AN ANALYTICAL AND EXPERIMENTAL INVESTIGATION OF CONTACT AREA STRESS DISTRIBUTION AND BUCKLING STRENGTH OF LIGHT GAUGE PUNCHED METAL HEEL PLATES FOR TIMBER TRUSSES

> Thesis for the Degree of Ph. D. MICHIGAN STATE UNIVERSITY ISAAC SHEPPARD, JR. 1969

THESIS



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#### thesis entitled

AN ANALYTICAL AND EXPERIMENTAL INVESTIGATION OF CONTACT AREA STRESS DISTRIBUTION AND BUCKLING STRENGTH OF LIGHT GAUGE PUNCHED METAL HEEL PLATES FOR TIMBER TRUSSES

presented by

Isaac Sheppard, Jr.

has been accepted towards fulfillment of the requirements for

Ph.D. degree in Agr. Eng.

Merle L'Esmay Major professor

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### ABSTRACT

### AN ANALYTICAL AND EXPERIMENTAL INVESTIGATION OF CONTACT AREA STRESS DISTRIBUTION AND BUCKLING STRENGTH OF LIGHT GAUGE PUNCHED METAL HEEL PLATES FOR TIMBER TRUSSES

### By

Isaac Sheppard, Jr.

The purpose of this investigation was to develop a simple testing procedure and make a theoretical and experimental study of the contact area stresses and buckling stresses of light gauge metal heel plates used on wood trussed rafters.

A small, hand-operated hydraulic cylinder was mounted in a specially designed jig to apply a concentrated load at the peak of 8'-0" long triangular trusses. By mounting a dial gauge on the joint, load-deflection data was obtained.

A theoretical investigation developed the theory of contact area stresses in accordance with recent work on nailed joints and other analyses that combine direct stresses vectorially with eccentric, or rotational, stresses to get critical combined stresses. Methods of computing tensile stresses in heel plates, shear streses, and bending stresses on small elements, are presented.

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An initial comparison of six plate sizes, shapes, and orientations revealed that contact area stresses were not significantly different for any of the plates studied at 0.015" heel joint deflection. At ultimate load, however, those plates 2-3/4" to 3-3/4" wide, and lengths from two to three times their width were best, and were 20% to 50% stronger than the next three. These two strong joint types were more than twice as good as the worst group, 5"x7", placed the "wrong way."

A detailed study of surface strains using Stress-Coat brittle lacquer revealed that the shear stress in the steel is highest directly over the joint between members; that corner teeth are initially stressed quite highly; but that even at loads that cause buckling, large areas of wider plates are not stressed significantly. It was concluded that heel plates should be kept to a lesser width to better utilize contact area strength and prevent an erroneous feeling of confidence due to excessive width of the heel plates.

In a first preliminary comparison of 24 matched specimens (two repetitions each): 8'-0" vs. 24'-0"; Douglas fir vs. white fir; 3"x5", 3"x8", and 5"x5" heel plates; all evaluated at 0.015", 0.040", 0.080", and 0.150" heel deflection; it was found that:

 The heel joints for 8'-0" specimens were 8% stronger than those on 24'-0" matched trusses.

2. The white fir heel joints were only 70% as strong as Douglas fir joints.

3. The 3"x5" and 3"x8" plates were almost identical, on a psi basis, but both were about 20% stronger than the 5"x5" plates.

4. Contact area stress was affected by several twoway interaction effects.

A second preliminary comparison verified these conclusions, plus showing there was no significant difference between 8'-0" specimens tested on the hand-operated jig and matched 8'-0" specimens tested on a Riehle mechanical testing machine.

A final analysis of variance comparison, performed with a least squares statistical routine on a Control Data Corp. 3600 computer, included the variables mentioned earlier, plus moisture content and specific gravity, along with their squares, as covariants, and was based on the load-deflection data from 56 different test specimens. This final comparison confirmed the earlier conclusions, plus finding that moisture content affects contact area stress significantly. Multiple correlation coefficients were computed that accounted for 91% of the variance and a contact area stress prediction equation was developed, with predicted stress being compared with measured stress for four deflection readings on each specimen.

A comparison of the theoretical results with the experimental tests showed that a simple axial stress calculation of contact stress, in the P/A manner, is a better predictor of test results than the theoretical method proposed. The experimental work led to recommendations for heel joint design that are also included.

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By

Isaac Sheppard, Jr.

# A THESIS

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## DOCTOR OF PHILOSOPHY

Department of Agricultural Engineering

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### INTRODUCTION

The twenty year period, 1948-1968, has seen the use of wood trussed rafters grow from an almost infinitesimal beginning to a major market factor. Trussed rafters are now used on about half of all single family residential construction, as well as on a large share of agricultural, and a significant share of commercial and industrial construction. The trussed rafter has the advantages of greater strength, more uniformity, and lower cost as opposed to conventional joistand-rafter construction. Greater spans without supports, faster construction and other benefits are provided by trussed rafters, too.

Trussed rafters, commonly called "trusses," may be built with any structurally suitable joint system to attach the wood framing members. Split-rings, nail-glued plywood gussets, bolts, nails, light gauge metal gusset plates, and other connector types have been used. The light gauge metal gusset plate has essentially taken over the market now, having displaced the other joint types due to its lower cost, faster fabrication, and easier shipment of completed trusses.

Many tests have been performed to insure that the truss plates have adequate tooth values or nail values and tensile strength. Other tests have been performed on completed trusses to show the over-all truss design to have adequate

strength. While both these sets of tests have shown structural adequacy, there have been only minor attempts to analyze the shear stresses, buckling stresses, and eccentric forces that affect the heel joint, where the bottom chord and top chord meet. Since this joint is subject to a more complex set of forces and stresses than any of the other truss joints, and since it requires more steel than any other joint, a more elaborate study of it seems warranted. This project is intended to answer that need.

### CHAPTER I

### **REVIEW OF LITERATURE**

The design loads on trusses are usually specified by local building codes or nationally recognized building codes such as the "Basic Building Code" (1965), the "Uniform Building Code" (1967), the "Southern Standard Building Code" (1967), or the "National Building Code of Canada" (1966). Where no building code governs, the requirements of the Federal Housing Administration (1966), the United States of America Standards Institute, or, in the case of farm buildings, by the American Society of Agricultural Engineers (1967) may be used. Local climatological data is available for more detailed study from the Dept. of Commerce (1968).

The lumber used in trussed rafters has been standardized as to grades and strength by the official grading associations, Western Wood Products Association (1965) for west coast woods, and the Southern Pine Inspection Bureau (1968) for southern woods. These lumber allowable stresses, plus connector values for bolts, split-rings, nails, etc., are all published in one booklet by the National Forest Products Association (1968). The properties of individual species are given in separate reports by Littleford on Douglas fir (1967) and the Forest Products Laboratory on

western hemlock (1965) and southern pine (1966). Strength and related properties of Canadian woods are summarized by Kennedy (1965). Probably the most important thing, the factor of safety, has been described in detail as a multivalued characteristic by Wood (1958).

The background testing for the lumber grading rules and specifications has been performed under the American Society for Testing and Materials (A.S.T.M.) Designation D 245-67T (1967). The "strength ratio" related these tests of small, clear specimens to structural size by allowing for the reduction effect of knots, slope of grain, and other strength-reducing characteristics. The "strength ratio" is discussed by the Forest Products Laboratory in the "Wood Handbook" (1955).

Non-destructive testing of lumber has been described by McKean (1962, 1963), Bolger (1962), Miller (1962), Sunley (1962), Senft (1962), and Wood (1964). This non-destructive testing, commonly called "machine grading," permits more uniform strength standards for timber based on a statistical correlation of strength with flatwise stiffness.

Recent arguments of "green" (unseasoned) vs. "dry" (moisture content of 19% or less) lumber are being resolved through a set of "green" sizes and allowable stresses that match the existing size standard, but a set of equivalent "dry" sizes with smaller dimensions to account for shrinkage. The ratio of dry to green clear wood properties has been determined by A.S.T.M. in D-2555 (1967). These equivalent

"dry" sizes were recommended by the Forest Products Laboratory (1964) on the basis of stiffness and shrinkage tests of green and dry joists.

The engineered use of nails for connections in wood structural members, particularly trusses, has been extensively reported by Stern (1952 through 1967). Nailed joint rigidity was studied by L. L. Boyd (1959) and rotational resistance of three-membered nailed joints was reported by Perkins (1962).

The use of nail-glued plywood gussets for wood trusses has been extensively investigated by Radcliffe (1954, 1956), J. S. Boyd (1955), Countryman (1954), Angleton (1960), and Suddarth (1961). A digital computer W-truss analysis program was developed by Suddarth (1964) for symmetric trusses with rigid joints (nail-glued plywood) or various combinations of rigid and pinned joints.

The design of light gauge metal connector plates with wood trussed rafters has been covered by the Truss Plate Institute's (T.P.I.) "Design Specifications for Light Metal Plate Connected Wood Trusses" in various editions (1962, 1965, 1966, 1968). These metal plates of every different manufacturer have been subjected to a large number of tensile tests, following either the T.P.I. procedure or the more recent A.S.T.M. procedure Designation D 1761-68 (1968). A tensile test has been proposed by Dudley, 1966, and A.S.T.M., 1968, to help evaluate the net tensile strength of steel, in addition to the strength of the truss plate teeth.

Deflection and creep characteristics of trussed rafters with metal plate fasteners were reported by Sliker (1965). The effect of three different types of metal plates, as compared to nail-glued plywood, as well as variations in moisture content, was reported by Radcliffe (1964). Moisture content cycling of trussed rafter joints was reported by Wilkinson (1966). An extensive series of Canadian trussed rafter tests to develop general performance criteria was reported by Hansen (1963). The effect of member stiffness and moisture content history on the deflection behavior of trusses fastened with metal plates was reported by Kawal (1965).

Suddarth (1963) reported on a detailed analytic study of W-trusses made with metal gusset plates, including the moment-rotation effect at the heel joint. This was his initial study, and reported that

A workable formula for the rotational slippageresisting moment relationship has been devised and tested for nailed joints with wood gussets by Perkins (1962). (He was referring to Perkins' conclusion that the torsion formula for the force on the extreme nail is suitable.) As yet, unpublished pilot experiments with short-tooth, long-tooth and nailed metal gusset plates have shown that the same fundamentals apply to the same degree. The rotation-moment formula is derived from the load-slip characteristics of a single fastener and considers the arrangement of the fasteners about their centroid.

Suddarth continued his study to analyze a 26'-8" span, 3/12 slope, 2"x4" W-truss as if it had rigid joints, then as if it had pinned joints but continuous chords and assumed that actual member moments in this metal plate connected truss lie between those obtained in these two cases.

A second report by Suddarth (1964) also concerned the fastener stresses, particularly the moment resisting capacity of metal plate joints. He reiterated his earlier conclusion (noted in the preceding paragraph). He also described a heel plate reduction ratio,  $P_k/F_{ki}$ , in which;

- F<sub>ki</sub> = extreme force on an individual fastener due to moment being transferred at the joint.

Suddarth's reduction ratio for 24' trusses with short-tooth metal plates varied as follows:

Pitch	Top Area	Bottom Area	Ave.
2½/12	.906	.848	.877
4/12	1.045	.616	.732
6/12	1.113	.527	.820

These percentages of allowable heel plate connector values were later adjusted to a uniform scale and adopted by the Truss Plate Institute (T.P.I.) as a practical engineering means of heel plate design to account for loss in heel strength due to moment transfer and eccentricity.

The Federal Housing Administration in its "Trussed Rafter Criteria" (1960) has always required a heel plate analysis based on the net vertical reaction, the distance from the intersection of member centerlines, and the polar section modulus of the heel plate. The FHA requirement is described in more detail under "Typical Calculations" and illustrated in Figure 8. Misra (1966) studied the stress distribution in the punched metal plates at a straight tension joint and concluded that even for this type of joint the tensile stresses are not uniform. The maximum stress he calculated was 2.4 times the average, and was based on the distance from centerline of joint to tensile area being considered, much like rows of rivets at a riveted joint. He used a difference equation, as well as the principle of minimum complementary energy to predict stresses and got good agreement with experimental results.

Der-chun Lee (1965) did an experimental analysis of a king-post truss with semi-rigid joints, measuring the relative rotation of the top chord with respect to the bottom chord by means of the Moire Fringe effect. He assumed the rafter member is supported by a continuous elastic foundation, i.e., by equally spaced nails, which yielded analytical results reasonably close to those found experimentally.

