0 0.0677 1495.0 16.0 0.0740 1515.0 17.0 0.0800 1540.0 18.0 0.0861 1550.0 19.0 0.0905 1545.0 20.0 0.0965 1540.0 21.0 0.1028 1535.0 22.0 0.1084 1530.0 23.0 0.1148 1520.0 24.0 0.1202 1505.0 25.0 0.1267 1480.0 26.0 0.1327 1445.0 27.0 0.1402 1405.0 28.0 0.1459 1355.0 29.0 0.1515 1300.0 30.0 0.1581 1240.0 31.0 0.1642 1180.0

0.1707

0.1763

0.1830

0.1886

1115.0

1045.0

990.0 930.0

32.0

33.0

34.0

35.0

## SAMPLE NUMBER 7

TEMPERATURE =  $-12.0^{\circ}$  C STRAIN RATE =  $2.66 \times 10^{-3} \text{min}^{-1}$ PERCENT SAND = 62.9PERCENT ICE = 94.5 TOTAL VOLUME CHANGE = NA CONFINING PRESSURE = 0 psi TIME DEFL. LOAD (MIN.) (INS.) (LBS.) 0.0000 0.0 0.0 1.0 0.0026 65.0 2.0 0.0054 170.0 330.0 3.0 0.0084 4.0 0.0117 555.0 5.0 0.0154 800.0 6.0 0.0186 1005.0 7.0 0.0231 1205.0 8.0 0.0283 1310.0 9.0 0.0341 1345.0 10.0 0.0401 1360.0 0.0461 11.0 1360.0 1360.0 12.0 0.0522 13.0 0.0586 1350.0 14.0 0.0647 1340.0 0.0708 15.0 1325.0 0.0769 16.0 1310.0 17.0 0.0829 1280.0 18.0 0.0887 1245.0 19.0 0.0948 1215.0 20.0 0.1010 1190.0 21.0 0.1072 1170.0 0.1133 22.0 1150.0 23.0 0.1193 1130.0 24.0 0.1255 1110.0 25.0 0.1318 1100.0 26.0 0.1384 1085.0 0.1449 27.0 1080.0 0.1512 28.0 1065.0

# SAMPLE NUMBER 10

TEMPERATURE = STRAIN RATE = 1 PERCENT SAND = 0 PERCENT ICE = 90 TOTAL VOLUME CHA CONFINING PRESSI TIME DEFL. (MIN.) (INS.	62.9 6.0 ANGE = NA URE = O psi	STRAIN PERCENT PERCENT TOTAL V CONFINI TIME	ATURE = -1 RATE = 2. SAND = 6 ICE = 95 OLUME CHA ING PRESSU DEFL. (INS.)	66 x 10 min 3.0 0.0 NGE = NA IRE = 355 psi LOAD
5.0 0.0067 6.0 0.0085 7.0 0.0104 8.0 0.0125 9.0 0.0146 10.0 0.0168 11.0 0.0192 12.0 0.0217 14.0 0.0270 16.0 0.0336 18.0 0.0394 20.0 0.0454 22.0 0.0514	45.0 90.0 145.0 210.0 270.0 355.0 460.0 580.0 690.0 780.0 1020.0 1130.0 1265.0 1320.0 1360.0 1390.0 1420.0 1445.0 1470.0 1495.0 1515.0 1535.0	10.0 11.0 12.0 13.0 14.0 15.0 16.0 17.0 18.0 19.0 20.0 21.0 22.0 23.0 24.0	0.0222 0.0276 0.0331 0.0388 0.0447 0.0505	165.0 345.0 540.0 765.0 960.0 1115.0 1225.0 1310.0 1385.0 1455.0 1515.0 1575.0 1635.0 1695.0 1760.0

#### 13 SAMPLE NUMBER SAMPLE NUMBER TEMPERATURE = -12.0° C TEMPERATURE = $-12.0^{\circ}$ C STRAIN RATE = $2.66 \times 10^{-3}$ min STRAIN RATE = $2.66 \times 10^{-3} \text{min}^{-1}$ PERCENT SAND = 62.8PERCENT SAND = 62.9PERCENT ICE = 97.5 PERCENT ICE = 95.0TOTAL VOLUME CHANGE = NA TOTAL VOLUME CHANGE = NA CONFINING PRESSURE = 350 psi CONFINING PRESSURE = 105 psi LOAD DEFL. LOAD TIME TIME DEFL. (INS.) (LBS.) (MIN.) (INS.)(LBS.) (MIN.)0.0 0.0 0.0 0.0 0.0000 0.0 0.0049 0.0 1.0 75.0 0.0040 1.0 0.0106 20.0 2.0 155.0 0.0082 2.0 3.0 0.0154 110.0 240.0 0.0125 3.0 220.0 4.0 0.0202 345.0 0.0169 4.0 5.0 0.0248 370.0 480.0 5.0 0.0213 560.0 6.0 0.0293 0.0255 660.0 6.0 755.0 0.0342 7.0 850.0 0.0305 7.0 8.0 0.0393 930.0 1020.0 0.0358 8.0 9.0 0.0447 1070.0 1170.0 0.0411 9.0 0.0503 1180.0 10.0 1270.0 0.0469 10.0 1260.0 11.0 0.0559 1340.0 0.0526 11.0 0.0618 1320.0 12.0 1405.0 0.0584 12.0 13.0 0.0676 1365.0 1455.0 0.0644 13.0 0.0736 1420.0 14.0 1500.0 0.0701 14.0 15.0 0.0795 1465.0 0.0761 1540.0 15.0 U.0855 1510.0 16.0 1580.0 0.0819 16.0 17.0 0.0905 1550.0 1615.0 0.0876 17.0 18.0 0.0975 1585.0 1640.0 0.0936 18.0 0.1036 1615.0 19.0 1670.0 0.0993 19.0 0.1097 1630.0 20.0 0.1051 1695.0 20.0 21.0 0.1157 1630.0 1720.0 0.1112 21.0 0.1219 1615.0 22.0 1735.0 0.1170 22.0 23.0 0.1281 1590.0 0.1232 1745.0 23.0 0.1344 1575.0 24.0 1755.0 0.1292 24.0 0.1404 1570.0 25.0 1755.0 0.1355 25.0 0.1467 1565.0 26.0 0.1420 1745.0 26.0 0.1529 1560.0 27.0 0.1481 1735.0 27.0 28.0 0.1591 1550.0 1700.0 0.1545 28.0 29.0 0.1654 1550.0 1675.0 0.1609 29.0 0.1714 30.0 1540.0 1635.0 0.1672 30.0 31.0 0.1777 1530.0 0.1838 1520.0 32.0 0.1518 0.0 40.0

### SAMPLE NUMBER 18

```
TEMPERATURE = -12.0° C
STRAIN RATE = 2.66 \times 10^{-3} \text{min}^{-1}
PERCENT SAND = 62.3
PERCENT ICE = 97.5
TOTAL VOLUME CHANGE = NA
CONFINING PRESSURE = 700 psi
                     LOAD
 TIME
           DEFL.
           (INS.)
(MIN.)
                    (LBS.)
 0.0
          0.0
                      0.0
          0.0051
                    100.0
 1.0
 2.0
          0.0104
                    205.0
                    355.0
          0.0154
 3.0
 4.0
          0.0202
                    545.0
          0.0253
                    735.0
 5.0
          0.0302
                    955.0
 6.0
 7.0
          0.0352
                   1160.0
          0.0406
                   1325.0
 8.0
 9.0
          0.0457
                   1440.0
          0.0513
                   1525.0
10.0
11.0
          0.0571
                   1605.0
12.0
          0.0628
                   1675.0
13.0
          0.0686
                   1740.0
          0.0743
                   1800.0
14.0
15.0
          0.0802
                   1870.0
          0.0858
16.0
                   1940.0
          0.0920
17.0
                   2010.0
18.0
          0.0977
                   2080.0
19.0
          0.1034
                   2160.0
20.0
          0.1098
                   2230.0
21.0
          0.1149
                   2295.0
22.0
          0.1208
                   2360.0
                   2425.0
23.0
          0.1265
24.0
          0.1324
                   2480.0
25.0
          0.1380
                   2530.0
26.0
          0.1438
                   2575.0
27.0
          0.1496
                   2615.0
28.0
          0.1554
                   2650.0
          0.1614
                   2685.0
29.0
30.0
          0.1672
                   2695.0
          0.1735
31.0
                   2710.0
32.0
          0.1793
                   2725.0
          0.1854
33.0
                   2730.0
          0.1914
                   2730.0
34.0
35.0
          0.1974
                   2730.0
          0.2035
                   2730.0
36.0
          0.2065
                   2730.0
```

36.5

TEMPERATURE =  $-12.0^{\circ}$  C STRAIN RATE =  $2.66 \times 10^{-2} \text{min}^{-1}$ PERCENT SAND = 62.5PERCENT ICE = 97.0TOTAL VOLUME CHANGE = +0.193 cc CONFINING PRESSURE = 700 psi LOAD TIME DEFL. (MIN.)(INS.) (LBS.) 0.0 0.0000 0.0 0.1 0.0048 165.0 0.0091 0.2 400.0 0.3 0.0135 710.0 0.4 0.0180 1090.0 0.5 0.0223 1475.0 0.6 0.0272 1810.0 0.7 0.0324 2055.0 0.78 0.0370 2135.0 8.0 0.0380 2130.0 0.9 0.0453 1815.0

TABLE A-1.--Continued.