Ivan Dah-Wu Chow (1965) worked along with Der-chun Lee on the analytical work and reported that the analytic results, using the assumption of semi-rigid joints, were closer to experimental results than the assumption of rigid joints.

## CHAPTER II

## PURPOSE

The purpose of this investigation was to develop a simple testing procedure and make a theoretical and experimental study of the contact shear stresses and the buckling stresses of light gauge metal heel plates used on wood trussed rafters. The specimens tested were fabricated with a variety of truss plate sizes from each of two manufacturers. Three different species of lumber were used.

### CHAPTER III

### THEORETICAL INVESTIGATION

The theoretical analysis of the heel joint was made by first describing the types of failure known to occur. These failure types are all caused by overstress. The next step, therefore, was an attempt to develop a rational design through prevention of premature failure by consideration of the types of overstresses that resulted in failure.

### Types of Heel Joint Failure

Assuming that the metal gusset plate is sufficiently strong to be properly impaled, there are four types of failure that can occur at the heel joint:

Tensile Failure

Tensile failure can occur when the length of plate in tension (and consequently the number of teeth) exceed the "development length."

"Development length" refers to primary tensile joints and means the length of truss plate contact area necessary on each side of the joint to balance the net steel section in tension at the critical location.

The development length is similar to the minimum permissible anchorage for reinforcing bars in reinforced concrete



construction. Development length in that case refers to the bar length that must be used to develop the strength of the reinforcing bar. The concept has been described in detail by Ferguson (1958).

When the contact area exceeds the development length, as when a longer plate is used, no extra strength is gained because the plate will fail in tension. The extra length, beyond the "development length" may add to better appearance, but can not increase the strength because the net tensile strength limits the joint performance.

This concept of development length is a means of assuring that contact area and net tensile section are both considered as possible limitations on joint strength. When riveted joints are designed in steel construction, both shear area of the rivets, as well as bearing area on the connected parts, must be checked, with the more limiting factor governing design. In the case of punched metal truss plates, connecting timber tension joints, both contact area on the wood and net tensile section of steel must be considered and the design is limited by the smaller value. Development length is the minimum length required for the contact area to develop the tensile capacity.

Truss plate areas shorter than the development length will be limited by their contact area stress, whereas those truss plate areas longer than the development length will be limited by net tensile capacity. Development length, then,
is a convenient expression of the maximum contact length that may be used without being limited by the net tensile strength of the steel.

The development length is affected by the truss plate's thickness, percentage of holes, and yield or ultimate tensile stress of the steel being used. In addition, since the tooth, nail, or plug value of the truss plate contact area is dependent on the density, specific gravity and species of lumber, these wood properties affect development length too. Development length is a property of both the truss plate and the lumber. The same connector plate will have a longer development length in balsa wood, due to its lesser nail holding power, than in white oak.

For a heel joint to fail in tension, the contact area of the plate provides more strength than the tensile crosssection. While this type of failure is much more common at true tensile joints (such as lower chord splice joints), it can be a factor in heel joints that are placed parallel to the bottom chord. The triangular contact areas on the top and bottom chord develop increasingly large tensile stresses in the small isthmus between teeth at the smallest end of the triangular area. See Figure 1.

Tensile failures can be prevented by providing more net section of steel, either by thicker or wider truss plates, or by reducing the percentage of holes in the truss plate surface, or by properly positioning the plate to prevent excessive tensile stresses.

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Figure 1. Tensile failure at heel plate.



Figure 2. Plate buckling along shear line.

Tooth Failure

Tooth failure refers to withdrawal of the teeth from the wood. Normally this occurs by progressive enlargement or elongation of the entrance area of the hole which the tooth makes in the wood during impalement. As this entrance area of the hole becomes more and more elongated (due to exceeding the bearing capacity of the wood) the tooth attempts to follow the slope of the hole by bending. The further the tooth bends, the more nearly it is loaded in withdrawal (as opposed to its typical shear loading). Eventually, the tooth is bent nearly 45° back from vertical and pulls out of the hole entirely.

It has been found that teeth being bent back toward their original hole in the parent steel are more vulnerable, less rigid, and weaker than teeth which are being bent further away from their original plane (within the parent steel). However, that was outside the area of this research and was not investigated further.

## Wood Failure

Wood failure occurs when the truss plate teeth essentially retain their original shape and direction, yet tear through the wood fiber. Wood failure results from the tooth exceeding the bearing capacity, and/or the shear parallel to grain capacity, of the wood. It may be counteracted by either choosing a denser species or by increasing the size of the metal plate. Wood failure and tooth failure are inter-related.

**4** .-

Buckling Failure

Buckling failure occurs along the shear line (i.e., the crack between the top and bottom chords) and is related to truss plate thickness, size and shape of holes (or more precisely, the isthmus size, shape, and thickness between holes), orientation of holes to the shear line (i.e, parallel to it, perpendicular, or some angle in between) and size and shape of over-all truss plate contact area. See Figure 2.

# Description of Stresses in the Heel Plate

It has already been established by Misra in a straight tensile test that the stresses in the isthmus between holes in the surface of the plate vary approximately linearly with each row of teeth from the end of the plate to the tensile joint. This verifies the commonly held belief that each tooth provides equal value. However, this is only true where it is a straight tensile joint with no eccentric effect. Further, Misra showed that the teeth, holes, and metal between holes of a thin truss plate behaved exactly the same as the theory has always been for rivets making tensile joints, as for example, relatively thick boiler plate.

At a heel joint, there are both axial forces and eccentric forces, due to the type of joint. The description of these two types of forces, as they affect heel joints, follows:

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Axial Contact Area Stresses

Axial contact area stresses which result from the direct forces in the members must be contained and resisted by the joints. These so-called axial forces, then, must move toward the surface of the member in the vicinity of the truss plate. They may move considerably away from the axis of the member. It is possible to place a truss plate in such a position that it fits less than half way onto one of the members, thereby not even passing over the axis of the member. See Figure 3.

Since the members are mono-planar in a metal plate connected wood truss, the heel gusset plate can not occur at the intersection of center lines because the lower chord butts into the bottom edge of the upper chord. It is essential that the direct forces in the members be taken by the metal plate at this contact line between the members. By keeping the metal plate essentially centered over the crack, half the contact area will be on the top chord and half will be on the bottom chord. Then, making the usual assumption, there will be a uniform load on the teeth due to these axial forces.

### Eccentric Contact Area Stresses

Eccentric contact area stresses are caused by the eccentric force, or rotational moment, brought into play by the fact that the two contact areas (one on the top chord and the other on the bottom chord) each have their own distinct centroids and that these centroids are separated by a certain distance, e. See Figure 4.





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To determine the magnitude of this rotational moment, both the size and direction of the forces must be known, as well as the distance between centroids of their respective contact areas. It would first appear that the magnitude and direction of the axial forces could be used, but closer inspection shows that these are not in fact equal or opposite since the top chord is on a slope and has a larger force than does the bottom chord.

- a. The horizontal torsion component results from the force in the bottom chord contact area. This force must be parallel to the chord since there is no vertical component (except when the top chord is birdsmouthed to bear on the support, letting the bottom chord hang in such manner that any ceiling load must be transmitted vertically into the top chord by the connector plate). This means that the force on the top chord contact area must be equal and opposite, rather than parallel to the slope of the top chord.
- b. The vertical component of the top chord force must be transferred directly to the support from the top chord by crushing on the very small feather end of the scarf cut of the bottom chord. This is due to the tight fit between chord members at the heel joint. A tight fitting heel joint is the general rule since it is the simplest joint to cut, easy to

clamp together in a jig, easy to inspect, and the wood-to-wood contact area is longer than other joints. See Figure 5.

c. The rotational moment is due to the vertical distance, e, between the centroids  $(c.g._u)$  of the upper chord contact area and the centroid  $(c.g._b)$ of the bottom chord. This concept is illustrated in Figure 6.

### Shear Stress in the Steel

Shear stress exists in the steel, being a maximum directly over the crack, since the top chord area is in compression and the bottom chord in tension. The heel plate must resist the entire axial force of both member, causing these shear stresses. Since the members are very large and stiff, compared to the plate, which results in the shear stress being essentially uniform along the shear crack.

# Proposed Heel Joint Contact Stress Calculation Method

The direct stress, b, is found by dividing the axial force, c, by the "effective" contact area  $A_{t.c.}$ , ("effective" area means that the nails within 1/4" edge distance or 1/2" end distance, assumed too close to the crack to be useful, have not been counted).

The eccentric moment stress, c, is found by multiplying the force under consideration by the distance, e, to the opposite force, and dividing this quantity by the polar section modulus,  $Z_p$ .

\$



Figure 5. Vertical forces taken by wood-to-wood bearing.



Rotational moment. Figure 6.

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The direct stress, b, and the eccentric moment stress, c, must be added vectorially,  $b \leftrightarrow c = a$ . The resultant, a, therefore depends on the angle, A, between "b" and "c," as well as on their relative quantities. This vectorial addition may be performed by the use of the Cosine Law,  $a^2 = b^2 + c^2 - 2bc \cos A$ . By noting which direction the vectors "b" and "c" point with respect to each other at each corner, the critical corner can be located so the Cosine Law solution need be applied only once, instead of at all four corners. Normally, the critical corner will be the outermost top chord corner, due to its having the largest angle, A, between "b" and "c" because of the effect of the top chord slope. See Figure 7.

# <u>Comparison of Existing Heel Joint</u> Analysis Methods

There are several alternate procedures for determining heel joint contact shear stress, as described below:

# General Method

The general requirement of heel joint analysis is that the connections be designed to provide adequate capacity for the direct axial forces at the joint involved. Normally the effects of eccentricity would be neglected by most engineers not familiar with the FHA or TPI requirements mentioned in the Review of Literature.





### TPI Method

The Truss Plate Institute requires, in their specification, TPI-68 that:

> To allow for moment effects at the heel joint, design the heel plate to have sufficient capacity to withstand the direct axial stress of the top and bottom chords by their respective nail, tooth, or plug groups, with the following reductions in allowable nail, tooth, or plug load:

> Under 3/12 slope85% of allowable3/12 to less than 4/12 slope80% of allowable4/12 to less than 5/12 slope75% of allowable5/12 to and including 5½/12 slope70% of allowableOver 5½/12 slope65% of allowable

### FHA Method

FHA requires that the eccentric moment be found by multiplying the net reaction,  $R_n$ , at the support, by the distance, e, measured from the intersection of center-lines of the top and bottom chord to the centroid of the connector plate. Then eccentric moment stress is added vectorially to direct axial stress to determine the critical stress. See Figure 8.

### Proposed Method

It is proposed that the eccentric moment be computed by using the bottom chord axial tension force, T, multiplied by the vertical distance, e, between the centroid,  $c.g._b$ , of the bottom chord contact area and the centroid,  $c.g._u$ , of the upper chord contact area. This eccentric moment results in an eccentric stress that must be added vectorially to the axial stress to obtain the critical stress.





The proposed method has several advantages:

- a. It includes the effect of eccentricity; an improvement over the "general method."
- b. It includes, as does the FHA method, the increase in rotational resistance of larger plates through their vastly increased polar section moduli; an improvement over the TPI method which has fixed percentage factors based entirely on slope, rather than plate size.
- It considers an eccentric moment that is not afс. fected by the size of the members, whereas the FHA method results in a much larger moment if the top chord is larger than the bottom chord, or a somewhat smaller moment if the bottom chord is larger than the top chord. Since the axial forces are dependent on pitch, span, configuration of webs, and loads, but are not affected by member size, it would seem that the eccentric moment should not be affected by differences in the top vs. bottom chord member size. For example, using the FHA analysis, assume a truss is designed with a 2"x6" top chord but a 2"x4" bottom chord and an appropriately selected heel plate size. If the design is changed to a 2"x6" bottom chord (usually a stronger, more expensive truss), the FHA analysis permits a smaller heel plate than with the 2"x4" bottom chord, due to the reduction in the distance from the plate centroid to the intersection of member center lines.

Typical Calculations

Typical heel joint calculations shown here are all for the same plate,  $3-11/16'' \ge 9''$ , shown in Figure 9. They give a comparison of the different methods. A further comparison of  $3'' \ge 5''$ ,  $3'' \ge 8''$ , and  $5'' \ge 5''$  plates is given in Table 1.

General method:

b = 
$$\frac{C}{A_{t.c.}}$$
 =  $\frac{3,160 \text{ lbs.}}{2 \text{ x } 13.25 \text{ in.}^2}$  = 119 psi

TPI method:

b = 
$$\frac{C}{A(gross) \times 75\%}$$
 =  $\frac{3,160 \text{ lbs.}}{33.2 \text{ in.}^2 \times 0.75}$  = 127 psi

FHA method:

$$R_{n} = 1,000 \text{ lbs.} \qquad e = 6\frac{1}{4}$$
  

$$b = \frac{3,160 \text{ lbs.}}{2 \text{ x 16.6 in.}^{2}} = 95 \text{ psi}$$
  

$$c = \frac{R_{n}e}{2Z_{p}} = \frac{1,000 \text{ lbs. x 6.25 in.}}{2 \text{ plates x 54 in.}^{3} \text{ each}} = 58 \text{ psi}$$
  

$$\mathcal{L}A = 22.3^{\circ} \text{ (plate)} + 90^{\circ} + 18.4^{\circ} (4/12 \text{ slope})$$
  

$$= 130.7^{\circ}$$
  

$$\cos A = \cos 130.7 = -\sin (130.7^{\circ} - 90^{\circ}) = -0.65$$
  

$$\cos A = \cos 130.7 = -\sin (130.7^{\circ} - 90^{\circ}) = -0.65$$
  

$$\cos A = (95)^{2} + (58)^{2} - 2(95)(58)(-0.65)$$
  

$$= 19,570 \text{ (psi)}^{2}$$
  

$$a = 140.4 \text{ psi}$$







Try C = 3,000 lbs. (top chord force)

 $M = \frac{3,000}{1.055} \times 1.42'' + \frac{3,000}{1.055} \times \frac{4}{12} \times 0.98''$ 

M = 4040 + 930 = 4970 lb.in.

Combined stress equation (FHA)

 $\frac{P}{2A} + \frac{M}{2S} = \frac{3,000\#}{2 \times \frac{1}{2} \times 3 \times 5} + \frac{4040\#''}{2 \times 14.6 \text{ in.}^3} + \frac{930}{2 \times 14.6}$ = 200 + 138 + 31.8 = 369.8 psi

The direct stress is 200 psi and the torsional moment adds 85% to total 370 psi.

Figure 9(b). Typical Heel Plate Contact Stress Calculations for 3"x5" Plate.



Try C = 4,800 lbs. (top chord force)

 $M = \frac{4,800}{1.055} \times 1'' + \frac{4,800}{1.055} \times 4 \times 1.00''$  M = 4,500 + 1,517 = 6,067 lb.in.Combined stress  $\frac{P}{2A} + \frac{M}{2S} = \frac{4,800 \text{ lbs.}}{2 \times \frac{1}{2} \times 3 \times 8} + \frac{4,550 \text{ lb.in.}}{2 \times 34.16 \text{ in.}^3} + \frac{1,517}{2 \times 34.16}$ 

= 200 + 66.5 + 22.2 = 288.7 psi

The direct stress is 200 psi and the torsional moment adds 44% to total 288 psi.

Figure 9(c). Typical Heel Plate Contact Stress Calculations for 3"x8" Plate.



Proposed method:

$$b = \frac{C}{A_{net}} = \frac{3,160 \text{ lbs.}}{2 \text{ x } 13.25 \text{ in.}^2} = 119 \text{ psi}$$

$$c = \frac{3,000 \text{ lbs. x } 1.25 \text{ in.}}{2 \text{ x } 54 \text{ in.}^3 \text{ each}} = 34.7 \text{ psi}$$
Cosine Law:
$$a^2 = (119)^2 + (34.7)^2 - 2(119)(34.7)(-0.65)$$

$$a = 143 \text{ psi}$$

Shear stress:

Assume the critical shear section is approximately 50% holes:  $S_s = \frac{C}{2l_d t \cdot 50\%}$ .  $= \frac{3,160 \text{ lbs.}}{9'' \text{ x } \sqrt{(4)^2 + (12)^2} \text{ x } 0.035 \text{ in.}}$  = 9,550 psi

where  $l_d$  = length of plate along shear line

t = thickness of plate

A comparison of these four theoretical heel joint calculation methods for 3''x5'', 3''x8'', and 5''x5'' heel plates (See Figures 9(b), 9(c), and 9(d)) yielded the results shown in Table 1. These three plate sizes were later studied experimentally, too.

# <u>Calculation of Tensile Stresses within</u> the Bottom Chord Contact Area

### Assumptions

It is assumed that the plate is positioned parallel to the bottom chord, with equal "effective" teeth into both

Methods	
Calculation 5"x5".	
Heel Joint 3"x8", and	
Comparison of for 3"x5",	
Table 1.	

			Cri	itical Contad	t Area Stres	s (psi)	
	Assumed			FHA Me	thod	Propose	1 Method
Heel Plate Size	Lop Chord Force (1bs.)	General Method P/A	TPI P/.75A	Eccentric Moment (1b.in.)	Resultant Stress	Eccentric Moment (1b.in.)	<b>Resultant</b> Stress
3''x5''	3,000	200	266.7	4,990	348	4,040	323
3"x8"	4,800	200	266.7	7,990	289	4,500	248
5"x5"	5,000	200	266.7	13,050	411	11,050	378

top and bottom chords, allowing 1/4" edge distance at top chord and 1/2" end distance (measure perpendicular to crack) for bottom chord, as shown hatched in Figure 10. Further, it is assumed that area within the crack allowance does not carry its share of tensile stress, except as required by shear from the adjacent areas.

### Notation

The numbers and letters on Figure 10 denote the following:

- a. Numbers across top of the plate denote that column of teeth, the areas between columns being denoted 11-1/2 (for the group of isthmuses between 11 and 12), 14-1/2 (for the solid parent steel between 14 and 15), etc. Note: unless specifically noted, the numbers refer only to the top chord portion of the column, or bottom chord portion, rather than entire column.
- b. Letters down the side mean the strips (or isthmus lines) between holes, and letters with the "T" subscript denote the rows of teeth.

# Shear Stress Calculations

The following steps were taken to arrive at shear stress:

a. Neglecting the effects of eccentricity, the direct force (3,000 lbs.) may be divided by the total number of teeth (2 sides x 44 teeth per side), 88, to get the axial load per tooth = 3000/88 = 34.1 lb.

3/32 23 24 21 22 0 -20 R (ບ 18 19 -ß ( Net tensile area per isthmus: 13/32" x 0.036" x 50**% =** 0.0073 in.<sup>2</sup> 17 15 16 50 R ធ ~ Net shear area per row: 3/8" x 0.036" = 0.0135 in.<sup>2</sup> Shear area converted to equivalent tensile area: 0.0135 in.<sup>2</sup> x 2/3 = 0.0090 in.<sup>2</sup> 14 52 ß 13 12 N ١ł R 10 11 U R 53 2 6 00 y y R y ภ 2 -9 ß 8 R N ŝ -X 21 Į ß Bottom Chorl 1 m eeth in 1 2 Y ſ ß Column -1 J J Bt A+ T/C Nails Ξ щ 11 ~ 0 Ξ X 8 0 P щ 4 NON

Figure 10. Typical Heel Plate for Tensile and Shear Calculations.

b. Assume uniform shear along the crack line; which is assumed further to have only 50% effective area (the other 50% holes). The shear per lineal inch will be 3,160 lbs.  $9\frac{1}{2}$ " x 2 sides x 50% (166 lbs./in. = Gross Shear).

c. Assume 50% net tensile area at all sections with teeth cut out.

- d. Assume allowable shear stress is 2/3 of allowable tension stress, and that the net shear area is 2/3 as effective, per inch, as the net tension area due to this 2/3 relationship.
- e. Tension section A-A (3 effective teeth @ 34.1 lbs. per tooth,

{(7 x 13/32") + 6/32"} x 0.036" x 50% = 0.054 in.<sup>2</sup>
net section in tension, 3/16" net shear line length.
f. Section A-

 $\frac{3 \text{ teeth x } 34.1 \text{ lb./each}}{(7\frac{1}{2} \text{ tensile strips } 0.0073 \text{ in.}^2) + 0.0045} =$ 

■1,730 psi

Section B-

 $\frac{10 \text{ teeth x } 34.1 \text{ lb.}}{(6\frac{1}{2} \text{ strips x } 0.0073) + (1\frac{1}{2} \text{ x } 0.009)} = 5,600 \text{ psi}$ 

Section C-

$$\frac{16T \times 34.1 \text{ lb.}}{(6 \times 0.0073) \times (2\frac{1}{2} \times 0.009)} = 8,240 \text{ psi}$$

Section D-

$$\frac{21 \times 34.1}{(5\frac{1}{2} \times 0.0073) \times (3\frac{1}{2} \times 0.0009)} = 10,000 \text{ psi}$$

Section E-

$$\frac{26 \times 34.1}{(4\frac{1}{2} \times 0.0073) + (4\frac{1}{2} \times 0.009)} = 12,100 \text{ psi}$$

Section F-

$$\frac{30 \times 34.1}{(4 \times 0.0073) + (5\frac{1}{2} \times 0.009)} = 13,000 \text{ psi}$$

Section G-

$$\frac{34T \times 34.1}{(3\frac{1}{2} \times 0.0073) + (6\frac{1}{2} \times 0.009)} = 13,800 \text{ psi}$$

Improvements to Calculations

Since the "slip" is uniform along the shear line (crack between the top and bottom chord), the shear stress must also be uniform along the crack, rather than different in each section as indicated in the preceding set of computations. If the shear stress is in fact uniform, then the amount of shear force at each strip may be subtracted from the tooth value tensile force to determine the effective tensile force to be carried by net tensile section of the isthmuses between the holes. This concept is used in the following calculations for the same sections used before:

Shear force per strip = 332 lbs./in. (net x 3/8" strip)

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= 125 1bs./strip
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Section A-

$$\frac{3 \times 34.1 \text{ lb.} - \frac{1}{2} \times 125 \text{ lb.}}{7\frac{1}{2} \text{ strips } \times 0.0073 \text{ in.}^2} = 730 \text{ psi}$$

Section B-

$$\frac{341 \text{ lb.} - 1\frac{1}{2} \times 125 \text{ lb.}}{6\frac{1}{2} \times 0.0073 \text{ in.}^2} = 3,200 \text{ psi}$$

Section C-

$$\frac{545 \ 1b. - 2\frac{1}{2} \ x \ 128}{6 \ x \ 0.0073} = 5,300 \ psi$$

Section D.

$$\frac{715 \text{ lb.} - 3\frac{1}{2} \times 125}{5\frac{1}{2} \times 0.0073} = 6,920 \text{ psi}$$

Section E-

$$\frac{886 \text{ lb.} - 4\frac{1}{2} \times 125}{0.0328} = 9,850 \text{ psi}$$

section F-

$$\frac{1023 \text{ lb.} - 5\frac{1}{2} \times 125}{0.292} = 11,500 \text{ psi}$$

Section G-

$$\frac{1160 \ 1b. - \ 6\frac{1}{2} \ x \ 125}{0.0256} = 13,550 \ psi$$

# Buckling and Shear Stresses in the Steel

Investigation of the Cause of Buckling

A small element centered over the shear line will be in a state of pure shear. The element may come from the area  $12\frac{1}{2}$  - E<sub>t</sub>, or that vicinity, on the truss plate shown in Figure 10. Figure 11 is a blown-up view of this element.

Since pure shear can exist only in one particular plane through a two-dimensional element, there also exist tensile and compressive stresses on other planes through the point. The maximum and minimum normal (principal) stresses occur as shown in Figures 12(b) and 12(c) on planes that bisect the angles between the planes on which the given shearing stresses act, and these principal stresses are equal in magnitude to the shearing stresses. The shearing stresses on these 45° (principal) planes are equal to zero.

The principal stresses at a point are used to compute the shearing stress as follows;

 $T_{max} = \frac{1}{2} (\sigma_{max} - \sigma_{min})$ in which a principal stress is considered to be positive if it is a tensile stress and negative if a compressive stress. Furthermore, this maximum shearing stress occurs on each of the two planes that bisect the angles between the planes on which the maximum and minimum principal stresses occur.

Compressive buckling, applying this concept to the truss plate, is caused when the compressive stresses that result from the shear exceeds the Euler formula critical level. The direction of the buckling can be determined, prior to its occurrence, from the slope of the shear line, rotating 45° to get to the maximum compressive stress.