			-		
SAMPLE	NUMBER 1	9	SAMPLE	NUMBER 2	O - ICE
TEMPER	ATURE = -1	2.0° C	TEMPER	ATURE = -1:	2.0° C -31
		$0.7 \times 10^{-5} \text{min} = 1$	STRAIN		56 x 10 <sup>-3</sup> min <sup>-1</sup>
	= 3.	$54 \times 10^{-4} \text{min}_{-1}^{-1}$		T SAND = 0	
		76 X IU MIN		T ICE = 98	
	T SAND = 6		TOTAL '	VOLUME CHAI	NGE = -0.403 cc
	T ICE = 97				RE = 700 psi
IOIAL	VOLUME CHA	NGE = +0.362 cc		DEFL.	LOAD
		RE = 700 psi	(MIN.)	(INS.)	(LBS.)
TIME (MIN.)	DEFL. (INS.)	LOAD (LBS.)	0.0	0 0000	0 0
(111111.)	(1113.)	(LD3.)	0.5	0.0000 0.0025	0.0 60.0
0.0	0.0000	0.0	1.0	0.0049	135.0
25.0	0.0028	75.0	2.0	0.0098	275.0
50.0	0.0061	180.0	3.0	0.0149	415.0
75.0	0.0092	300.0	4.0	0.0206	500.U
100.0	0.0124	425.0	5.0	0.0264	570.0
125.0	0.0159	520.0	6.0	0.0319	635.0
150.0	0.0196	585.0	7.0	0.0378	685.0
175.0	0.0233 0.0271	645•0 695•0	8.0 9.0	0.0436 0.0496	715.0
200.0	0.0308	740.0	10.0	0.0557	740.0 755.0
234.0	0.0321	745.0	12.0	0.0679	760.0
235.0	0.0325	785.0	14.0	0.0802	750.0
240.0	0.0357	1000.0	16.0		735.0
245.0	0.0392	1125.0	18.0		715.0
250.0	0.0429	1215.0	20.0	0.1172	700.0
255.0	0.0466	1275.0	22.0 24.0	0.1296 0.1418	690.0
260.0 265.0	0.0505 0.0544	1325.0 1370.0	26.0	0.1510	670.0 665.0
275.0	0.0544	1445.0	28.0	0.1663	655.0
285.0	0.0700	1535.0	30.0	0.1784	650.0
295.0		1625.0	32.0	0.1907	640.0
305.0	0.0856	1730.0	34.0	0.2027	635.0
315.0	0.0931	1835.0	36.0	0.2151	630.0
325.0	0.1009	1930.0	37.0	0.2210	630.0
335.0	0.1085	2000.0			
345.0	0.1164	2105.0			
355.0	0.1242	2190.0			
365.0 368.5	0.1319 0.1347	2265•0 2300•0			
369.5	0.1363	2470.0			
370.0	0.1392	2675.0			
371.0	0.1427	2800.0			
272.0	0.1462	2885.0			
373.0	0.1500	2940.0			
374.0	0.1539	2970.0			
375.0	0.1579	2980.0			
376.0	0.1618	2975.0			
377.0 377.5	0.1660 0.1680	2965•0 2945•0			
377.5	0.1000	<b>∠</b> 7 <b>7</b> J ♦ V			

# SAMPLE NUMBER 22

TEMPERATURE = -12. STRAIN RATE = 2.66 PERCENT SAND = 63. PERCENT ICE = 97.0 TOTAL VOLUME CHANG CONFINING PRESSURE TIME DEFL. (MIN.) (INS.)	S X 10 min .0 ) GE = +0.662 cc E = 350 psi LOAD	PERCENT S PERCENT I TOTAL VOL	TE = 2.6 AND = 62 CE = 96. UME CHAN PRESSUR DEFL.	6 x 10 min . .8 0 GE = NA E = 350 psi _LOAD
6.0 0.0292 17 7.0 0.0351 18 8.0 0.0411 19 9.0 0.0540 11 11.0 0.0604 11 12.0 0.0688 11 13.0 0.0730 11 14.0 0.0794 11 15.0 0.0856 11 17.0 0.0985 11 17.0 0.0985 11 17.0 0.1048 11 19.0 0.1111 12 20.0 0.1175 12 21.0 0.1238 12 22.0 0.1305 13 22.0 0.1367 12 24.0 0.1431 13 25.0 0.1495 12 26.0 0.1559 12 27.0 0.1622 12 28.0 0.1685 12 29.0 0.1748 13 30.0 0.1814 13 31.0 0.1880 13 32.0 0.1944 33.0 0.2074 13	1105.0 1305.0 1430.0 1510.0	0.0 1.0 2.0 3.0 4.0 5.0 6.0 7.0 8.0 9.0 10.0 11.0 12.0 13.0 14.0 15.0 16.0 17.0 18.0 19.0 20.0 21.0 22.0 23.0 24.4 25.0	0.0318 0.0375	285.0 500.0 755.0 1025.0 1250.0 1395.0 1490.0 1550.0 1575.0 1590.0 1610.0 1630.0 1650.0 1680.0 1720.0 1765.0 1805.0 1805.0 1805.0 1890.0 1890.0 1890.0 1870.0

### SAMPLE NUMBER 24 SAMPLE NUMBER 27 TEMPERATURE = -12.0° C TEMPERATURE = -12.0° C STRAIN RATE = $2.66 \times 10^{-3} \text{min}^{-1}$ STRAIN RATE = $2.66 \times 10^{-3} \text{min}^{-1}$ PERCENT SAND = 63.0 EST. PERCENT SAND = 62.5 PERCENT ICE = 96.0 EST. PERCENT ICE = 96.5 TOTAL VOLUME CHANGE = NA TOTAL VOLUME CHANGE = +0.403 cc CONFINING PRESSURE = 350 psi CONFINING PRESSURE = 350 psi TIME DEFL. LOAD TIME DEFL. LOAD (MIN.)(MIN.) (INS.)(LBS.) (INS.) (LBS.) 1.0 0.0045 205.0 0.0 0.0 0.0 0.0087 2.0 410.0 1.0 0.0039 175.0 3.0 0.0129 665.0 2.0 0.0081 390.0 0.0223 1280.0 5.0 0.0124 645.0 3.0 7.0 1470.0 0.0334 4.0 0.0166 930.0 0.0509 10.0 1635.0 5.0 0.0216 1165.0 13.0 0.0691 1730.0 6.0 0.0269 1320.0 16.0 0.0869 1885.0 7.0 0.0325 1430.0 19.0 0.1045 2075.0 0.0382 8.0 1505.0 22.0 0.1224 2225.0 0.0439 9.0 1540.0 25.0 0.1404 2285.0 0.0499 10.0 1600.0 27.0 0.1631 2275.0 11.0 0.0557 1650.0 SAMPLE NUMBER 26 12.0 0.0617 1705.0 0.0675 13.0 1760.0 TEMPERATURE = $-12.0^{\circ}$ C 14.0 0.0734 1810.0 STRAIN RATE = $2.66 \times 10^{-3} \text{min}^{-1}$ 15.0 0.0792 1870.0 PERCENT SAND = 62.016.0 0.0850 1930.0 PERCENT ICE = 97.5 17.0 0.0909 1990.0 TOTAL VOLUME CHANGE =+.656 cc 18.0 0.0967 2040.0 CONFINING PRESSURE = 0 psi 19.0 0.1028 2070.0 TIME DEFL. LOAD 20.0 0.1089 2080.0 (MIN.)(INS.) (LBS.) 0.1151 21.0 2045.0 22.0 0.1214 1985.0 0.0 0.0 0.0 22.41 0.1240 1955.0 0.0029 105.0 1.0 23.0 0.1124 0.0 2.0 0.0059 230.0 3.0 0.0093 355.0 4.0 0.0129 525.0 0.0168 730.0 5.0 0.0210 6.0 945.0 7.0 0.0257 1140.0 8.0 0.0305 1280.0 9.0 0.0360 1370.0 10.0 0.0417 1425.0 11.0 0.0476 1460.0 12.0 0.0536 1470.0 13.0 0.0596 1480.0 15.0 0.0719 1480.0 17.0 0.0843 1470.0 0.0968 19.0 1470.0 21.0 0.1094 1450.0 23.0 0.1221 1410.0 23.62 0.1257 1395.0 24.0 0.1075

### TEMPERATURE = -12.0° C STRAIN RATE = $2.66 \times 10^{-3} \text{min}^{-3}$ PERCENT SAND = 62.7PERCENT ICE = 96.5 TOTAL VOLUME CHANGE = +0.484 cc CONFINING PRESSURE = 700 psi LOAD TIME DEFL. (INS.) (LBS.) (MIN.)415.0 0.0095 2.0 760.0 0.0142 3.0 0.0191 925.0 4.0 0.0241 1120.0 5.0 1315.0 0.0303 6.0 0.0414 1560.0 8.0 0.0529 1740.0 10.0 2040.0 0.0759 14.0 0.0992 2365.0 18.0 0.1224 2680.0 22.0

2860.0

2885.0

## SAMPLE NUMBER 33

26.0

29.0

21.0

23.0

0.1458

0.1638

TEMPERATURE = -12.0° C STRAIN RATE =  $2.66 \times 10^{-3} \text{min}^{-1}$ PERCENT SAND = 62.4PERCENT ICE = NA TOTAL VOLUME CHANGE = NA CONFINING PRESSURE = 0 psi DEFL. LOAD TIME (INS.) (LBS.) (MIN.) 0.0025 95.0 1.0 200.0 2.0 0.0060 4.0 0.0139 535.0 1005.0 6.0 0.0222 1225.0 8.0 0.0330 10.0 0.0445 1350.0 0.0667 1415.0 12.0 1465.0 14.0 0.0689 0.0809 1530.0 16.0 18.0 0.0932 1585.0

0.1118

0.1246

1630.0

1610.0

## SAMPLE NUMBER 34

TEMPERATURE = -12.0° C STRAIN RATE =  $2.66 \times 10^{-3} \text{min}^{-1}$ PERCENT SAND = 62.9PERCENT ICE = NA TOTAL VOLUME CHANGE = +0.282 cc CONFINING PRESSURE = 0 psi DEFL. LOAD TIME (INS.) (LBS.) (MIN.)0.0033 190.0 1.0 0.0064 370.0 2.0 0.0144 905.0 4.0 0.0243 1310.0 6.0 0.0355 1490.0 8.0 12.0 0.0593 1610.0 1670.0 16.0 0.0817 18.0 0.0958 1720.0 SAMPLE NUMBER 35 TEMPERATURE = -12.0° C STRAIN RATE =  $2.66 \times 10^{-3} \text{min}^{-1}$ PERCENT SAND = 63.0 EST. PERCENT ICE = NA TOTAL VOLUME CHANGE = NA CONFINING PRESSURE = 700 psi LOAD DEFL. TIME (INS.) (LBS.) (MIN.) 295.0 1.0 0.0047 0.0089 595.0 2.0 0.088 0.0134 3.0 1155.0 0.0182 4.0 0.0286 1530.0 6.0 1725.0 8.0 0.0398 0.0514 1820.0 10.0 2020.0 14.0 0.0748 0.0980 2320.0 18.0 2605.0 0.1210 22.0 2775.0 26.0 0.1444 2830.0 29.0 0.1620 2840.0 0.1726 30.7