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Figure 12. Free-body diagrams of shear element.

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Discussion of Shear Stress in the Steel

The shear stress in the steel at the crack is uniform along the plate. If the truss plate is oriented parallel to the shear line and centered over it, the equal contact areas will provide an approximately equal number of effective teeth into each chord member. Since the "parallel to shear crack" orientation keeps the eccentricity of the two contact area centroids (see Figure 13) approximately the same as the "parallel to bottom chord" orientation, the effect of the eccentric moment will be minimized.

The "parallel to crack" orientation permits a more precise determination of cross-sectional area at the shear crack than does the "parallel to bottom chord" orientation. Since the tooth hole punch-outs are located in uniform rows (in one of the types of plates investigated), in line with each other, the net steel area parallel to either the "die direction" of the plate (b, which is always equal to some multiple of 2-1/4") or the "across die direction" (h, which is equal to 2-7/8", 3-11/16", or 5-5/16") is about 50% of surface area, at the critical section of that particular plate type.

For orientations of the plate other than "parallel to crack" or "perpendicular to crack," it is much more difficult to precisely compute effective net shear area, due to the unequal way the rows of teeth cross the shear line. This can be easily seen in Figure 10, which is shown for a 4 in 12 pitch.



Figure 13. Eccentricity for alternate heel plate positions.
Since the net steel area exactly parallel or exactly perpendicular to the plate, measured along the critical line, is 50% (for this particular manufacturer's plates), no other plate orientation results in a shear line of less than 50%. For design purposes, it could be assumed that the net steel was 50% of the shear line length. This assumption is conservative.

Calculation of Shear Stress at Critical Section

The calculation of shear stress at the critical section uses the conventional formula:

$$S_{s} = \frac{C}{2(\text{plates})\text{Lt 50\%(net)}} = \frac{C}{\text{Lt}}$$
where C = top chord compressive force (which acts parallel to the shear line)  
L = length of plate along shear line  
t = thickness of plate  
From Figure 9:

$$S_s = \frac{3,160 \text{ lbs.}}{9'' \times \sqrt{(4)^2 + (12)^2} \times 0.035''} = 9,550 \text{ psi}$$

For a similar plate parallel to the crack:

$$S_s = \frac{3,160 \text{ lbs.}}{9'' \times 0.035''} = 10,050 \text{ psi}$$

This shear stress must be transferred through eleven full size steel sections, 0.375 in. x 0.035 in., and two half sections 0.1875 x 0.035 per plate. These sections are approximately 13/64 in. high (0.203 in.). See Figure 14.

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Figure 14. Critical shear stress (buckling) area.



Figure 15. Free body diagram at shear line.

Analysis of Section A-B-C-D (shown hatched in Figure 14).

a. Shear force on line E-F =

$$\frac{3,160 \text{ lbs.}}{22 \text{ full sections } + 4 \text{ half sections}} = \frac{3,160}{22 + 2}$$

$$131.8 \text{ lbs. per section}$$
b. Shear stress on a full section, such as E-F =
$$S_{s} = \frac{P}{A} = \frac{131.8 \text{ lbs.}}{3/8'' \times 0.035''} = 10,050 \text{ psi}$$
(This checks with the general calculations on the preceding page.)
c. From Figure 15, the stress at the line C-D can be

c. From Figure 15, the stress at the line C-D can be computed by assuming that C-D-E-F is a short cantilevel beam, 3/8" deep, 13/128" long, 0.035" thick, with a concentrated load of 1,318 lbs. at the end.

d. Section Modulus, S, at section C-D =  

$$\frac{bd^2}{6} = \frac{(0.035 \text{ in.})(.375 \text{ in.})^2}{6} = 0.00082 \text{ in.}^3$$

e.  $f = \frac{M}{S} = \frac{P1}{S} = \frac{131.8 \text{ lbs. } x \text{ } 13/128 \text{ in.}}{0.00082 \text{ in.}^3} = 16,300 \text{ psi}$ 

### CHAPTER IV

### EXPERIMENTAL ANALYSIS

#### General

A variety of heel plate sizes and shapes were used to test the proposed heel joint analysis method. A small 8'-0" test specimen and corresponding jig were developed and used to permit a large number of different specimens to be tested quickly and cheaply. Each type of plate could have several repetitions very easily to confirm results. A second set of 8'-0" specimens was built and matched to 24'-0" trusses to correlate the load-deflection data with full scale trusses. Lastly, Stress-Coat brittle lacquer was used to determine location and direction of the principal stresses.

## Test Specimens

The initial set of test specimens were built using 20 ga. TroyTrus plates of various sizes of the type shown in Figure 10. The lumber was all 1500f Industrial Light Framing West Coast Hemlock. All the plates and lumber were supplied, and specimens fabricated, by Troy Steel Corp. using a press assembly similar to that shown in Figure 19. All the lumber was kiln dried, but no attempt was made to determine moisture content or specific gravity. See Table 2.

				-	
Table	2.	List	of	Specimens	Tested.

No.	Size	Mfr.	Lg.	Pitch	Species.	Grade	Remarks
1	3 x 10	TW	8'	4/12	Doug.	1500f	
2	3 X 8	" TD	11	11	Uem	••	18
	$\frac{3.7 \times 0.7}{5 \times 7}$		11	11	Hem.	11	
	5	1 1			Doug.		
5	5 x 5	"	11	- 11	"	11	18
6	2.9 x 6.8	TR	11	6/12	Hem.	1500f	(1)
7	3.7 x 4.5	11	11	11	11	**	
8	11 11	"	11	11	11	11	(1)
9	$\frac{2.9 \times 9}{2.9 \times 9}$				**	**	
	$3.7 \times 2.2$						(1) (5)
	$2.9 \times 0.8$	11	11	11			
$\frac{12}{13}$	$5 3 \times 4 5$	11	11	4/12	11	11	
14	$3.7 \times 6.8$	11	**	1,12	••	11	1
15	2.9 x 9	11 .	11		••	11	1
16	5.3 x 4.5	"	11	11	**	F1	(1)
17	11 11	11	11	11	**	11	$\left  \begin{array}{c} \left( \overline{2} \right) \right $
18	11 11	"	11	11	11	11	(3)
19	5.3 x 6.8	11	11	11	11	**	
20	2.9 x 9	· · ·	11	11	11	**	
21	3.7 x 6.8	"	11	11	11	11	
22	$3.4 \times 5.1$	DU			11	11	(3)
23	3.7 x 6.8	TR					
24	5.5 X 0.8	+			+		
25	$5.7 \times 4.5$						
20	$5.3 \times 4.3$		- 11			••	
28	11 11	11	11	11	11	17	<b> </b>
29	3.7 x 6.8	11	11	11	11	••	
30	2.9 x 9	11	- 11	11	••	11	(-)
31	5.3 x 4.5	11	11	11	11	+1	(2)
32							
33	$3.4 \times 5.1$	DU	11 .		11	11	J
34	2.9 x 9	TR					
35	3.7 x 6.8						
30	<u>3.4 x /.6</u>			11	11		(7)
3/	3 <b>v</b> E	TW			Dour	Conct	
30	J X J 11 11	11	11		Doug.		
40	3 x 8	11	11	11	1 11	11	<u> </u>
41		11	11	11	11		
42	5 x 5			11		11	(7)
43	11 11	11	11	11	11	11	(7)
44	3 x 5	11	24'	"	11	"	
45	11 11	11	11	"	"	11	
46	3 x 8		"	11	11	17	
47			"		11	11	
48	1 5 x 5	[ "	"	11			

г	ah	16	2	(cont'd)	
T	aυ	TC	2.		

No.	Size	Mfr.	Lø.	Pitch	Snecies	Grade	Remarks
					opeeres	UTauc	Kemai KS
49	5 x 5	TW	24'	4/12	Doug	Const	
51	3 x 5	1	81		Wh Fir	1650f	
52		1,	i ii		11	10501	
53	3 x 8		<del>                                     </del>		11	1	
54		11	11	.,			
55	5 * 5						
56		+	<u>├</u>		11	+	
57					Doug	Stand	
50					Doug.	Stanu.	
- <u>50</u>		<del> </del>	241		Wh Fin	+	
59			11	••			
61	7 - 0			,,			
-22-		+	+			+	
67	<b>5 5</b>	,,					
03							
04	<u> </u>				7.7 F F	ļ	
05	55/10X41/2		8.		w.Hem.		(2)
00	311/10X03/	4 "					
0/	<u>311/10x41/</u>	<u>+</u>					
68							
69	55/10x41/2	1					(2)
70		— <u> </u>	L				(2)
71							(2)
72	55/16x63/4				11		(3)
73		<u> </u>				11	
74							<u>.</u>
75					**		(1)
76			11	**		1500f	(1)
77							(1)
78	3 x 5	TW		**	Doug.	1500f	
79				**	11		
80			11	11	11		
81	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,			11	**	''	
82	11 11	"	24'	11	11	11	
83	11 11		" -	11	11		
84	17 11			11	11		
85			11	11	11	"	
86	3 x 8		8'	11	11		(4)
87	11 11	"	".	11	**	''	
88	11 11		11	11	11	"	
89	17 17	" _	11	11	11	11	
90	5 x 5		11	11	11	''	
91	11 11		11	11	11	11	
92	11 11	1 11	"	11	11	11	
93	11 11		"	11	11		
94	3 x 8	11	**	11	Wh.Fir.	1500f	
95	11 11		"	11	11		
96	11 11	11	11	11	11	"	
97	11 11	"	"	11	11	''	
98	3 x 5	"	"	**	Doug.	••	

No.	Size	Mfr.	Lg.	Pitch	Species	Grade	Remarks
99 100	3 x 5	TW ''	8 ' ''	4/12	Doug.	1500f	
101	11 11	11	11	11	17	11	(4)
102	11 11	- 11	11	11	Wh.Fir.	,,	(+)
103	11 11	- 11	11	11	11	••	
104	11 11	11	11	11	11	• • •	
105	11 11	- 11	11	11			
106	5 x 5	11	"	11	••	- 11	
107	** **	11	"	11	11	11	
108	11 11	11	11	**	- 11	••	
109	11 11	11	**	11	11	11	

Table 2. (cont'd.)

"Lg." in Table denotes length of test specimen. "Mfr." in Table denotes manufacturer of truss plates as follows:

TW stands for TrusWal Systems

TR stands for Troy Steel Corporation DU stands for Duratile.

Remarks" (1) Plates parallel to crack (2) Plates perpendicular to bottom chord
(3) Plates perpendicular to bottom crack
(4) Riehle testing machine (5) Two plates each side(6) Three plates each side (7) Plates not impaled properly

The second set of test specimens, including 24'-0" trusses, were built using truss plates of 3"x5", 3"x8", and 5"x5" of a second type, shown in Figure 39. The lumber was of Coast Region Douglas Fir for one set, both 8'-0" specimens and matched 24'-0" trusses, and white fir for a second matched set, both 8'-0" and 24'-0". Truss plates of 20 gauge steel were applied without nails, using a roller press. Moisture content and specific gravity at time of test were determined for the top and bottom chords of each test specimen and are recorded in Table 3.

## Test Jigs

For the first series of tests, a small 8'-0" long test jig with single hand-pumped hydraulic cylinder (Blackhawk Mfg. Co., Milwaukee, Wis., 53227, Model R159 Porto-Power 10 ton capacity, 6" travel, 1.688" diameter ram with Model P76 pump) was built as shown in Figure 17. The actual jig is shown in Figure 20 with a test specimen in place.

For the second series of tests, a wall mounted full scale hydraulic test jig located in the Michigan Building Components plant on Decker Road, Walled Lake, Michigan, was used to test the 24'-0" trusses. It is shown in Figure 21.

For the third series of tests, an old Riehle Testing Machine located in the Forestry Building, Michigan State University, was used to test 8'-0" specimens. It is shown in Figure 22.

Table 3. Moisture Content and Specific Gravity

Specific Gravity .4825 4415 5510 5110 5475 ഗ .4165 502 .405 367 567 .605 .458 .402 ഗ 51 Average .45% Moisture Content 20.15% 90 17.30\$ 17.15% 2 16.70\$ 90 17.35\$ 90 90 90 ~ 9.35% .45% 4 19.0 16.9 ∞. 9. 2 (%) 17 ∞ 17 16 œ œ ---Specific Gravity 

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 00 00 00 00 00 0000 00 000 000 00 00 0 Content (%) 21.6% 18.7% Moisture 7.48 8.19 6.88 19 19.68 æ မှ 1 % 5 % 90 ~ 2 2 8 7.19 8.48 9.69 9.69 . . . 16. 22. 15. - - C 8. . • 17 17 5 9 Water Mater Displ.Displ.132.5132.6122.5122.142. 137. 138. 138. 148. 137. Dry Wt. Oven 78.61 79.68 78.91 78.91 78.91 91.03 91.03 72.43 72.43 72.43 72.43 72.95 69.52 69.52 69.52  $\begin{array}{c} \text{Wt.} \\ \text{(g)} \\ \text{(g)} \\ 73.50 \\ 880.28 \\ 880.66 \\ 880.08 \\ 77.68 \end{array}$ 001 est 000000 • 54 54 63 69 Species ധ White " Doug = = = = = = = = = = = = = = = = = = = -= = = = = = No Spec. 52 53 53 53 54 53

Table 3. (cont'd.)

Specific Gravity 5135 0.3795 0.3465 0.395 .498 0.380 0.393 533 .484 0.489 0.406 0.405 0.392 • Ö Ö Ö Average Moisture 9.55\$ ------Content 90 96 æ 96 20 đ مد æ 20 20.15\$ 16.95 19.6 .2 9.7 20.6 21.4 20.2 9.6 9.8 ഗ M (\$) . 18 21 23 --\_ -Specific Gravity  $\begin{array}{c} 0.401\\ 0.358\\ 0.358\\ 0.351\\ 0.351\\ 0.353\\ 0.352\\ 0.356\\ 0.352\\ 0.356\\ 0.356\\ 0.356\\ 0.356\\ 0.373\\ 0.373\\ 0.407\\ 0.407\\ \end{array}$ .508 .468 .598 .401 00 00 00 Content
(%) Moisture 16.9% 19.5% 15.8% 18.4% 20.5% 20.7% 21.5% 18.8% 22.8% 20.0% 20.5**%** 18.6**%** 222.4% 18.7% 231.2% 18.1% 21.4% 21.4% 17.5% 17.5% 20.7<del>\$</del> 22.2**\$** 17.2<del>\$</del> 29.3**\$** 7.8 δ -Water Displ. (cc) 35.8 

 143.7

 137.6

 135.8

 132.4

 152.7

 160.1

 161.7

 181.8

 169.5

 166.5 184.2 156.9 161.0 168.2 155.1 167.5 170.7 174.4 176.0 171.5 168.2 Oven Dry  $\begin{array}{c} 70.27\\ 53.72\\ 58.58\\ 70.41\\ 63.82\\ 63.20\\ 85.12\\ 85.12\\ 80.21\\ 81.69\\ 105.28\end{array}$ Wt. (g) 54.37 49.59 49.41 60.16 57.62 67.80 67.00 67.00 65.90 63.53 57.13 72.15 72.15 68.80 100.15 80.76 79.91 65.24 65.24 65.24 68.55 87.01 87.01 83.19 83.19 83.19 83.19 83.19 83.19 83.19 83.19 83.19 83.19 77.45 77.45 128.67 63.57 59.26 57.22 71.25 68.95 128.67 80.51 129.51 Test Wt. (g) . Species White " Ð Doug White " Doug : = = = = = F = = : F = = = = = = : N0 B F a F a F BE Spec. 79 80 80 80 

Table 3. (cont'd.)

Specific Gravity 0.479 502 519 543 509 .454 σ 587 504 0.462 0.500 0.440 371 0.474 .499 0 0. . . 0 . . 0 0 0 Average Moisture Content (%) 90 % % 96 % 96 % 90 90 90 90 96 90 90 ഗ 2. 0 М 2 0 ø 9 Σ .2 ø 9 0 m 16. . ٠ • 15. 20. 19. 18 22 20 22 δ 13 14 18 21 17 -Specific Gravity  $\begin{array}{c} 0.468\\ 0.468\\ 0.5459\\ 0.5459\\ 0.505\\ 0.505\\ 0.464\\ 0.478\\ 0.478\\ 0.464\\ 0.478\\ 0.464\\ 0.478\\ 0.464\\ 0.478\\ 0.525\\ 0.464\\ 0.478\\ 0.464\\ 0.405\\ 0.337\\ 0.337\\ 0.464\\ 0.405\\$ 477 526 476 432 487 551 531 467 Moisture Content (%)  $\begin{array}{c} 168.1\\ 129.5\\ 1229.6\\ 1229.5\\ 1225.6\\ 1225.5\\ 1$ Water Displ. (cc) Oven Dry 80.15 91.80 57.40 661.42 661.42 661.42 662.51 662.51 662.51 662.51 662.51 662.51 662.51 662.51 662.51 662.51 662.55 662.55 662.55 662.55 662.55 662.55 662.55 662.55 662.55 662.55 662.55 662.55 662.55 662.55 662.55 662.55 662.55 662.55 653.68 653.68 653.68 653.68 653.68 653.68 653.68 653.68 653.68 653.68 653.68 653.68 653.68 653.68 653.68 653.55 655.55 653.55 653.55 653.55 653.55 653.55 653.55 653.55 653.55 653.55 653.55 653.55 653.55 653.55 653.55 653.55 653.55 653.55 755.5 Wt. (g)  $\begin{array}{c} 91.49\\ 04.84\\ 70.87\\ 770.87\\ 770.87\\ 773.77\\ 772.28\\ 772.28\\ 772.28\\ 772.28\\ 772.23\\ 772.23\\ 772.23\\ 772.23\\ 772.23\\ 772.23\\ 772.23\\ 772.23\\ 772.23\\ 772.23\\ 772.23\\ 772.23\\ 772.51\\ 77$ Test Wt. (g) -. S Specie മ Doug. Whit. = = = = = = = = = = = No N pec 
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	ge	Specific Gravity	0.396	0.355	0.351	0.485	0.453	0.494	0.571	0.444	0.38	0.346	0.359	0.357	0.398	0.364	0.400
	Avera	Moisture Content (\$)	14.7 %	15.9 %	15.4 %	27.8 \$	26.0 %	29.1 %	39.7 %	16.9 %	19.3 \$	13.2 %	16.0 %	14.7 %	14.3 %	14.7 %	13.8 %
		Specific Gravity	0.437 0.356	0.365 0.345	0.386 0.316	0.494 0.476	0.445 0.412	0.548 0.441	0.578 0.565	0.402 0.486	0.440 0.320	0.353 0.339	0.347 0.371	0.328 0.386	0.394 0.402	0.339 0.389	$0.409 \\ 0.392$
ont'd.)		Moisture Content (%)	14.8%	17.9% 13.9%	17.5 13.3	32.1 <b>%</b> 23.5%	29.3\$ 22.7\$	32.2 <del>8</del> 26.0 <del>8</del>	46.9% 32.6%	14.7% 19.1%	22.4% 16.3%	13.0% 13.4%	14.08 17.98	13.5 <b>%</b> 15.8 <b>%</b>	13.9% 14.6%	12.9 <b>%</b> 16.4 <b>%</b>	12.9% 14.7%
le 3. (c		Water Displ. (cc)	126.9	146.0 136.5	125.8 120.1	131.6 132.5	124.1 145.6	142.2 123.0	132.0 122.4	132.5 121.5	132.6 140.1	153.4 145.8	118.3 115.5	145.9 131.3	139.4 135.7	132.5 127.3	124.7 121.7
Tabl		Oven Dry Wt. (g)	55.43 44.70	53.35 47.04	48.59 37.92	65.04 63.12	61.47 59.93	77.91 54.20	76.31 69.12	53.21 59.06	58.29 44.82	54.15 49.47	41.10 42.86	47.92 50.69	54.96 54.58	44.92 49.50	51.00 47.67
		Test Wt. (σ)	63.63 51.22	62.91 53.56	57.10 42.97	85.89 77.97	79.47 73.54	103.00 68.28	112.07 91.63	61.01 70.32	71.34 52.11	61.18 56.09	46.81 50.53	54.40 58.68	62.59 62.53	50.73 57.63	57.58 54.68
		Species	White "	= =	: :	Doug.	= :	: :	1	White "	= =	= =		: :			White "
		Spec. No	95 B 95 T	96 B 96 T	97 B 97 T	98 B 98 T	99 B 99 T	100 B 100 T	101 B 101 T	102 B 102 T	103 B 103 T	104 B 104 T	105 B 105 T	106 B 106 T	107 B 107 T	108 B 108 T	109 B 109 T



Figure 16. 8'-0" test specimen.



#### Instrumentation

A Starrett dial gauge, accurate to 0.001", was mounted at one heel joint as shown in Figure 18. It was mounted with screws on the centerline of the top chord. Its plunger was against a steel angle which was screwed symmetrically over the bottom chord center line.

A hydraulic gauge on the R159 Porto-Power was used to read the pressure on the peak of the initial 8'-0" specimen. The gauge had marks for every 400 psi and was read to 200 psi accuracy. This gauge was calibrated on the Instron machine at the Forestry Building, Michigan State University, and the calibration data is given in Table 4, page 64.

A hydraulic gauge on the wall-mounted full scale test jig was installed in the hydraulic line at the peak of the 24'-0" trusses as shown in Figure 21. It was marked in 25 psi increments and read in 10 psi increments. This gauge was also calibrated on the Michigan State University Forestry Department Instron machine. The calibration data is given in Table 5, page 65.

The Riehle testing machine used for the last series of 8'-0" specimens is mechanically operated and has a balance scale accurate to 5 lb. increments. The heel deflection was read every 200 lbs. of peak force, at the instant the balance arm hit the top. See Figure 22, page 63.

### Test Procedure

For the initial series of 8'-0" tests, on the handpumped hydraulic test jig, the heel deflection was read



Figure 18. Dial gauge set-up.



(a) Truss assembly jig.



(c) During impalement.



(b) Ready to impale plate.



(d) After impalement.



(a) Test apparatus for 8'-0" specimens.



(b) Close-up of gauges.

Figure 20. Small test jig for 8'-0" specimens.



(a) Wall mounted hydraulic apparatus.



(b) Close-up of heel, showing gauge.

Figure 21. Test jig for 24'-0" trusses.



(a) Front view.



(c) Load application and specimen support.



(b) Front close-up.



(d) Rear view showing dial gauge and balance arm.

Figure 22. Riehle test machine for 8'-0" specimens.

		F									
Act	Press	Instron Reading									
Press.	Read.	#1	#2	#3	#4	Ave.					
0	0	0	0	0	0	0					
5/	25	85	88	83	75	82./5					
58.4	50		132	128	125						
00.0	100			180	1/2						
102.5	100	202	232	229	221						
14.0	125	202 775		280	270						
176 0	175	100	332	320	322 705	329.23					
200	200	400	390	397	303 177	393.00					
218 5	200	440	432	440	437	440.75					
240 5	250	537	542	433 541	532	578 25					
264	275	592	595	591	581	580 75					
286	300	638	645	642	631	639.00					
312	325	693	705	698	687	696.75					
335	350	745	757	747	742	747.75					
356	375	794	802	797	790	795.75					
379	400	845	852	850	838	846.25					
400	425	887	902	897	890	894.00					
422	450	937	948	946	938	942.25					
450	475	1007	1017	1013	1000	1009.25					
472	500	1057	missed	1063	1053	1057.67					
495	525	1109	1115	1110	1105	1109.75					
518	550	1153	1163	1162	1155	1158.25					
540	575	1202	1215	1212	1208	1209.25					
562	600	1255	1263	1260	1262	1260.00					

## Table 4. Calibration Data for Blackhawk Hydraulic Gauge.

Blackhawk Porto-Power hand operated hydraulic pump Model R159 Serial #A21233 Area: 2.2365 sq. in. Oil capacity: 13.419 cu. in. 6" travel 1.688" diameter cylinder 8950 psi maximum pressure @ 103 1b. handle pressure

Hyd. Press.	Instron Reading										
	#1	#2	#3	#4	# 5	Ave.					
0	0	0	0 · 575	0	0	0					
1000	975	1065	1050	1040	1035	1033					
2000	1910	2025	2055	2000	1985	1995					
3000	2935	2970	2960	9240	2910	2943 2943					
4000	2910 4455	4065	3960	3920 4405	3915 4410	3956 4390					
5000	4900	5000		4950	4900	4938					

Table 5. Calibration Data for Full Scale Test Jig.

approximately every 400 lbs. of peak pressure. This gave a minimum of five readings and a maximum of ten, depending on specimen type. It was necessary to use both hands to take the deflection data, which necessitated releasing the hydraulic pump handle. This in turn allowed a slight relaxation in the pressure, reducing the measured deflection. As a result, it was believed that the load-deflection data from these initial 8'-0" specimens indicated too much stiffness. To counteract this possibility, later tests were performed on the Riehle testing machine. Duration of tests varied from five to ten minutes for these tests and all tests were performed indoors at  $60^{\circ}$  to  $65^{\circ}$  F, on this hand jig.