SAMPLE NUMBER 36	SAMPLE NUMBER 38 continued.
TEMPERATURE = -12.0° C STRAIN RATE = 2.66 x 10 <sup>-3</sup> min <sup>-1</sup>	TIME DEFL. LOAD (MIN.) (INS.) (LBS.)
PFRCFNT SAND = 63.5 FST	20.0 0.1052 2675.0
PERCENT ICE = 96.0 EST.	22.0 0.1165 2790.0
TOTAL VOLUME CHANGE = NA	24.0 V.1280 2075.0
CONFINING PRESSURE = 700 psi TIME DEFL. LOAD	28.0 0.1517 2940.0
(MIN.) (INS.) (LBS.)	29.0 0.1577 2935.0
(1111.)	22.0 0.1165 2790.0 24.0 0.1280 2875.0 26.0 0.1397 2920.0 28.0 0.1517 2940.0 29.0 0.1577 2935.0 29.25 0.1591 2935.0
1.0 0.0047 320.0	30.0 0.1136 0.0
2.0 0.0089 635.0	SAMPLE NUMBER 39
3.0 0.0134 960.0 4.0 0.0183 1245.0	SAMILE NOMBER 35
4.0 0.0183 1245.0 6.0 0.0286 1640.0	TEMPERATURE = $-12.0^{\circ}$ C $_{-3}$ $_{-1}$
8.0 0.0398 1800.0	STRAIN RATE = $2.66 \times 10^{\circ}$ min
10.0 0.0514 1880.0	PERCENT SAND = 63.2
14.0 0.0751 2085.0	PERCENT ICE = 97.0 TOTAL VOLUME CHANGE = +0.696 cc
1010	CONFINING PRESSURE = 360 psi
~~~~	TIME DEFL. LOAD
30.0 0.1875 2970.0	(MIN.) (INS.) (LBS.)
32.0 0.1794 2990.0	
SAMPLE NUMBER 38	0.0 0.0000 0.0 1.0 0.0042 140.0
SAMEL NOMBER 33	2.0 0.0084 320.0 3.0 0.0123 525.0 4.0 0.0166 775.0
TEMPERATURE = $-12.0^{\circ}$ C $_{-3}$ $_{-1}$	3.0 0.0123 525.0
STRAIN RATE = $2.66 \times 10^{-3} \text{min}^{-1}$	4.0 0.0166 775.0
PERCENT SAND = 63.0 PERCENT ICE = 97.0	3.0 0.0213 333.0
TOTAL VOLUME CHANGE = +0.559 cc	6.0 0.0262 1175.0 7.0 0.0313 1310.0
CONFINING PRESSURE = 700 psi	8.0 0.0366 1420.0
TIME DEFL. LOAD	9.0 0.0419 1520.0
(MIN.) (INS.) (LBS.)	10.0 0.0475 1615.0
0.0 0.0000 0.0	12.0 0.0582 1775.0
0.0 0.0000 0.0 1.0 0.0044 190.0	14.0 0.0693 1950.0 16.0 0.0804 2095.0
2.0 0.0088 470.0	18.0 0.0917 2215.0
3.0 0.0132 740.0	20.0 0.1029 2315.0
4.0 0.0179 1010.0	22.0 0.1144 2370.0 24.0 0.1259 2375.0
5.0 0.0225 1230.0 6.0 0.0277 1400.0	24.0 0.1259 2375.0 25.0 0.1318 2350.0
7.0 0.0330 1530.0	26.0 0.1378 2295.0
8.0 0.0383 1645.0	27.0 0.1017 0.0
9.0 0.0439 1750.0	
10.0 0.0492 1840.0 12.0 0.0604 2010.0	
14.0 0.0716 2200.0	
16.0 0.0827 2375.0	
18.0 0.0938 2535.0	

17.0

0.0

### SAMPLE NUMBER 40 SAMPLE NUMBER 42 TEMPERATURE = -12.0° C TEMPERATURE = -12.0° C STRAIN RATE = $2.66 \times 10^{-3} \text{min}^{-1}$ STRAIN RATE = $2.66 \times 10^{-3} \text{min}^{-1}$ PERCENT SAND = 63.0PERCENT SAND = 62.8PERCENT ICE = NA PERCENT ICE = 96.0 TOTAL VOLUME CHANGE = NA TOTAL VOLUME CHANGE = +0.240 cc CONFINING PRESSURE = 100 psi CONFINING PRESSURE = 0 psi TIME DEFL. LOAD TIME DEFL. LOAD (MIN.)(INS.) (LBS.) (MIN.)(INS.) (LBS.) 0.0044 100.0 1.0 0.0033 140.0 1.0 0.0084 180.0 2.0 0.0062 275.0 2.0 4.0 435.0 3.0 0.0098 440.0 0.0165 0.0248 910.0 4.0 0.0139 665.0 6.0 5.0 1295.0 0.0185 900.0 8.0 0.0348 1495.0 0.0457 6.0 0.0229 1100.0 10.0 0.0573 1630.0 8.0 0.0338 1345.0 12.0 14.0 0.0686 1730.0 10.0 0.0453 1440.0 1790.0 12.0 0.0568 1480.0 0.0808 16.0 1790.0 13.0 0.0627 1485.0 0.0868 17.0 1770.0 0.0687 1482.0 18.0 0.0932 14.0 SAMPLE NUMBER 43 SAMPLE NUMBER 41

TEMPERATURE =  $-12.0^{\circ}$  C STRAIN RATE =  $2.66 \times 10^{-3} \text{min}^{-1}$ TEMPERATURE = -12.0° C STRAIN RATE =  $2.66 \times 10^{-3}$ PERCENT SAND = 63.6PERCENT SAND = 62.9PERCENT ICE = 96.5 PERCENT ICE = 96.0 TOTAL VOLUME CHANGE = +0.426 cc TOTAL VOLUME CHANGE = +0.246 cc CONFINING PRESSURE = 0 psi CONFINING PRESSURE = 100 psi TIME DEFL. LOAD TIME DEFL. LOAD (MIN.)(INS.) (LBS.) (MIN.)(INS.) (LBS.) 0.0 0.0 0.0000 0.0028 100.0 1.0 0.0 0.0000 0.0 205.0 0.0035 80.0 2.0 0.0057 1.0 565.0 2.0 0.0070 135.0 4.0 0.0141 1075.0 405.0 0.0214 4.0 0.0162 6.0 865.0 0.0319 1385.0 0.0248 8.0 6.0 0.0347 1285.0 0.0430 1545.0 8.0 10.0 1505.0 1635.0 10.0 0.0456 12.0 0.0545 1645.0 0.0604 1660.0 0.0572 13.0 12.0 1660.0 0.0688 1735.0 14.0 0.0661 14.0 16.0 0.0721 0.0807 1770.0 15.0 1650.0 1755.0 0.0838 15.25 0.0737 1640.0 16.5 0.0548 0.0

0.1746

550.0

### SAMPLE NUMBER 47 SAMPLE NUMBER 44 TEMPERATURE = $-12.0^{\circ}$ C TEMPERATURE = $-12.0^{\circ}$ C STRAIN RATE = $2.66 \times 10^{-3} \text{min}^{-1}$ STRAIN RATE = 5.33 x 10 -3 min -1 PERCENT SAND = 63.5PERCENT SAND = 63.5 PERCENT ICE = 96.5 PERCENT ICE = 96.0 TOTAL VOLUME CHANGE = +0.450 CC TOTAL VOLUME CHANGE = +1.00 cc CONFINING PRESSURE = 700 psi CONFINING PRESSURE = 700 psi DEFL. LOAD TIME DEFL. LOAD TIME (INS.) (LBS.) (MIN.) (INS.) (LBS.) (MIN.) 0.0 0.0000 0.0 0.0 0.0000 0.0 1.0 0.0043 1.0 0.0084 595.0 250.0 2.0 0.0084 2.0 0.0172 1305.0 530.0 4.0 0.0171 1170.0 3.0 0.0270 1865.0 6.0 0.0265 1740.0 4.0 0.0378 2145.0 8.0 0.0372 2070.0 5.0 0.0489 2305.0 10.0 0.0482 2220.0 6.0 0.0601 2455.0 12.0 0.0595 2355.0 7.0 0.0714 2585.0 14.0 0.0729 2535.0 8.0 0.0832 2675.0 16.0 0.0842 2660.0 9.0 0.0952 2770.0 0.1071 2885.0 18.0 0.0954 2800.0 10.0 0.1067 20.0 2935.0 11.0 0.1187 2980.0 22.0 0.1181 3040.0 12.0 0.1305 3035.0 22.5 0.1210 13.0 0.1420 3050.0 3050.0 22.75 0.1226 3045.0 14.0 0.1539 3060.0 0.1658 3050.0 24.0 0.0771 500.0 15.0 0.1224 16.0 370.0 SAMPLE NUMBER 45 ICE TEMPERATURE = -12.0° C STRAIN RATE = 2.66 x 10 -3 min -1 PERCENT SAND = 0PERCENT ICE = 98.0 TOTAL VOLUME CHANGE = +0.294 cc CONFINING PRESSURE = 0 psi DEFL. LOAD TIME (MIN.) (INS.) (LBS.) 0.0 0.0 0.0 1.0 0.0032 120.0 2.0 0.0062 245.0 4.0 0.0148 460.0 590.0 6.0 0.0254 8.0 0.0368 660.0 10.0 0.0485 685.0 12.0 0.0602 685.0 15.0 0.0786 660.0 18.0 0.0967 630.0 615.0 21.0 0.1146 24.0 0.1325 580.0 27.0 0.1503 565.0 0.1682 560.0 30.0

### 48 SAMPLE NUMBER SAMPLE NUMBER 50 TEMPERATURE = -12.0° C TEMPERATURE = $-12.0^{\circ}$ C STRAIN RATE = 5.33 x 10 -3 min -1 STRAIN RATE = 2.66 x 10 - 3 min - 1 PERCENT SAND = 63.7PERCENT SAND = 63.2 PERCENT ICE = 96.0 PERCENT ICE = 96.0 TOTAL VOLUME CHANGE = +0.493 cc TOTAL VOLUME CHANGE = +0.745 cc CONFINING PRESSURE = 700 psi CONFINING PRESSURE = 690 psi DEFL. LOAD TIME TIME DEFL. LOAD (MIN.) (MIN.) (INS.) (LBS.) (INS.) (LBS.) 0.0 0.0000 0.0 0.0 0.0000 0.0 1.0 0.0084 545.0 10.0 0.0046 210.0 20.0 0.0092 2.0 0.0171 1250.0 445.0 0.0265 3.0 1850.0 30.0 0.0140 675.0 4.0 0.0373 2135.0 40.0 0.0190 885.0 50.0 0.0236 5.0 0.0487 2290.0 1065.0 6.0 0.0601 2435.0 60.0 0.0291 1215.0 0.0716 2585.0 7.0 70.0 0.0346 1355.0 8.0 0.0833 2720.0 80.0 0.0400 1475.0 9.0 0.0951 2840.0 100.0 0.0513 1715.0 10.0 0.1062 2950.0 120.0 0.0627 1935.0 11.0 0.1177 3040.0 140.0 0.0739 2145.0 12.0 0.1290 3100.0 0.0853 160.0 2330.0 0.0967 13.0 0.1409 3120.0 180.0 2535.0 200.0 0.1082 2695.0 13.5 0.1470 3130.0 0.1016 360.0 220.0 0.1199 14.0 2840.0 240.0 0.1318 2955.0 SAMPLE NUMBER 51 260.0 0.1435 3025.0 270.0 0.1494 3060.0 TEMPERATURE = -12.0° C 0.1525 275.0 3060.0 STRAIN RATE = 2.66 x 10<sup>-3</sup>min<sup>-1</sup> 276.0 0.1072 360.0 PERCENT SAND = 63.5 EST. PERCENT ICE = 96.0 EST. TOTAL VOLUME CHANGE = NA CONFINING PRESSURE = 660 psi DEFL. TIME LOAD (MIN.) (INS.) (LBS.) 0.0044 270.0 1.0 0.0087 2.0 535.0 815.0 3.0 0.0131 4.0 0.0177 1110.0 5.0 0.0226 1340.0 0.0277 6.0 1520.0 0.0355 1780.0 8.0 10.0 0.0500 1980.0 12.0 0.0613 2160.0 14.0 0.0726 2335.0 16.0 0.0840 2495.0 18.0 0.0955 2590.0

19.0