The second set of tests, performed on the 24'-0" fullscale wall mounted hydraulic jig, took twenty to twenty-five minutes per test. Pressure was applied 24" o.c. using a motor driven pump which maintained constant pressure. The heel deflection gauge was allowed to stabilize before each reading, and readings were made about every 50 psi, for a minimum of six per test specimen. These tests, also inside, were performed at temperatures ranging from 65° to 85°.

The third set of tests, performed on Michigan State University Forestry Department's Reihle machine, involved readings at every 200 lbs. of peak loading. The load was mechanically applied at a uniform speed of 1/16" per minute and readings were made each time the balance arm hit the top. About twenty readings were made per test specimen.

In all cases, the deflection gauge at the heel had to be removed when failure appeared imminent to prevent damage to the gauge. This meant that deflection data could not be taken in the neighborhood of ultimate load. Should further research by others be continued on this type of joint, the dial gauge should be mounted to read by extension rather than by compression, to eliminate the danger of damage and permit the full range of readings to be made.

# Test Results

Types of Failure of Experimental Specimens

During the testing program, all the types of failure described earlier were observed. A record of type of failure was made of most of the specimens, with the following results:

a. All <u>3"x5"</u> and <u>3"x8"</u> in both white fir and Douglas fir, and all <u>2-7/8"x9"</u>, <u>3-11/16"x4-1/2"</u>, and <u>3-11/16"x6-3/4"</u> in western hemlock failed by the tooth withdrawal associated with the highest stresses. See Figure 23 for photographs of this type of failure. Very little rotation was noticed in the 3"x5" and 3-11/16"x4-1/2" sizes, and no rotation was seen in the three longer sizes. This amount of rotation, or lack of it, was in accordance with the proposed theoretical analysis which predicts less rotation in longer plates due to their higher polar section modulus (higher resistance to eccentric forces).



Figure 23. Typical wood and tooth failures (contact area).

5" x 5" plate. (p)

- b. All the <u>5"x5"</u> plates (which had teeth oriented in all four directions, every 90<sup>0</sup>) showed considerable rotation, as well as some S-shaped distortion, prior to failure. See Figure 24 for photographs of this S-shaped distortion, though of a different, heavier gauge plate. The rotation was less pronounced but somewhat similar to that shown for the nailed plate in Figure 25. Ultimate failure of these 5"x5" plates was the result of tooth withdrawal, which always started essentially simultaneously at the upper left and lower right corners as they lifted out of the wood first, due to that diagonal dimension of the plate stretching as the plate became S-shaped.
- c. All the <u>5-5/16"x6-3/4"</u> plates which were equally applied on top and bottom chords failed by buckling, regardless of their orientation. Those placed perpendicular to the crack (see photo sequence in Figures 26 and 27) failed at lower loads than those placed parallel to the bottom chord (see photo sequence in Figures 29 and 30). This showed the higher shear value and greater buckling resistance when the long dimension of tooth holes is oriented approximately parallel to the crack.
- d. All the 5-5/16''x4-1/2'' plates (which had teeth and holes pointed perpendicular to the bottom chord) showed both buckling and rotation, as seen in the



(a) Right-hand heel joint. (Note S-shape of ends of plate.)



(b) Left-hand heel joint.

Figure 24. Distortion of 18 gauge heel plates.



 (a) Original location, showing deflection gauge.



(b) Deflected position.





(a) Initial set-up.



(b) 0.019" deflection.



(c) 0.045" deflection. (Note initial buckling along shear line.)



(d) 0.075" deflection. (Initial buckling is more severe.)



(e) 0.088" deflection.



(f) 0.162" deflection.

Figure 26. Initial buckling of Specimen 26.





(a) 3/16" deflection.



(b) 1/4" deflection.



(c) 5/16" deflection.



(d) 7/16" deflection.



(e) 9/16" deflection. (No rotation. All buckling failure.)



(f) 9/16" deflection. (Close-up.)

Figure 27. Progressive buckling of Specimen 26.



(a) 1/4" deflection. (Note rotation of plate.)



(b) 3/8" deflection. (Hole enlargement at upper right.)



(c) 1/2" deflection. (Pulling of teeth at pencil.)



(d) 5/8" deflection. (Lifting of teeth at pencil.)



(e) 3/4" deflection. (Buckling severely.)



(f) 1" deflection. (Holes enlarged on adjacent corners, showing rotation.)

Figure 28. Buckling sequence of 5-5/16" x 4-1/2" plate.

photo sequence in Figure 28, prior to ultimate failure by tooth withdrawal. Close inspection of the corner teeth in Figure 28 reveals the hole enlargement, especially at the upper right behind the tooth at the pencil, and at the lower left.

e. The <u>3"x10"</u> plates on one of the earliest specimens tested failed in tension, rather than by either buckling or tooth withdrawal. The tensile joint had already been studied by Misra and was only of marginal interest to this study as an additional limiting factor, rather than a part of the main study of contact area stresses and buckling strength. As a result, it was not studied in more detail. Shorter heel plates were selected to prevent this type of failure in the main protion of the tests.

Stress-Coat Analysis

A Stress-Coat analysis was made of several sizes of plates, on both 8'-0" specimens and full size 24'-0" trusses. Both showed the same pattern of stress cracks.

The Stress-Coat crack pattern development sequence has been photographed (Figure 29) for specimen 27, a 5-5/16"x 6-3/4" plate applied in the normal position. Since the cracks were too small to show up in the photos, red dye etchant was painted over the increasing area that had Stress-Coat cracks, for each new level of loading. By following the sequential photos, Figures 29(a) through 29(e), the spreading Stress-Coat pattern indicates that the strains are greatest



(a) 0.037" Deflection. (Stress-Coat cracks painted.)



(b) 0.056" Deflection



(c) 0.072" Deflection.



(d) 0.105" Deflection.



(e) 0.214" Deflection. (Some areas still have no stress cracks.)



(f) 0.401" Deflection. (Entire plate painted to show buckling.)

Figure 29. Photos of Stress-Coat cracks on Specimen 27.





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(a) 3/8" deflection.



(b) 1/2" deflection.



(c) 5/8" deflection.



(d) 3/4" deflection.



(e) 3/4" deflection.



(f) 1" deflection.

Figure 30. Progressive buckling of Specimen 27.



in the area of the shear crack, with just a few teeth at the upper right and lower left beginning to show high strains in Figure 29(d) at 0.105" deflection. Even in Figure 29(e), at 0.214" deflection, just prior to the start of buckling, the top three rows of teeth (about 1-1/4") and bottom three rows (another 1-1/4" strip of plate) still showed very few Stress-Coat cracks. This means that for a 5-5/16" wide plate, almost 2-1/2", or 50%, is not contributing its full value to joint strength. The joint apparently would have been just as strong, in terms of total top chord axial force, had a somewhat smaller heel plate been used.

The entire surface of the plate has been painted in Figure 29(f) to better illustrate the buckling sequence by showing the light reflection off the ripples.

A small-scale sequence of crack pattern development on a 5-5/16"x6-3/4" plate is shown in Figure 31, followed by larger scale drawings in Figures 32, 33, and 34. It should be noticed in Figure 32 that the Stress-Coat cracks <u>between</u> teeth start in the vicinity of the shear crack between top and bottom chord members. At the same time, initial Stress-Coat cracks also occur at the <u>bases</u> of teeth located in the extreme upper right and lower left corners. This verifies two important predictions:

- a. Shear stress in the steel is greatest along the joint between chords.
- b. Tooth stresses are highest, initially, on corner teeth.

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(a) 4,320 lbs.

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(b) 5,690 lbs.



(c) 6,320 lbs.

(d) 6,950 lbs.



Axial force in top chord is given below each drawing of progressive stress cracks.

(e) 8,850.1bs. Start of buckling.

Figure 31. Sequence drawing of Stress-Coat cracks on 5-5/16" x 6-3/4" plate.



(b) 5,690 lbs. top chord force.

Figure 32. Large scale of initial Stress-Coat cracks on 5-5/16" x 6-3/4" plate.



(b) 6,950 lbs. top chord force.

Figure 33. Large scale of later Stress-Coat cracks on 5-5/16" x 6-3/4" plate.



<sup>(</sup>No Stress-Coat cracks in this area.

8,850 lbs. top chord force.

Figure 34. Large scale of Stress-Coat cracks at start of buckling of  $5-5/16'' \ge 6-3/4''$  plate.

Close inspection of Figure 33 reveals that stresses and strains are definitely increasing rapidly along the shear line, due to these increased top chord forces. There is very little indication of new Stress-Coat cracking at the upper right and lower left corner teeth, indicating that the plate, or teeth, is slightly distorted or undergoing relaxation, and tooth forces are being redistributed.

Figure 34 shows very dramatically that large areas of this 5-5/16" wide plate are not stressed highly enough to cause Stress-Coat cracking, despite forces high enough to initiate buckling along the shear line between top and bottom chords. Load-deflection data showed that the initiation of buckling precluded higher loadings. Large areas of the plate just weren't very highly stressed, even at ultimate load.

Figure 35 shows drawings of the Stress-Coat crack development for a 3-11/16"x6-3/4" plate applied with its centerline directly over the crack between top and bottom chords (the so-called "parallel to crack" orientation).

Figure 36(a) indicates that initial stresses at the base of the teeth are highest for teeth nearest the crack, and that one tooth at the upper right corner is also stressed about the same amount (apparently due to rotation, or attempted rotation, of the plate). Figures 36(b) and (c) show the progressive development of stress cracks at higher top chord forces, indicating the higher strains at the shear line, and one tooth base at the lower left corner. Since

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(a) 3,790 lbs.

(b) 4,420 lbs.



(c) 5,050 lbs.



(e) 6,320 lbs.

(d) 5,690 lbs.

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(f) 6,920 lbs.

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Top chord axial force is given below each drawing.

(g) 7,270 lbs.

Figure 35. Sequence drawing of Stress-Coat cracks on 3-11/16" x 6-3/4" plate.

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(a) 3,790 lbs. top chord force.



(b) 4,420 lbs. top chord force.



(c) 5,050 lbs. top chord force.

Figure 36. Large scale of initial Stress-Coat cracks on 3-11/16" x 6-3/4" plate.



(a) 5,690 lbs. top chord force.



(b) 6,320 lbs. top chord force.

Figure 37. Large scale of later stress cracks on 3-11/16" x 6-3/4" plate.



Dark areas are where Stress- Holes somewhat elongated. Coat crazed off the plate.

(a) 6,920 lbs. top chord force.

Original location of plate had moved about as shown dashed.



(b) 7,270 lbs. top chord force (ultimate load).

Figure 38. Large scale of Stress-Coat cracks at failure of 3-11/16" x 6-3/4" plate. this plate has only nine rows of teeth, instead of thirteen, as in the 5-5/16" width, stress cracks would be expected to cover a larger percentage of total plate surface area.

Figures 37 and 38 follow the sequential increase in stress cracks at increasing loads on this same plate. They indicate, in Figure 38(a), that even at a top chord force of 6,920 lbs. (278 psi axial contact area stress), while the holes behind the teeth are considerably elongated and one corner of the plate is lifting, that there are still no stress cracks in the outermost row of teeth, either top or bottom of plate. This same observation is verified in Figure 38(b) even at ultimate load (7270 lbs. total, equivalent to 292 psi contact stress).

Figure 38(b) indicates the approximate distortion of the plate at ultimate load, and shows why the corners at the upper left and lower right lift up first and pull out their teeth. Those two corners are trying to become further apart, extending that diagonal dimension and pulling those teeth first. The other diagonal is shortening and imposing still higher forces on the upper right and lower left teeth, but not pulling them because they are being forced closer together, in the early stages of S-shaped distortion, or plate buckling.

Nailed plates were also subjected to the Stress-Coat analysis in an attempt to get a clearer picture of plate stresses. Figure 39 shows the Stress-Coat cracks that had occurred in a 3-3/8"x5-1/16", 20 gauge plate at 0.260"



lower right or upper left corner nails.