0.1014

# SAMPLE NUMBER 72

	• • • • • • • • • • • • • • • • • • • •	-			
PERCENT S PERCENT S TOTAL VOI	ATE = 2.6 SAND = 6: ICE = 96. LUME CHAN G PRESSUI	56 x 10 <sup>-3</sup> min <sup>-1</sup> 3.2	STRAIN F PERCENT PERCENT TOTAL VO	TURE = -12 RATE = 4.4 SAND = 62 ICE = 57.0 DLUME CHANG PRESSUR	2 x 10 min .7 0 GE = NA E = 0 psi
			_		LOAD
(MIN•)	(102.)	(LBS.)	(MIN.)	(INS.)	(LBS.)
1.0 2.0	0.0000 0.0046 0.0084	425.0	0.0 0.5 1.0	0.0071	121.0
3.0	0.0126			0.0142	
-	0.0171			0.0204	
-		1215.0	4.0		616.0
6.0	0.0269	1395.0	5.0	0.0342	767.0
		1535.0	6.0	0.0419	873.0
-	0.0375	1650.0	7.0	0.0510	909.0
9.0	0.0429	1750.0	8.0	0.0610	865.0
10.0	0.0484	1850.0	9.0	0.0717	755.0
11.0	0.0538	1940.0	10.0	0.0833	631.0
12.0	0.0594	2030.0	11.0	0.0953	475.0
14.0	0.0705	2215.0	12.0	0.1083	298.0
16.0	0.0816	2385.0	13.0	0.1204	220.0
	0.0922			0.1308	
-			15.0	0.1411	164.0
		2745.0	16.0	0.1510	155.0
-	0.1264	2800.0		0.1611	
26.0		2830.0	-	0.1713	132.0
		2830.0		0.1817	
		260.0	20.0		121.0
• 0					

SAMPLE NUMBER 73	SAMPLE NUMBER 76
PERCENT SAND = 62.1  PERCENT ICE = 53.6  TOTAL VOLUME CHANGE = NA  CONFINING PRESSURE = 350 psi	TEMPERATURE = -12.0° C STRAIN RATE = 2.66 x 10-3min-1 PERCENT SAND = 63.4 PERCENT ICE = 58.2 TOTAL VOLUME CHANGE = NA CONFINING PRESSURE = 700 psi TIME DEFL. LOAD (MIN.) (INS.) (LBS.)
0.0       0.0000       0.0         2.0       0.0073       325.0         3.0       0.0113       478.0         4.0       0.0152       620.0         5.0       0.0197       733.0         8.0       0.0338       1109.0         10.0       0.0440       1302.0         12.0       0.0546       1463.0         14.0       0.0656       1559.0         16.0       0.0770       1678.0         18.0       0.0892       1709.0         20.0       0.1040       1683.0         25.0       0.1352       1572.0         30.0       0.1691       1465.0         35.0       0.2038       1303.0         40.0       0.2373       1163.0	0.0 0.0000 0.0 2.0 0.0097 500.0 5.0 0.0270 1161.0 7.0 0.0389 1438.0 10.0 0.0565 1797.0 12.0 0.0676 1992.0 15.0 0.0845 2252.0 17.0 0.0964 2372.0 20.0 0.1164 2459.0 22.0 0.1266 2405.0 25.0 0.1428 2377.0 30.0 0.1696 2313.0 33.0 0.1859 2260.0 35.0 0.1963 2230.0 40.0 0.2232 2136.0 45.0 0.2499 2055.0
45.0 0.2697 1077.0 SAMPLE NUMBER 74	SAMPLE NUMBER 77
PERCENT SAND = 62.5  PERCENT ICE = 55.8  TOTAL VOLUME CHANGE = NA	TEMPERATURE = -12.0° C STRAIN RATE = 2.66 x 10 <sup>-3</sup> min <sup>-1</sup> PERCENT SAND = 62.3 PERCENT ICE = 95.0 TOTAL VOLUME CHANGE = +0.890 cc CONFINING PRESSURE = 1000 psi TIME DEFL. LOAD (MIN.) (INS.) (LBS.)
0.0       0.0       0.0         1.0       0.0059       214.0         2.0       0.0104       487.0         4.0       0.0208       975.0         6.0       0.0318       1307.0         8.0       0.0428       1607.0         10.0       0.0542       1880.0         12.0       0.0658       2135.0         14.0       0.0774       2365.0         16.0       0.0895       2551.0         18.0       0.1013       2653.0         20.0       0.1131       2715.0         22.0       0.1251       2744.0         24.0       0.1377       2737.0         26.0       0.1496       2684.0         28.0       0.1609       2660.0	0.0       0.0000       0.0         2.0       0.0082       464.0         5.0       0.0229       1451.0         7.0       0.0356       1940.0         10.0       0.0568       2160.0         12.0       0.0693       2314.0         15.0       0.0877       2548.0         17.0       0.0998       2689.0         20.0       0.1182       2873.0         22.0       0.1291       2961.0         24.7       0.1471       3040.0         26.0       0.1551       3012.0         28.0       0.1652       2945.0         30.0       0.1745       2938.0

#### SAMPLE NUMBER 78 SAMPLE NUMBER TEMPERATURE = -12.0° C TEMPERATURE = -12.0° C STRAIN RATE = 2.66 x 10 - 3 min - 1 STRAIN RATE = 2.66 x 10 - 3 min - 1 PERCENT SAND = 63.4 PERCENT SAND = 62.9 PERCENT ICE = 55.0 PERCENT ICE = 95.5 TOTAL VOLUME CHANGE = NA TOTAL VOLUME CHANGE = +1.184 cc CONFINING PRESSURE = 100 psi CONFINING PRESSURE = 200 psi DEFL. LOAD LOAD TIME TIME DEFL. (MIN.) (INS.) (LBS.) (MIN.) (INS.) (LBS.) 0.0000 0.0 0.0 0.0000 0.0 0.0 125.0 1.0 0.0042 1.0 0.0036 208.0 2.0 0.0086 259.0 0.0074 495.0 2.0 4.0 0.0190 572.0 0.0111 820.0 3.0 809.0 0.0313 0.0159 6.0 4.0 1172.0 0.0431 964.0 8.0 5.0 0.0198 1467.0 1055.0 10.0 0.0558 0.0248 1665.0 6.0 0.0581 1060.0 10.3 0.0311 1732.0 7.0 12.0 U.0689 1045.0 0.0375 8.0 1793.0 988.0 15.0 0.0875 9.0 0.0445 1852.0 20.0 0.1199 848.0 10.0 0.0508 1810.0 25.0 0.1537 702.0 11.0 0.0579 1725.0 0.1883 576.0 30.0 12.0 0.0639 1064.0 35.0 0.2214 499.0 SAMPLE NUMBER 81 0.2474 485.0 39.0 TEMPERATURE = -12.0° C STRAIN RATE = 2.66 x 10 - 3 min - 1 SAMPLE NUMBER 79 PERCENT SAND = 62.6 TEMPERATURE = -12.0° C STRAIN RATE = 2.66 x 10 -3 min -1 PERCENT ICE = 96.0 TOTAL VOLUME CHANGE = +1.178 cc PERCENT SAND = 63.7 CONFINING PRESSURE = 1000 psi PERCENT ICE = 59.4 DEFL. LOAD TIME TOTAL VOLUME CHANGE = NA (MIN.) (INS.) (LBS.) CONFINING PRESSURE = 0 psi DEFL. TIME LOAD 0.0115 742.0 2.0 (MIN.) (INS.) (LBS.) 0.0170 1090.0 3.0 4.0 0.0228 1413.0 0.0. 0.0000 0.0 0.0293 1694.0 5.0 . 1.0 0.0049 183.0 0.0363 1888.0 6.0 0.0109 369.0 2.0 7.0 0.0436 2035.0 3.0 0.0179 558.0 0.0511 2144.0 8.0 4.0 0.0254 096.0 9.0 0.0588 2247.0 5.0 0.0324 801.0 10.0 0.0662 2362.0 6.0 0.0405 **837.0** 12.0 0.0807 2552.0 7.0 0.0485 855.0 0.0950 14.0 2758.0 0.0559 8.0 852.0 16.0 0.1093 2907.0 10.0 0.0714 786.0 0.1236 3022.0 18.0 12.5 0.0902 542.0 20.0 0.1382 3083.0 15.0 0.1022 384.0 22.0 0.1527 3121.0 20.0 0.1317 255.0 0.1676 24.0 3013.0 25.0 0.1559 201.0 26.0 0.1824 3086.0 30.0 0.2135 3000.0

	SAMPLE	NUMBER 82		SAMPLE	NUMBER 8	34
	TEMPERA	TURE = -12.0° C _3	_1	TEMPERA	TURE = -1	2.0° C _3 _1
	STRAIN	FURE = $-12.0^{\circ}$ C RATE = $2.66 \times 10^{-3}$	min'	STRAIN	RATE = 2.	.66 x 10 <sup>-3</sup> min <sup>-</sup>
	PERCENT	SAND = 62.8			SAND = 6	
		ICE = 97.0			ICE = 95	
		OLUME CHANGE = NA NG PRESSURE = 200	psi	TOTAL V CONFINI	OLUME CHA NG PRESSU	NGE = NA IRE = 100 psi
	TIME	DEFL. LOAD		TIME	DEFL.	LOAD
	_	(INS.) (LBS.)			(INS.)	
2	0.0		• 0	1.0030.5	0.0031	80.0
	1.0	0.0059 131.0		1.0	0.0068	168.0
	2.0	0.0111 281.0		2.0	0.0123	450.0
	3.0	0.0149 510.0 0.0186 791.0 0.0222 1087.0		3.0 4.0	0.0174	794.0
	4.0	0.0186 791.0		4.0	0.0226	1184.0
	5.0	0.0222 1087.0		5.0	0.0284	1546.0
	0.0	0.0204 13/1.0		6.1	0.0362	1680.0
		0.0313 1637.0		7.0	0.0424	1657.0
		0.0371 1805.0		10.0	0.0607	1555.0
		0.0437 1894.0			0.0882	
		0.0505 1943.0			0.1258	
		0.0576 1984.0		25.0	0.1555	1409.0
		0.0705 2025.0				
		0.0877 1973.0				•
		0.1112 1906.0				
		0.1387 1786.0		SAMPLE N	UMBER 87	
	28.0					
	SAMPLE N	NUMBER 83		TEMPERAT	URE = -12	.0° C -31
					ATE = 2.6	
	TEMPERAT	TURE = -12.0° C	1		SAND = 63	
	STRAIN	$RAIE = 2.66 \times 10^{-6} \text{m}$	in '		ICE = 32.	
		SAND = 63.5			LUME CHAN	
		ICE = 96.0				E = 100 psi
		LUME CHANGE = NA		TIME	DEFL.	LOAD
		NG PRESSURE = 0 psi		(MIN.)	(INS.)	(LBS.)
	TIME	DEFL. LOAD		1 0	0 0055	3.60
	(WIN.)	(INS.) (LBS.)		1.0	0.0055	168.0
		0.0027 172.0		2.0	0.0110	322.0
	1.0	0.0037 173.0		2.5	0.0138	400.0
	2.0	0.0078 378.0		3.0	0.0168	471.0
	3.0	0.0111 613.0		4.0	0.0234	600.0
	4.0	0.0145 870.0		5.0	0.0303	705.0
	5.0	0.0184 1139.0		6.0	0.0377	782.0
	6.0	0.0230 1358.0		7.0	0.0455	824.0
	7.0	0.0288 1502.0		7.5	0.0495	838.0
	8.0	0.0348 1564.0		8.0	0.0533	828.0
	9.0	0.0416 1597.0		10.0	0.0677	799.0
	11.0	0.0546 1537.0		15.0	0.0983	695.0
	13.0	0.0671 1496.0		20.0	0.1286	575.0
	15.0	0.0801 1438.0				
	20.0	0.1127 1215.0				
	25.0	0.1499 840.0				
	30.0	0.1892 322.0				
	35.0	0.2251 170.0				

SAMPLE	NUMBER 8	8	SAMPLE N	UMBER S-	1 UNFR	DZEN SAND
STRAIN PERCENT PERCENT	ICE = 98	66 x 10 <sup>-3</sup> 4.3	STRAIN R	URE = 20° ATE = 2.6 SAND = 64 ICE = 0	6 x 10 ~	3 <sub>min</sub> -1
CONFINI TIME (MIN.)	DEFL.	NGE = NA RE = 100 psi LOAD (LBS.)	TIME	G PRESSUR DEFL. (INS.)	LOAD	. <b>۵V</b>
3.0 4.0 4.7 5.0 5.7 6.0 7.0	0.0143 0.0199 0.0239 0.0263 0.0315 0.0330 0.0406 0.0523 0.0636	206.0 474.0 798.0 1188.0 1451.0 1553.0 1640.0 1620.0 1574.0 1495.0 1432.0 1343.0	45.0 50.0 55.0 60.0	0.1574 0.1896 0.2216 0.2540 0.2870 0.3195 0.3516 0.3833	277.0 255.0 250.0 243.0	+1.55 +1.50
			65.0	0.4151	243.0	+1.50
SAMPLE	NUMBER 8	9	SAMPLE N	NUMBER S	-2 UNFR	OZEN SANL
STRAIN PERCENT PERCENT	SAND = 6 ICE = 99	3.0 .0		RATE = 2.0 $SAND = 6.0$	66 x 10	3 <sub>min</sub> -1
CONFINI	OLUME CHA	NGE = NA RE = 100 psi	CONFINIA	IG PRESSU	DE - 40	
TIME	DEFL.	LOAD	TIME	DEFL.	LOAD	ΔV
(MIN.)	(INS.)	(LBS.)	(MIN.)	(INS.)	(LBS.)	
0.5 1.0 1.5 2.0 3.0 4.0 4.5 5.0 5.5 6.0 8.0	0.0027 0.0060 0.0083 0.0111 0.0167 0.0228 0.0273 0.0313 0.0358 0.0406 0.0560 0.0659	107.0 222.0 355.0 506.0 857.0 1227.0 1412.0 1500.0 1534.0 1532.0 1330.0 1203.0	0.0 1.0 3.0 5.0 10.0 15.0 20.0 25.0 30.0 35.0 40.0 45.0	0.0000 0.0060 0.0184 0.0307 0.0626 0.0951 0.1267 0.1593 0.1913 0.2237 0.2542 0.2881 0.3073	0.0 52.0 104.0 122.0 144.0 152.0 156.0 148.0 136.0 118.0 115.0	0.0 -0.05 -0.10 -0.05 +0.25 +0.55 +1.05 +1.40 LEAK
					- 4 T • U	

SAMPLE NUMBER S-3 UNFROZEN SAM	ID SAMPLE NUMBER S-4 UNFROZEN SAND
TEMPERATURE = 20° C STRAIN RATE = 2.66 x 10 <sup>-3</sup> min <sup>-1</sup> PERCENT SAND = 64.0 PERCENT ICE = 0	TEMPERATURE = 20° C STRAIN RATE = 2.66 x 10 <sup>-3</sup> min <sup>-1</sup> PERCENT SAND = 64.0 PERCENT ICE = 0
CONFINING PRESSURE = 21.5 psi	CONFINING PRESSURE = 14.3 psi

CONFINING	G PRESSUR	E = 21.5	psi	CONFINING	G PRESSURE	= 14.3	psi
TIME	DEFL.	LOAD	· Δ <b>V</b>	TIME	DEFL.	LOAD	٠Δ٧
(MIN.)	(INS.)	(LH5.)	(CC)	(MIN.)	(INS.)	(LBS.)	(CC)
1.0	0.0400	6.0	-0.01	0.0	0.0000	0.0	+0.0
2.0	0.0040	24.0	-0.03	0.5	0.0050	3.0	-0.03
3.0	0.0090	42.0	-0.07	1.0	0.0080	5.0	-0.04
4.0	0.0180	56.0	-0.09	2.0	0.0110	10.0	-0.09
5.0	0.0260	67.0	-0.07	3.0	0.0190	23.0	-0.20
6.0	0.0360	75.0	+0.0	4.0	0.0280	32.0	-0.27
7.0	0.0460	89.0	+0.09	5.0	0.0380	39.0	-0.32
8.0	0.0570	100.0	+0.17	6.0	0.0490	44.0	-0.32
9.0	0.0670	111.0	+0.38	7.0	0.0590	48.0	-0.32
10.0	0.0800	115.0	+0.48	8.0	0.0700	52.0	-0.26
11.0	0.0930	116.0	+0.72	9.0	0.0810	55.0	-0.14
12.0	0.1050	116.0	+0.89	10.0	0.0930	56.0	+0.03
13.0	0.1160	117.0	+1.10	11.0	0.1040	58.0	+0.09
16.0	0.1280	128.0	+1.28		0.1160	60.0	+0.20
17.0	0.1400	120.0	+1.49	13.0	0.1280	62.0	+0.29
18.0	0.1520	120.0	+1.70		0.1410	63.0	+0.42
19.0	0.1640	121.0	+1.88	15.0	0.1520	64.0	+0.55
20.0	0.1820	117.0	+2.14	16.0	0.1640	65.0	+0.67
21.0	0.2020	116.0	+2.40		0.1760	65•0	+0.85
22.0	0.2130	116.0	+2.57	18.0	0.1880	65.0	+1.00
23.0	0.2290	116.0	+2.74		0.2000	65.0	+1.16
24.0	0.2510	116.0			0.2110	66.0	+1.26
25.0	0.2630	115.0		21.0	0.2250	66.0	+1.46
26.0	0.2770	115.0		22.0	0.2350	66.0	+1.61
27.0	0.3010	112.0		23.0	0.2500	66 • J	+1.71
28.0	0.3170	112.0		24.0	0.2620	66.0	+1.85
29.0	0.3350	112.0			0.2740	66.0	+1.99
30.0	0.3410	112.0		26.0	0.2860	66.0	+2.09
31.0	0.3420	100.0		27.0	0.2980	65.0	+2.21

## SAMPLE NUMBER S-5 UNFROZEN SAND

TEMPERATURE = 20° C STRAIN RATE = 2.66 x 10<sup>-3</sup>min<sup>-1</sup> PERCENT SAND = 64.0 PERCENT ICE = 0

PERCENT	100 - 0		
CONFININTIME (MIN.)	DEFL. (INS.)	E = 28.6 LOAD (LBS.)	psi ΔV (CC)
0.0 1.0 2.0 3.0 4.0 5.0 6.0 7.0 8.0 9.0 10.0 11.0 12.0 13.0 14.0 15.0 16.0 17.0 18.0 19.0 20.0 21.0 22.0	0.0000 0.0020 0.0020 0.0120 0.0200 0.0300 0.0400 0.0510 0.0640 0.0770 0.0900 0.1020 0.1120 0.1260 0.1380 0.1510 0.1620 0.1760 0.1890 0.2020 0.2130 0.2270 0.2400	0.0 27.0 37.0 54.0 67.0 89.0 109.0 123.0 131.0 136.0 140.0 149.0 152.0 155.0 158.0 160.0 162.0 163.0 164.0 164.0	0.0 -0.03 -0.05 -0.08 -0.02 +0.14 +0.30 +0.45 +0.60 +0.76 +1.21 +1.61 +1.82 +2.03 +2.27 +2.45 +2.88
23.0 24.0 25.0	0.2520 0.2650	165.0 166.0	+3.06 +3.24 +3.32
26.0 27.0	0.2770 0.2920 0.3050	166.0 164.0 162.0	+3.50 +3.68
28.0	0.3180	156.0	+3.86

# SAMPLE NUMBER S-6 UNFROZEN SAND

TEMPERATURE = 20° C STRAIN RATE = 2.66 x 10<sup>-3</sup>min<sup>-1</sup> PERCENT SAND = 64 PERCENT ICE = 0