This plate is 3-3/8"x5-1/16" - 20 ga., a flat, nailed plate shown full-size, with the Stress-Coat cracks that had occurred by 0.260 in. deflection.

Figure 39. Stress-Coat cracks in nailed plate specimen 44.

deflection. Note that very few cracks had occurred at the upper left and lower right extreme nails, verifying the earlier analytic and Stress-Coat work.

Figure 40 shows the stress pattern for a larger plate, 3-3/8" x 7-5/8" with 24 holes, half of which had 1-1/2" long, 8d, screw type nails located as shown. The stress cracks indicate the distribution of strains near each nail, in accordance with the nail's push against the plate, and its attempt to buckle the 20 ga. plate.

Figure 41 shows the same size plate as Figure 40, but oriented roughly at right angles to the crack. This drawing verifies that the stress cracks form at lower loads when a plate is oriented perpendicular to the crack than when its long dimension is parallel to the crack. Keeping the plate parallel to the crack (or parallel to the bottom chord in the standard orientation) reduces the eccentricity and increases the joint's over-all strength since a higher portion of the truss plate's capacity is available for axial load resistance.

# Determination of Top Chord Axial Force

The top chord axial force was determined as follows:

a. The total load applied on the test specimen was computed, being corrected for the hydraulic gauge discrepancies noted in the calibration data, Table
4. page 64 and Table 5, page 65.



Very few cracks at upper left or lower right corner

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Stress-Coat cracks in nailed-plate specimen 36. Figure 40.



Figure 41. Stress-Coat cracks in nailed plate specimen 37.

- b. The total load was divided by two to get the value of the two equal reactions. All loadings were applied symmetrically.
- c. For the 24'-0" trusses, continuity was counted at the quarter panel points since the 2"x4" chords were continuous members across those joints. The peak, heel, and bottom chord splice joints were assumed as pin-connected. To account for the twospan continuity of the chords, 5/8 of the top chord load on each side was assumed to act at the quarter point (for a two-span continuous beam on unyielding supports) rather than 1/2 as in the case of pinconnected joints. The vertical heel panel load, then, was only 3/16 of the top chord load instead of 1/4 as for pin-connected designs. This analysis resulted in the net reaction being 13/16 of top chord load, rather than 3/4 for pin-connected, increasing the calculated axial force in the top chord by about 8-1/3% over a pin-connected analysis.
- d. The 8'-0" specimens were assumed pin-connected throughout.
- e. Top chord axial forces were computed using the geometrical relationship of forces at the heel joint after the net reaction had been computed.

Determination of Contact Stress and Shear Line Stress

The contact area stress was determined by dividing the top chord axial force by the area of the heel plate. The area of one plate equals one-half the area of the front and rear plates. This was a straight P/A stress calculation. No allowance was made for end distance or edge distance and none for eccentricity.

The shear line stress in the steel was computed by dividing the top chord axial force by the length of one truss plate measured along the shear line crack. To get the stress per inch on one plate, these values would have to be divided by two, for the front and rear plates.

### Comparison of Six Plate Types

The load-deflection data for the initial series of 8'-0" test specimens are given in the Appendix in Tables 27 through 32. The results of repetitive tests on six different 20 ga. Plates manufactured by Troy Steel Corp. were compared statistically using Duncan's New Multiple Range Test. Duncan's Test compares all possible pairs of means to determine whether the differences are significant.

The six truss plates used for this evaluation were all impaled in kiln-dried western hemlock (tsuga Heterophylla).

a. 3-11/16" x 4-1/2" - 2 specimens

b. 3-11/16" x 6-3/4" - 5 specimens

c. 2-7/8" x 9" - 5 specimens

d. 5-5/16" x 4-1/2"  $\perp$  - 5 specimens

e. 5-5/16" x 6-3/4" - 3 specimens

f.  $5-5/16'' \ge 6-3/4'' \perp - 4$  specimens (perp. to crack) The three  $5-5/16'' \ge 6-3/4''$  plates in group e were applied parallel to the crack, rather than parallel to the bottom chord (the usual position). They were applied off-center, and had only four rows of teeth (about 1.84 inches) instead of six rows (about 5.31''/2 = 2.65'') as normally required. The contact area calculations were based on actual area, 1.84''  $\ge 6.75''$ , rather than the expected area. This group, then, had actual contact area about equal to that of the  $3-11/16'' \ge 6-3/4''$  plates in group b.

The statistical comparison of these 8'-0" specimens, done in part on Michigan State University's CDC 3600 Computer using the AES Stat Series, Description 13, was performed using the cards and data given in Table 8. The output for each of four levels of deflection (0.015", 0.040", 0.080", 0.150") and ultimate load is given in Table 9 along with the Duncan Table of Mean Differences for each level.

Initial Comparison of 8'-0" vs. 24'-0" Test Specimens

The load-deflection data for the 8'-0" and 24'-0" matched specimens are given in Tables 33 through 38. The results of repetitive tests (two in each cell) were analyzed with the M.S.U. CDC 3600 Computer using AES Stat Description 14. Analysis of Variance with Equal Frequency in Each Cell, in two separate preliminary analyses as follows:

a. 8'-0" vs. 24'-0" specimens - See Table 6, next page.

b. 8'-0" small jig tests vs. 8'-0" Riehle tests - See Table 7, page 98.

These preliminary analyses indicated that the following factors had a significant effect on strength (stress level):

- a. Species of lumber Douglas fir was stronger than white fir.
- b. Size of heel plate The 3"x5" plates were strongest,
  3"x8" next, and 5"x5" weakest, in terms of contact area stress.
- c. Length of test specimen The 8'-0" specimens were significantly stronger than the 24'-0" trusses, all other factors being equal.
- d. Species and plate size had a significant interaction.
- e. Species and deflection level had a significant interaction.
- f. Plate size and deflection level had a significant interaction.

It was also found that the repetitions (whether the sample was No. 1 or No. 2 of a matched pair) were not significant in either preliminary analysis. The level of deflection had a highly significant effect on contact area stress, as would certainly be expected. The location of the test jig used, whether the small 8'-0" hand hydraulic jig used at home, or the Riehle mechanical testing machine at M.S.U., had no significant effect on results. Table 6. Preliminary Comparison of 8' vs. 24' Specimens.

ANALYSIS OF VERIANCE TABLE

DEPENDENT VARIARLE IS X( 6) STRESS

CF. AT.	Reps. not sig.	Specie highly si	Length highly si	Plate size highl sig.	Defl. highly sig	No specie-length interaction	Specie interacts with plate size	Specie interacts with defl.	Length interacts with plate size	No length inter- action with defl	Plate size inter acts with defl.	3-way interactio here	No interaction here	<b>3-way interactio</b> <b>here</b>	No interaction here			
APPRCX, SIGNIFICAN Probability of F St	0,385 1.	<0,0005 2.	<0.0005 3.	<0,0005 4.	<0,0005 5.	0,045 6.	<0.0005 7.	<0,0005 8.	<0°0002 0.	0.222 10.	<0.0005 11.	0.015 12.	0,218 13.	0,001 14.	0.422 15.			
F STATISTIC	0,74820	413,59890	. 55,61346	28,46873	747,49689	3,55943	22,34373	27,86948	11.65221	1.51213	6,77085	4.54208	1,43715	4,80091	0.95299		Į.	
4EAN SOUARE	143,0416666	79590.04146603	10500,1666651	5375,07291663	141132,0555344	572,04166666	4215,63541663	5261,93055558	2200,01041663	2A3,5000000	1278,37847221	<b>3</b> 57,57291666	271,34375000	305,440972 <b>2</b> 1	179,93055555	1 R9, 80671165	1	
UEGS, OF Freedom	1	1	1	~	£	1	2	3	2	3	9	2	Ŷ	Ŷ	3	£5 .	95	
SUH OF SGUARES	145,0414666	) hecoc.04140403	1556, 16646651	10750,14583325	423396,16666412	672,04166666	R437,27083325	15785,79166675	4476,02083325	856,500n0n0r	7676.270A3337	1715,14583331	1628,06250n0ņ	5438,64583325	. 539,7916666	1rt06,72971753	58r031.83337402	( 2) SPECIE ( 3) LFNSTH ( 4) PL, STZF ( 5) DFFL,
SOUACE OF Variance	Repetitions (No. 1 or No. 2)	pecie Doug. Fir or White Fir	Length 1 (8'-0" or 24'-0")	Plate Size (3x5, 3x8, or 5x5)	Deflection Deflection 1 (.015,.040,.080,.150	8 Specie-Length	C Specie-Plate Size	D Specie-Deflection	IC Length-Plate Size	D Length-Deflection	<b>D</b> Plate Size-Deflection	BC Specie-Length-Plate Size	COLength-Plate Size-Defl.	CO Specie-Plate Size-Defl.	RD Specie-Length-Defl.	IEMAINING ERROH	OTAL	A IS CATEGNAY VAPIABLE X B IS CATEGORY VAPIABLE X C IS CATEGORY VAPIABLE X D IS CATEGORY VAPIABLE X

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Table 7. Preliminary Comparison of 8' Small Jig vs. Riehle Machine.

ANALYSIS OF VAHIANCE TABLE

DEPENDENT VARIAPLE IS X( 6) STRESS

SOUNCE OF VARIANCE	SUM OF SUUARES	DEGS. OF Freedom	WEAN SOUARF	+ STATISTIC	APPPOX. SIGNI	FICAWCE F STAT
E (No. 1 or No. 2)	372,09375 <b>0</b> 0r	1	372,0937500-	0.65411	0.422	1. Reps. not sig.
A (Doug. Fir or White Fir	r) 81142.51N41603	1	81142.51041603	142.64296	<0.00.05	2. Specie highly sig.
B (Home or M.S.U. test)	518,01041666	1	518.01041666	. 0.91043	0_344 .	3. No effect of location
C (3x5, 3x8, 5x5)	19858.27nA33u2	2	1391511°6266	17.45473	2000.42	4. Plate size highly sig
Deflection D (.015, .040, .080, .150	))392006.6145858A	3	130658,87152463	229.79675	200.02	5. Level of defl. highly sig
A <sup>n</sup> Specie-Location	981.76041667	1	9A1.74041667	1.72587	0.195	6. No specie-location interaction
AC Specie-Plate Size	9135.14583325	2	4567,57291663	6.02947	0.001	<ol> <li>Specie interacts with plate size</li> </ol>
An Specie-Deflection	12798.2A1250un	3	4246.0937500f	7.49949	<0.005	8. Specie interacts with load
BC Location-Plate Size	3291.02083331	2	1645.51041666	2,89269	0.04	<ol> <li>9. No location-plate size interaction</li> </ol>
8 <sup>n</sup> Location-Deflection	4NE3.2A125AUP	£	1341.09375009	2,3=755	0.042	<pre>IO. No location-defl. interaction</pre>
Cn Plate Size-Deflection	14266,72916651	so.	2367 <b>.</b> 78819442	4,14241	0.002	<ol> <li>Plate size inter- acts with defl.</li> </ol>
APC 3-way Interactions	13A2,645A3331	2	691.3229166A	1.21530	0.305	<pre>[2. No 3-way inter- action!!!</pre>
BCC3-way Interactions	3296.31250000	æ	549°3R541666	0,94578	0.457	<pre>13. No 3-way inter- action:!:</pre>
ACD3-way Interactions	3956 <b>.1</b> 875000n	Ŷ	659,36458333	1,15912	0,342	<pre>[4. No 3-way inter- action!!!</pre>
A <sup>AD</sup> 3-way Interactions	1063.03125000	3	354,34375000	16229*0	0.603	l5. No 3-way inter- action!!!
REMAINING ERRAR	31149,09367371	53	568.85092403			
TATAL	5741An.9895019=	66		1		
A IS CATEGORY VAPIABLE X A IS CATEGORY VAPIABLE X C IS CATEGORY VAPIABLE X D IS CATEGORY VAPIABLE X F IS CATEGORY VAPIABLE X F IS CATEGORY VAPIABLE X	( 2) SPECIE ( 3) LOCATION ( 4) PL, SIZE ( 5) DFFL, 1 AFFL					

Final Statistical Comparison of Matched 8' and 24' Specimens

A final statistical analysis was prepared, after the preliminary results were available as a guide to the interaction effects, combining all the specimens, plus the extras that had been deleted earlier from the initial comparisons to make all the cells equal. This final statistical analysis used the M.S.U. AES Stat Series Description 18, Analysis of Covariance and Analysis of Variance with Unequal Frequencies Permitted in the Cells (Least Squares Routine).