CONFINING	PRESSURE	= 50 p	si
TIME	DEFL.	LOA()	ΔV
(MIN.)	(INS.)	(LBS.)	(CC)
1.0 3.0 5.0 10.0 15.0 20.0 25.0 30.0	0.0000 .0055 0.0173 0.0297 0.0608 0.0942 0.1242 0.1542 0.1818 0.2004	0.0 60.0 120.0 139.0 157.0 162.0 162.0 157.0 152.0	0.0 0.0 -0.01 -0.20 -0.10 +0.10 +0.30 +0.40

TABLE A-2

CREEP TEST DATA

TABLE A-2.--Creep Test Data.

SAMPLE	NUMBER 9	O UNIAXIAL	SAMPLE N	IUMBER 91	STEP-S	TRESS
CONSTAN PERCENT PERCENT	SAND = 6: ICE = 94	TRESS = 1070 3.3 .7	psi CONSTANT PERCENT	<b>SAND = 6 ICE = 95</b>	TRESS = 3.6 .1	·
TIME	DEFL.	LOAD	TIME	DEFL.	LOAD	σ3
(MIN.)		(LBS.)	(MIN.)	(INS.)	_	
1.0 10.0 30.0 60.0 90.0 120.0 150.0 180.0 210.0 240.0 270.0 300.0 310.0 322.0 330.0		1074.0 1074.0 1072.0 1066.0 1065.0 1065.0 1065.0 1065.0 1065.0 1065.0 1065.0 1065.0 0.0	1.0 10.0 20.0 30.0 60.0 90.0 120.0 150.0 187.0 191.0 200.0 210.0 240.0 270.0 300.0 330.0	0.0348 0.0427 0.0482 0.0527 0.0563 0.0594 0.0600 0.0663 0.0672 0.0681 0.0700 0.0714 0.0724 0.0737		0   0   0   350
			380.0		1121.0	350

TABLE A-2.--Continued.

SAMPLE I	NUMBER 9:	BUNIAXIAL	SAMPLE	NUMBER 94	Continue	ed .
CONSTAN	TURE = -12	rress = 400 psi	TIME (MIN.)	DEFL. (INS.)	LOAD (LBS.) 407.0	σ3 _(PSI)
PERCENT	SAND = 63	0	70.0 80.0	0.0338 0.0347	-	
PERCENT	ICE = 60.	· Ο = ΝΔ	90.0	0.0355		
TOTAL V	ULUME CHAP	אטב - ווא	100.0	0.0363		
<b>-</b>	·>/==	1.0.55	110.0	0.0369		
TIME	DEFL.	LOAD	120.0	0.0375		
(MIN.)	(INS.)	(LBS.)	122.0	0.0376		100
1 0	0.0150	400.0	124.0	0.0391		200
1.0 10.0	0.0201	403.0	130.0	0.0398	411.0	1
30.0	0.0242	405.0	140.0	0.0406	413.0	
60.0	0.0275	405.0	150.0	0.0412	413.0	
90.0	0.0300	406.0	160.0	0.0419	406.0	
120.0	0.0316	+09.0	170.0	0.0423	417.0	
150.0	0.0330	409.0	178.0	0.0426		200
180.0	0.0340	408.0	181.0	0.0453		400
210.0	0.0349	406.0	190.0	0.0462		
240.0	0.0357	408.0	200.0	0.0467		
270.0	0.0364	407.0	210.0	0.0472		
300.0	0.0371	406.0	220.0	0.0476		
330.0	0.0378	406.0	230.0	0.0479		
350.0	0.0382	407.0	240.0	0.0482		400
351.0	0.0358	0.0	242.0	0.0483		400
355.0	0.0352	0.0	245.0	0.0504		600
			250.0	0.0508		
			260.0	0.0514		
SAMPLE N	UMBER 94	STEP-STRESS	270.0	0.0519 0.0522		
		• • •	280.0 290.0	0.0525		
	URE = -12		300.0	0.0528		
		RESS = $400 \text{ psi}$	303.0	0.0530		600
	SAND = 63		307.0	0.0558		800
	ICE = 59.		310.0	0.0560	410.0	1
TOTAL VO	LUME CHAN	GE - NA	320.0	0.0565	411.0	
T = MC		LOAD	330.0	0.0569	412.0	
TIME	UEFL.	LOAD 03	340.0	0.0572	412.0	
(MIN.)	(INS.)	(LBS.) (PŠI)	350.0	0.0575	412.0	ļ
1 0	0.0152	422.0 0	360.0	0.0577	412.0	į į
1.0 5.0	0.0190	402.0	361.0	0.0577	412.0	800
10.0	0.0210	402.0	365.0	0.0606	415.0	1000
20.0	0.0236	402.0	370.0	0.0610	415.0	1
30.0	0.0254	401.0	380.0	0.0614	416.0	
40.0	0.0269	402.0	390.0	0.0618	415.0	
50.0	0.0280	402.0	400.0	0.0620	416.0	_
60.0	0.0290	402.0	409.0	0.0622	416.0	1000
62.0	0.0293	404.0 0				
64.0	0.0327	405.0 100				
-						

SAMPLE	NUMBER 9	6 UNIAXIAL	SAMPLE	NUMBER 98	STEP-S	STRESS
CONSTAN PERCENT	TURE = -1: T AXIAL S SAND = 6: ICE = 95	TRESS = 400 3.8	psi CONSTAN PERCENT	TURE = -12 IT AXIAL ST SAND = 63 ICE = 60.	RESS = 6 .6	540 psi
		NGE = -0.078	CC TOTAL V	OLUME CHAN	GE = NA	
TIME	DEFL.	LOAD	TIME	DEFL.	LOAD	σ <b>3</b>
(MIN.)	(INS.)	(LBS.)	(MIN.)	(INS.)	(LBS.)	(PSI)
1.0	0.0066	405.0	1.0	0.0172	616.0	Ò
10.0	0.0085	405.0	10.0	0.0307	650.0	•
30.0	0.0098	402.0	30.0	0.0403	651.0	
60.0	0.0111	404.0	50.0	0.0458	653.0	Ó
90.0	0.0120	403.0	56.0	0.0470	653.0	100
120.0	0.0125	403.0	58.0	0.0513	660.0	100
150.0	0.0131	402.0	60.0	0.0518 0.0535	660.0 659.0	
180.0	0.0135	405.0	70.0	0.0548		İ
210.0	0.0140	404.0	80.0	-	660.0 660.0	
240.0	0.0145	403.0	90.0	0.0560 0.0579	660.0	
	0.0148	403.0	110.0			100
	0.0152	403.0	115.0	0.0585	660.0	100 200
	0.0154	402.0	118.0	0.0600	662.0	200
320.0	0.0140	115.0	120.0	0.0602	658.0	
	0.0135	115.0	130.0	0.0610	663.0	
SAMPLE N	NUMBER 97	UNIAXIAL	140.0	0.0616	665.0	
			150.0	0.0622	670.0	
TEMPERA1	TURE = $-12$	2.0° C	160.0	0.0629	670.0	200
CONSTANT	T AXIAL ST	RESS = 640	psi 163.0	0.0652	662.0	400
PERCENT	SAND = 63	3.3	1/0.0	0.0663	660.0	
PERCENT	ICE = $58$ .	8	180.0	0.0679	662.0	ı
TOTAL VO	DLUME CHAN	IGE = NA	210.0	0.0726		
			230.0	0.0757		
TIME	DEFL.	LOAD	239.0	0.0774	663.0	400
(MIN.)	(INS.)	(LBS.)	243.0	0.0804	660.0	600
			250.0	0.0809	664.0	
1.0	0.0194	639.0	260.0	0.0816	663.0	
10.0	0.0329	648.0	270.0	0.0835	665.0	
30.0	0.0429	651.0	280.0	0.0914	665.0	
60.0	0.0514	656.0	L	EAK AT 180	MIN	<del></del>
90.0	0.0571	655.0				
120.0	0.0619	659.0				
150.0	0.0659	661.0				
180.0	0.0697	663.0				
150.0	0.0659	661.0				
180.0	0.0697	663.0				
210.0	0.0734	662.0				
240.0	0.0766	663.0				
270.0	0.0798	662.0				
300.0	0.0829	662.0				
330.0	0.0861	662.0				
360.0	0.0891	662.0				
365.0	0.0895	662.0				
365.0	0.0865	120.0				
380.0	ú.0851	120.0				
	0.0031	12000				

TABLE A-2.--Continued.

SAMPLE	NUMBER	99 UNIAX	(IAL	SAMPLE	NUMBER 1	00 Continu	ed.
	ATURE = -			TIME	DEFL.	LOAD	σ3
	NT AXIAL S		640 ps1				(PSI)
	T SAND = (				0.028		
	T ICE = 95		0.70		0.0289		
IOTAL	VOLUME CHA	ANGE = -0	0.078 cc	-	0.0289		
<b>==</b>				160.0	0.0293		İ
TIME	DEFL.			170.0			200
(MIN.)	(INS.)	(LBS.)		177.0	0.0299		200
				181.0	0.032		400
1.0	0.0042			190.0	0.0329		
10.0	0.0062			200.0	0.0328		
30.0	0.0083			210.0	0.033		ľ
60.0	0.0107	645.0		220.0	0.0333		j
90.0	0.0122	645.0		225.0	0.0339		
120.0		644.0		230.0	0.0336	_	400
150.0	0.0147			240.0	0.0339		400
180.0	0.0156			243.0	0.0363		600
210.0	0.0165			245.0	0.0364		
240.0	0.0174			250.0	0.0367		1
244.0	0.0175			260.0	0.0370		j
244.7	0.0150			270.0	0.0373		l
250.0	0.0142			280.0	0.0374		1
256.0	0.0138			290.0	0.0377		İ
SAMPLE N	NUMBER 10	O STEP-	STRESS	300.0	0.0379		600
				302.0	0.0380		800
TEMPERAT	TURE = $-12$	.0°C		305.0	0.0405		800
CONSTAN	T AXIAL ST	RESS = 6	40 psi	310.0	0.0408		Ĭ
PERCENT	SAND = 63	. 8		320.0	0.0410		
PERCENT	ICE = $95$ .	5		330.0	0.0413		
TOTAL VO	DLUME CHAN	GE = -0.0	078 сс	340.0	0.0416		ı
				350.0	0.0417		800
TIME	DEFL.	LOAD	σ3	358.0			1000
(MIN.)	(INS.)	(LHS.)	(PŠI)	361.0	0.0445 0.0446		1000
			(. 0 - 7	365.0			
1.0	0.0114	668.0	0	370.0	0.0448		I
10.0	0.0146	644.0	1	380.0 390.0	0.0450		
20.0	0.0160	650.0		400.0	0.0452 0.0454		
30.0	0.0171	648.0		405.0	0.0454		1060
40.0	0.0181	650.0	i i	405.0	0.0455	655.0	1000
50.0	0.0187	645.0	)				
58.0	0.0194	645.0	0				
60.0	0.0228	644.0	100				
70.0	0.0236	650.0	1				
80.0	0.0242	649.0					
90.0	0.0249	650.0					
100.0	0.0253	650.0					
110.0	0.0259	649.0	l				
119.0	0.0264	649.0	100				
121.0	0.0275	654.0	200				

SAMPLE	NUMBER 1	O1 UNIAXIAL	SAMPL	E NUMBER 1	02 Conti	nued.
TEMPERA	TURE = -1	2.0° C	TIME	DEFL.	LOAD	
CONSTAN	T AXIAL S	TRESS = $640 p$	si (MIN.)	(INS.)	(LBS.)	
PERCENT	SAND = 6	2.9	290.7	0.0573	130.0	
	ICE = 95		291.0	0.0548		
TOTAL V	OLUME CHA	NGE = -0.012	CC 300.0	0.0530		
	•		310	0.0526		
TIME	DEFL.	LOAD	320.0	0.0523		
(MIN.)	(INS.)	(LBS.)	020.0	7,000	20000	
	•		SAMPLE	NUMBER 1	04 STEP-	STRES
1.0	0.0108	650.0				• • • • • • • • • • • • • • • • • • • •
10.0	0.0142	642.0	TEMPERA	TURE = $-1$	2.0° C	
30.0	0.0169	644.0		T AXIAL ST		50 ns
60.0	0.0195	643.0		SAND = 6		. P3
90.0	0.0214	646.0		ICE = 60		
120.0	0.0231	648.0		OLUME CHAN		
150.0	0.0246	650.0	TOTAL V	OLONE CHA	102 1171	
180.0	0.0256	648.0	TIME	DEFL.	LOAD	- 4
210.0	0.0266	649.0	(MIN.)	(INS.)	(LBS.)	σ3
240.0	0.0275	649.0	(MINO)	(1/1/2*)	(600)	(PS
270.0	0.0283	647.0	1.0	0.0265	745.0	0
300.0	0.0291	650.0	2.0	0.0324	763.0	•
330.0	0.0298	650.0				į
350.0	0.0302	650.0	3.0	0.0361	763.0	
351.0	0.0302	650.0	4.0	0.0398	766.0	l
352.0	0.0269		5.0	0.0413	766.0	,
360.0	0.0259	105.0	5.7	0.0427	766.0	0
370.0	0.0257	105.0	8.0	0.0498	772.0	100
570.0	0.0237	105.0	9.0	0.0510	777.0	1
SAMPLE N	UMBER 10	2 UNIAXIAL	10.0	0.0519	777.0	j
		L UNITATIVE	11.0	0.0527	778.0	
FMPFRAT	URE = -12	0 ° C	12.0	0.0535	778.0	
CONSTANT	AXTAL ST	RESS = 1070 p	. 13.0	0.0541	778.0	_ }
PEDCENT	SAND = 63	7 - 10/0 h		0.0543	778.0	100
	ICE = 95.		15.0	0.0575	786.0	200
			16.0	0.0582	786.0	- 1
IOTAL VO	LOME CHAIN	GE = +0.144 c	11.0	0.0588	786.0	1
T = 145"	0551		18.0	0.0592	786.0	
TIME	DEFL.	LOAD	19.0	0.0597	786.0	ı
(MIN.)	(INS.)	(LBS.)	20.0	0.0603	786.U	ı
			21.0	0.0610	786.0	200
1.0		1065.0	23.0	0.0644	776.0	400
10.0		1085.0	24.0	0.0651	780.0	1
30.0		1084.0	25.0	0.0656	776.0	
50.0		1090.0	26.0	0.0661	776.0	1
90.0		1100.0	27.0	0.0669	776.0	<b>I</b> .
20.0		1097.0	28.0	0.0686	775.0	400
50.0		1100.0				
30.0	0.0568	1098.0		LEA	к ——	
0.0	0.0591	1097.0				
.0.0		1099.0				
-		1103.0				
70.0						

0.0908

80.0

#### SAMPLE NUMBER 108 UNIAXIAL UNIAXIAL SAMPLE NUMBER 107 TEMPERATURE = -12.0° C TEMPERATURE = -12.0° C CONSTANT AXIAL STRESS = 750.0 psi CONSTANT AXIAL STRESS = 750 psi PERCENT SAND = 63.5 PERCENT SAND = 63.7 PERCENT ICE = 59.6 PERCENT ICE = 95.2 TOTAL VOLUME CHANGE = -0.054 CC TOTAL VOLUME CHANGE = NA LOAD DEFL. TIME DEFL. TIME LOAD (MIN.) (INS.) (LBS.) (MIN.) (INS.) (LBS.) 0.0269 760.0 1.0 0.0211 752.0 1.0 0.0328 757.0 2.0 10.0 0.0264 760.0 0.0377 762.0 0.0308 3.0 760.0 30.0 765.0 4.0 0.0409 0.0348 763.0 60.0 0.0437 765.0 5.0 90.0 0.0376 764.0 0.0539 768.0 10.0 20.0 0.0399 765.0 772.0 15.0 0.0614 50.0 0.0418 765.0 20.0 0.0677 773.0 80.0 0.0434 765.0 25.0 0.0733 776.0 0.0449 10.0 768.0 30.0 0.0788 778.0 0.0461 767.0 40.0 780.0 0.0843 35.0 70.0 0.0470 767.0 40.0 0.0902 783.0 190.0 0.0478 767.0 790.0 43.0 0.0945 767.0 194.0 0.0479 0.0961 788.0 44.0 196.0 0.0453 122.0 45.0 0.0978 788.0 100.0 0.0446 115.0 0.0996 788.0 46.0 0.0441 115.0 110.0 0.0932 80.0 46.7 0.0438 120.0 115.0 47.0 0.0920 80.0 80.0 48.0 0.0916 80.0 50.0 0.0911

SAMPLE N	NUMBER 10	9 STEP-	STRESS	SAMPLE	NUMBER 109	Continu	ed.
TEMPERA	TURE = -12	e° C		TIME	DEFL.	LOAD	σ3
CONSTAN'	T AXIAL ST	RESS = 4	00 psi	(MIN.)		(LBS.)	(PSI)
	SAND = 63		•	330.0	0.0339	411.0	1
PERCENT	ICE = $95$ .	5		340.0	0.0340	405.0	
TOTAL VO	OLUME CHAN	IGE = -0.	072 cc	350.0	0.0341	410.0	
				359.0	0.0343	410.0	800
TIME	DEFL.	LOAD	σ3	362.0	0.0365	410.0	1000
(MIN.)	(INS.)	(LBS.)	₹PŠI	370.0	0.0368	410.0	1
				380.0	0.0371	405.0	
1.0	0.0125	400.0	Ò	390.0	0.0373	410.0	
10.0	0.0147	404.0	ĺ	400.0	0.0376	405.0	
20.0	0.0155	400.0		410.0	0.0377	405.0	i
30.0	0.0161	405.0		413.0	0.0378	411.0	1000
40.0	0.0165	405.0				_	
50.0	0.0169	406.0	I	SAMPLE	NUMBER 11	1 UNIAX	IAL
59.0	0.0171	404.0	0			_	
61.0	0.0204	407.0	100		ATURE = $-12$		
70.0	0.0207	404.0	1		NT AXIAL ST		'50 psi
80.0	0.0210	405.0			T SAND = 63		
90.0	0.0214	406.0			T ICE = 70.		
100.0	0.0227	405.0		TOTAL	VOLUME CHAN	GE = NA	
110.0	0.0219	405.0	}				
120.0	0.0221	405.0	100	TIME	DEFL.	LOAD	
122.0	0.0231	409.0	200	(MIN.)	(INS.)	(LBS.)	
130.0	0.0234	409.0		_			
140.0	0.0238	405.0		1.0	0.0158	750.0	
150.0	0.0240	406.0		10.0	0.0250	756.0	
160.0	0.0242	405.0		30.0	0.0330	764.0	
170.0	0.0243	405.0		60.0	0.0391	767.0	
180.0	0.0245	409.0		90.0	0.0431	767.0	
182.0	0.0246	409.0	200	120.0	0.0459	767.0	
185.0	0.0266	408.0	400	150.0	0.0483	768.0	
190.0	0.0268	410.0	1	180.0	0.0502	767.0	
200.0	0.0270	405.0		210.0	0.0519	770.0	
210.0	0.0273	411.0		240.0	0.0534	770.0	
220.0	0.0274	405.0		270.0	0.0547	770.0	
230.0	0.0276	405.0		300.0	0.0559	770.0	
240.0	0.0277	410.0		330.0	0.0571	770.0	
241.0	0.0277	410.0	400	360.0	0.0584	772.0	
243.0	0.0298	410.0	600	390.0	0.0594	772.0	
250.0	0.0302	408.0	1	420.0	0.0602	772.0	
260.0	0.0304	405.0		450.0	0.0611	772.0	
270.0	0.0305	410.0		480.0	0.0621	773.0	
280.0	0.0307	405.0		510.0	0.0629	773.0	
290.0	0.0309	405.0		530.0	0.0634	772.0	
300.0	0.0311	410.0		530.7	0.0582	108.0	
304.0	0.0312	410.0	600	533.0	0.0566	108.0	
307.0	0.0333	407.0	800		<b>4 4 5 5 6 6</b>		
310.0	0.0334	407.0	1				
320.0	0.0337	405.0					
	U U U U U I		•				

190.0

200.0

205.0

0.0637

0.0643

0.0647

0.0650

- LEAK -

660.0

662.0

662.0

663.0

SAMPLE NUMBER	112	STEP-STRESS	SAMPLE NUMBER	113	STEP-STRESS
SAMPLE NUMBER	116	31EF-31KE33	SAMPLE NUMBER	113	O LEP O I KE O

TEMPERATURE = -12.0° C CONSTANT AXIAL STRESS = 640 ps PERCENT SAND = 64.0 PERCENT ICE = 60.0 EST. TOTAL VOLUME CHANGE = NA TEMPERATURE = -12.0° C
CONSTANT AXIAL STRESS = 400 psi
PERCENT SAND = 63.1
PERCENT ICE = 60.0 EST.
TOTAL VOLUME CHANGE = NA

TIME (MIN.)	DEFL. (INS.)	LOAD (LBS.)	σ3 (PSI	TIME (MIN.)	DEFL. (INS.)	LOAD	σ3 (PSI)
1.0	0.0180	648.0	0	1.0	0.0124	407.0	ọ
5.0	0.0255	650.0		10.0	0.0192	405.0	· 1
10.0	0.0303	654•V	ł	30.0	0.0243	406.0	j
20.0	0.0357	655 <b>•</b> 0	- 1	60.0	0.0283	406.0	j
30.0	0.0395	653.0	1	62.0	0.0286	406.0	0
40.0	0.0423	655.0		64.0	0.0320	405.U	100
50.0	0.0446	655.0		70.0	0.0330	407.0	1
60.0	0.0464	652.0	Ò	90.0	0.0348	407.0	l
62.0	0.0502	656.0	100	120.0	0.0365	410.0	j
70.0	0.0515	654.0	1	122.0	0.0366	410.0	100
80.0	0.0527	657.0	i	124.0	0.0382	414.0	200
90.0	0.0538	657.0		130.0	0.0391	412.0	1
100.0	0.0547	657.0		150.0	0.0424	411.0	
110.0	0.0556	660.0		180.0	0.0476	410.0	
120.0	0.0565	660.0	100	182.0	0.0478	410.0	
123.0	0.0581	663.0	200		LEAK		
130.0	0.0587	663.0	200				
140.0	0.0593	660.0					
150.0	0.0598	662.0					
160.0	0.0603	665.0					
170.0	0.0607	665.0	-				
			200				
180.0	0.0611	661.0	200				

400

TABLE A-2.--Continued.

SAMPLE !	NUMBER 11	4 UNIAXIAL	SAMPLE I	NUMBER 11	7 STEP-S	TRESS	
CONSTAN' PERCENT PERCENT	SAND = 64 ICE = 68.	RESS = 750 PS1 .2 5	TEMPERATURE = -12.0° C CONSTANT AXIAL STRESS = 750 psi PERCENT SAND = 63.6 PERCENT ICE = 60.5 TOTAL VOLUME CHANGE = NA				
TOTAL V	OLUME CHAN	GE - NA	TOTAL V	DEOME CHAN	GE III		
TIME (MIN.)	DEFL.	LOAÜ (LBS.)	TIME (MIN.)	DEFL. (INS.)	LOAD	σ3 (PSI)	
1.0	0.0239	751.0	1.0	0.0344	750.0	0	
10.0	0.0393	762.0	2.0	0.0399	765.0	1	
30.0	0.0501	765.0	3.0	0.0438	765.0	ı	
60.0	0.0583	770.0	4.0	0.0475	770.0		
90.0	0.0636		5.0	0.0502	770.0		
120.0	0.0677		6.0	0.0524	770.0	i	
150.0	0.0709		7.0	0.0544	770.0	1	
180.0	0.0740	775.0	8.0	0.0562	770.0	1	
210.0	0.0766		9.0	0.0578	770•0	į	
220.0	0.0775	780.0	10.0	0.0592	770.0	0	
230.0	0.0784	780.0	12.0	0.0644	775.0	100	
	0.0793	780.0	13.0	0.0655	775.0	1	
240.5	0.0756	100.0	14.0	0.0663	776.0	I	
241.0	0.0741	100.0	15.0	0.0672	776.0	1	
245.0	0.0729	100.0	16.0	0.0679	777.0	100	
250.0	0.0723	100.0	18.0	0.0704	776.0	200	
-			19.0	0.0712	776.0	1	
SAMPLE I	NUMBER 11	5 CONFINED	20.0	0.0717	780.0	1	
			21.0	0.0724	780.0	1	
TEMPERA	TURE = $-12$	.0° C	22.0	0.0729	780.0	İ	
		RESS = 750 psi		0.0732	782.0	į	
PERCENT	SAND = 63	. 2	24.0	0.0736	780.0	Ì	
PERCENT	ICE = $95.9$	y 	25.0	0.0740	780.0		
TOTAL V	OLUME CHAN	GE = -0.012  cc		0.0744	780.0		
		E = 210 psi	27.0	0.0747	780.0	200	
TIME	DEFL.	LOAD	29.0	0.0770	780.0	400	
(MIN.)	(INS.)	(LBS.)	30.0	0.0774	780.0		
			31.0	0.0778	780.0		
1.0	0.0163	750.0	32.0	0.0780	780.0	1	
10.0	0.0209	758.0	33.0	0.0783	780.0		
30.0	0.0249	762.0	34.0	0.0786	780.0		
60.0	0.0283	762.0	35.0	0.0789	780.0	j	
90.0	0.0306	762.0	36.0	0.0791	780.0		
120.0	0.0324	762.0	37.0	0.0793	780.0		
150.0	0.0340	762.0	38.0	0.0796	780.0		
180.0	0.0353	767.0	39.0	0.0797	780.0	1	
210.0	0.0364	767.0	40.0	0.0799	780.0	400	
240.0	0.0374	767.0	41.0	0.0801 0.0825	780•0 780•0	600	
270.0	0.0383	767.0	43.0 45.0			. 1	
300.0	0.0391	767.0	45.0	0.0829	780.0	ı	

TABLE A-2.--Continued.

SAMPLE	NUMBER 117	'-Continu	ed.	SAMPLE	NUMBER	118 CONFINED	
TIME	DEFL.	LOAD	σ3	TEMPERA	ATURE = -	12.0° C	
(MIN.)	(INS.)	(LBS.)	(PSI)		NT AXIAL	STRESS = 750 ps	ij
47.0	0.0833	780.0	1		T SAND =		
49.0	0.0836	780.0	1		T ICE = 9		
51.0	0.0838	785.0	1			ANGE = $-0.216$ c	: C
53.0	0.0841	785.0				URE = 600 psi	
55.0	0.0844	785.0		TIME	DEFL.		
57.0	0.0849	785.0		(MIN.)	(INS.	) (LBS.)	
59.0	0.0851	785.0	i				
61.0	0.0853	785.0		2.0	0.0192		
64.0	0.0877	780.0	800		0.0227		
67.0	0.0883	783.0	1	30.0	0.0266		
70.0	0.0888	784.0		60.0	0.0298		
75.0	0.0893	785.0	İ	90.0	0.0324		
80.0	0.0898	785.0		120.0	0.0342		
85.0	0.0901	785.0		150.0	0.0357		
90.0	0.0905	785.0		180.0	0.0371		
95.0	0.0907	785.0		210.0	0.0381		
100.0	0.0909	785.0	800	240.0	0.0390		
104.0	0.0896	775.0		270.0	0.0398		
105.0	0.0896	775.0		276.0	0.0327		
115.0	0.0896	775.0		280.0	0.0322		
120.0	0.0899	775.0		290.0	0.0317		
130.0	0.0901	775.0		300.0	0.0315		
135.0	0.0902	775•0		310.0	0.0313		
137.0	0.0904	775.0		SAMPLE	NUMBER 1	19 CONFINED	
142.0	0.0883	775.0	400			0 00 0	
145.0	0.0885	775.0	1		TURE = -1		
150.0	0.0886	775.0	- 1			STRESS = 650 ps	1
155.0	0.0887	775.0	Į		SAND = 6		
160.0	0.0889	775.0	400		ICE = 60		
165.0	0.0889	775.0				NGE = NA	
170.0	0.0862	775.0	200			RE = 205 psi	
180.0	0.0864	775.0	1	TIME	DEFL.	LOAD	
190.0	0.0866	775.0	200	(MIN.)	(INS.)	(LBS.)	
195.0	0.0867	775.0	200		0 0005	<b>(50.0</b>	
200.0	0.0842	775.0	0	1.0	0.0225	650.0	
210.0	0.0856	775.0		10.0	0.0309	650.0	
220.0	0.0868	775.0	- 1	20.0	0.0346	650.0	
230.0	0.0878	775.0	1	30.0	0.0373	656 <b>•</b> 0	
240.0	0.0887	775.0	Ī	40.0	0.0397	656.0	
250.0	0.0897 0.0900	775•0 775•0		50.0	0.0423	656.0	
253.0 254.0	0.0819	75.0		60.0	0.0450	656.0	
255.0	0.0806	75.0	1	70.0	0.0474	656.0	
260.0	0.0300	75.0		0.08	0.0506	656.0	
265.0	0.0790	75.0	l,	90.0	0.0534	656 <b>•</b> 0	
270.0	0.0789	75.0		100.0	0.0564	656.0	
274.0	V.0787	75.0		10.0	0.0597	656.0	
217.0	V. VIOI	, , , ,		50.0	0.0632 0.0757	656•0 656•0	
			-		- LEAK -		
					LLAK -		

TABLE A-2.--Continued.

SAMPLE	NUMBER 1	20 CONF	INED	SAMPLE	NUMBER 121	-Continue	d.
TEMPER	ATURE = -1	2.0° C	640 ==	TIME	DEFL. (INS.)	LOAD (LBS.)	σ3 (PSI)
CONSTA	NT AXIAL S	1KE22 =	040 ps	1(MIN.)	(1113.)		(131)
	T SAND = 6			120.0	0.0367		100
	T ICE = 64		,	122.0	0.0368		200
	VOLUME CHA			124.0	0.0379		200
	ING PRESSU		ppi	130.0	0.0383	*	1
TIME	DEFL.			140.0	0.0389		ı
(MIN.)	(INS.)	(LBS.)	,	150.0	0.0394		1
	0 0204	/FF 0		160.0	0.0399		l
2.0	0.0394			170.0	0.0403		
5.0	0.0438			180.0	0.0407		200
10.0	0.0473			181.0			200
20.0	0.0510	660.0		183.0	0.0427		400
30.0	0.0531			190.0			
60.0	0.0566	662.0		200.0	0.0437		
90.0	0.0585			210.0	0.0441		
120.0	0.0597			220.0	0.0445		[
150.0	0.0606	660.0		230.0	0.0449		
180.0	0.0614			240.0	0.0451		1
210.0	0.0619			243.0	0.0452		400
240.0	0.0624			245.0	0.0482		600
260.0	0.0628	665.0		250.0	0.0485	767.0	l
				260.0	0.0488	767.0	l
SAMPLE !	NUMBER 12	1 STEP-S	TRESS	270.0	0.0490	767.0	İ
				280.0	0.0493	767.0	j
TEMPERA'	TURE = $-12$	.0° C		290.0	0.0497	767.0	
CONSTAN	T AXIAL ST	RESS = 7	'50 psi	300.0	0.0500	767.0	ı
	SAND = 62			304.0	0.0501	767.0	600
PERCENT	ICE = $95$ .	5		306.0	0.0515	770.0	800
TOTAL V	DLUME CHAN	GE = -0.	.048 cc	310.0	0.0517	770.0	ļ
				320.0	0.0521	770.0	ļ
TIME	DEFL.	LOAD	σ3	330.0	0.0524	770.0	
	(INS.)	(LBS.)	(PSĬ)	340.0	0.0526	770.0	1
_			( 7	350.0	0.0529	770.0	İ
1.0	0.0170	755.0	0	360.0	0.0530	770.0	Į
10.0	0.0216	760.0	i	365.0	0.0532	770.0	800
20.0	0.0237	760.0	Ì				Ou u
30.0	0.0252	757.0					
40.0	0.0266	757.0	İ				
50.0	0.0278	760.0	Ì				
60.0	0.0288	757.0	l				
61.0	0.0288	757.0	0				
63.0	0.0325	760.0	100				
70.0	0.0332	759.0	1				
80.0	0.0352	763.0					
90.0	0.0347	761.0					
100.0	0.0354	761.0					
110.0	0.0361	757.0					
	444301		I				

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