This LS routine permitted the inclusion of moisture Content and specific gravity as covariants along with the Category variables of species, length of test specimen, Plate size, and deflection level. It required the creation of twenty "indicator variables" as described in Description 18 for all these categories and the two-way inter-actions mentioned previously. The transformation instructions for the creation of those indicator variables are given near the beginning of Table 17 followed by the data cards. Two additional covariants were created, (a) the square of the moisture content and (b) the square of the specific gravity, as Variables nos. 29 and 30, with the transformation sub-deck.

The computer output from this analysis is reprinted, after slight abridgement to reduce unnecessary material, as

Table 18. Statistics on Transformed Variable.
Table 19. Analysis of Variance for Over-All Regression.
Table 20. Simple Correlation Coefficients.
Table 21. Measured Stress vs. Predicted Stress.

#### CHAPTER V

# DISCUSSION OF RESULTS

# General

This section presents load-deflection curves of each set of plates evaluated experimentally to permit quick, convenient visual comparison of the data. These load-deflection curves are grouped according to their purpose, and include a small drawing of the plate size, orientation, and other pertinent data. These load-deflection curves can be compared in terms of top chord axial force (Graph A for each figure), contact area stress in lbs. per sq. in. (Graph B for each figure), or shear on the joint in lbs. per lineal inch (Graph C for each figure).

The statistical analysis of the experimental results is **presented** in more detail in this chapter for each comparison **studied**. The raw data input, the computer statistical output, **other** comparison calculations, and a discussion of the sig**nificance** of the findings is included.

A prediction equation for the contact area stress is **presented**, along with a table comparing the predicted contact **stress** with the experimentally measured contact stress. **Finally**, the results of the theoretical and experimental **analyses** are compared.

# Initial Study of Effect of Size, Shape, and Orientation on Contact Area Strength

Description

Six different types of heel joints, using 20 ga. truss **plates** manufactured by Troy Steel Corporation impaled in western hemlock were compared. The plate sizes, orientation, and load-deflection curves are shown in Figures 43 through 47. The raw data for these plates is in the Appendix, Tables 27 through 32.

Statistical Comparison

This data was prepared as the computer input given in Table 8, for comparison of the contact area stress at 0.015", O.O40", 0.080", 0.150", and ultimate load. The results, including Duncan's Multiple Range Comparison of Mean Differences, are given in Table 9 (a) through (e).

Analysis of Results

An analysis of Tables 9 (a) through (e) yields the following:

a. From Table 9(a), for 0.015" deflection, there are no significant differences between the plates tested. This is reassuring since truss plate design values are based on strength at 0.015" deflection, as well as on ultimate. Any plate size, shape, and orientation can be used at the same relative efficiency for this low level of load.



Figure 42. Load-Deflection Curves for 2-7/8"x9" Plates.

3000 NO 2000 N SHLAR ON JOINT - LES PER SQ. IN OF AREA

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Plates (Parallel to Crack).

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Figure 46. Load-Deflection Curves for 5-5/16"x4-1/2" Plates (1 to Bottom Chord).

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- b. From Table 9(b), both 2-7/8"x9" and 3-11/16"x6-3/4"
  heel plates are significantly stronger than 5-5/16"x
  6-3/4" plates applied perpendicular to the top
  chord, at 0.040" deflection.
- c. From Table 9(c), 2-7/8"x9", 3-11/16"x6-3/4", 5-5/16"x6-3/4" (parallel to the crack), and 5-5/16"x 4-1/2" plates perpendicular to the bottom chord are all highly significantly (at 0.01 level) stronger than the weakest ones, 5-5/16"x6-3/4" plates applied perpendicular to the crack. It might be noted that these range from 55% to 88% stronger than the weakest ones.
- d. From Table 9(d), at 0.150" deflection, the same results as in c above, plus the fact that both 2-7/8"x9" and 3-11/16"x6-3/4" plates are significantly stronger than the 3-11/16"x4-1/2" plates.
- e. From Table 9(e), at ultimate load, all plates were significantly stronger than the 5-5/16"x6-3/4" applied perpendicular to the crack. Also, the 2-7/8"x9" and 3-11/16"x6-3/4" were the strongest, and were significantly better than all the others. (The 5-5/16"x6-3/4" plates applied parallel to the top chord were not positioned uniformly over the two members, which made their results, based on the lesser contact area, appear better than normal.)

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U TONY STEEL TOUSS PLATE COMPARISON (UNEO1)
D.6.24
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X(1) \bullet \bullet X(5) = AOV(X(6)) *
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401
     76 10118225530432513
412
        7212225521123113
403
     77
4^4
     17 132203240274291 3
405
     65 39104144177213 3
416
     69 77166202228239 3
407
     70 71161228270305 3
     71 128200246281305 3
408
400
     24 6610813815516612
     72 7111214016117612
410
     73 5910313515515912
411
412
     74 6911213314115012
413
     9 112219279300212 2
    15 146245308340364 2
414
415
     20 75156240303345 2
     30 35122101308335 2
416
     34 48134209270315 2
417
    14 159256322357367 4
418
410
     21 103216288339355 4
420
     23 72147208243329 4
     35 76160240201304 4
421
422
     3 45138214254292 4
423
     67
        77147100220220 5
     68 62125156187200 5
424
END OF DUN
```

Table 9(a) Duncan's Multiple Range Comparison of Six Plate Sizes at 0.015" Deflection Level

SUM OF SQUARED

	HIIS	FRED	MEAN	HEAN INCREMENT	SUM OF SQUARES	STANDARD Devlation	PEVIATIONS FROM THE MEANS
(OVERALL)	2004,004000	24	83.6666667		<u> 193864.00000</u>	33.532161	25861.333336
CATEGORY							
2-7/8" × 9"	414.00000	Ś	53.2000000	-0.466667	43014.080088	45.03394	6402.806800
5-5/16" x 4-1/2" L	447. PDA000	5	89.4000800	5.733333	46299.00000	39.803266	6337.208800
3-11/16" × 6-3/4"	455,00000	5	91.0000000	7.33333	48875.00000	43,214581	7470.006860
3-11/16" x 4-1/2"	130,00000	2	69.5000000	-14.166667	9273.00006	10.406602	112.508080
5-5/16" x 6-3/4" L	264, AOTOUO	*	66.00000000	-17.666667	17522.00000	5.715476	00000000
5-5/16" x 6-3/4"	287.000030	3	95.66666667	12.000000	28381.09006	21.901938	924.464667

					Table of	Mean Di	fference	S
Rank	Size	Freq.	Mean	P=2	P=3	P=4	P=5	P=6
1.	5-5/16" x 6-3/4"	ю	95.67 psi	4.7	6.3	12.5	26.2	29.7
2.	3-11/16" x 6-3/4"	ъ	91.00 psi	1.6	7.8	21.5	25.0	
3.	5-5/16" x 4-1/2" <b> </b>	ъ	89.40 psi	6.2	19.9	23.4		
4.	2-7/8" x 9"	ъ	83.20 psi	13.7	17.2			
ъ.	3-11/16" x 4-1/2"	2	69.50 psi	3.5				
6.	2-5/16" x 6-3/4" T	4	66.00	Z	o signif	icant di	fference	s.

	SUM OF SQUARED Deviations From The Means	46937.62 <b>388</b> 0		11608.000000	6390.79999	9910.799999	242.008600	54.756800	2524.004100	
tte Sizes	STANDARD DEVLATION	15.274841		53,851648	39.971240	49.776500	15,556349	4.272002	35.538711	
ison of Six Pla evel	SUM OF SQUARES	658461.050088		£64725.00000	<u> 45502.00006</u>	181476.00098	37234.00000	47361.00000	82233. 0400ef	
Range Compari Deflection Le	MEAN INCREMENT			15.375000	7.175000	25,575000	-23.625000	-50,875000	3.375000	
's Multiple at 0.040"	HEAN	159.62500800		175.0000000	166.80000000	1.85.20000000	136.6000000	108,75000000	163.0000000	
Dunca	FREQ	24		5	2	Ś	2	*	-	
ole 9(b).	SUM	3 <b>831.000000</b>		875,000000	R34.000000	924,000090	222.00000	435,000000	489. n0n030	
Tat		(OVERALL)	CATEGORY	u6 × u8/2-Z	5-5/16" x 4-1/2" L	3-11/16" x 6-3/4"	3-11/16" x 4-1/2"	5-5/16" x 6-3/4" T	5-5/16" x 6-3/4"	•

Table of Mean Differences

								I
Rank	Size	Freq.	Mean	P=2	P=3	P=4	P=5	P=6
1.	3-11/16" x 6-3/4"	ъ	185.2 psi	10.2	18.4	22.2	49.2	76.4*
2.	2-7/8" x 9"	S	175.0 psi	8.2	12.0	39.0	66.3 <b>*</b>	
3.	5-5/16" x 4-1/2" <u>T</u>	S	166.8 psi	3.8	30.8	58.1		
4.	5-5/16" x 6-3/4"	3	163.0 psi	27.0	54.3			
5.	3-11/16" x 4-1/2"	2	136.0 psi	27.25				
.9	5-5/16" x 6-3/4" L	4	108.75 psi					
* De	notes statistical sig	nifican	re at 0.05 le	vel				

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<pre>c Plate Sizes</pre>	
Si:	
of	
Comparison	ction Level
Range	Deflec
Multiple	at 0.080"
Duncan's	
9 (c).	
Table	

111	SUM 5222.60000	FREQ 24	HEAN 217.56333533	MEAN INCREMENT	SÛM DE SQUARES 1207390.080080	55.426797	FROM THE MEANS
	1227,000000	2	245.4000800	27.816667	\$10467.080086	48.876647	9361.208865
/2" 1	1060.00000	5	212.00000000	-5.583333	231640.00000	41.393269	6920.008480
5/4"	1281.00000	2	256,2000000	38.616667	53769,00099	48.725763	9496.808083
1/2"	355.000000	2	177.5000000	-40.083333	63937 . DEDDB0	30.405592	924.508800
/4" 1	544,0000.10	+	136.5000000	-81.09333	74558.040088	3.109126	29,006800
4''	75%.000000	£	251.00000000	33.416667	189899.080080	6.928203	96.006480

						Table of	E Mean D	ifference	S
Rank	Size	Freq.	Mea	ц	P=2	P=3	P=4	P=5	P=6
1.	3-11/16" x 6-3/4"	Ŋ	256.2	psi	5.2	10.8	44.2	78.7*	119.7**
2.	5-5/16" x 6-3/4"	3	251.0	psi	5.6	39.0	73.5	114.5**	
3.	2-7/8" x 9"	Ŋ	245.4	psi	33.4	67.9	108.9**		
4.	5-5/16" x 4-1/2" T	ъ	212.0	psi	34.5	75.5**	4		
5.	3-11/16" x 4-1/2"	2	177.5	psi	41.0				
6.	5-5/16" x 6-3/4" L	4	136.5	psi					
* *	Denotes statistical s Denotes statistical s	ignifica ignifica	ince at ince at	$0.05 1 \\ 0.01 1$	evel. evel.				

Sizes
Plate
Six
of
Comparison tion Level:
Range Deflec
Multiple tt 0.150"
Duncan's a
9(d).
<b>[able</b>

SOUARED TIONS E HEANS	. 033313		.008800		. 606603	.000000	000000	.00000	
SUN OF DEVIA FROM TH	15075		3194	8166	10164	002	216	4868	
STANDARD Devlation	64,578768		28,259742	45.185175	50,418326	29.498485	102501.0	49.325450	
SOM OF SQUARES	1637176.080000		271574.00000	815191. DĚODOG	450616.00000	57410.0000	93652,00000	218233.080000	
NEAN INCREMENT			52,59333	-5.615667	43,383333	-45.415667	-100.416667	13.583335	
MEAN	253,41666667		396.00000000	247.80300000	296,600000000	208.0000000	153,00000000	267.000000000	
FRE3	24		ŝ	5	5	~	•	3	
SUM	6092.00001		1531.000010	1239,000033	1484.00000	414,000000	619,00000	A01.000000	
	(OVFRALL)	CATEGORY	<u>//8 x 6 3 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2</u>	5-5/16" x 4-1/2" L	<u>-3-11/16" x 6-3/4"</u>	3-11/16" x 4-1/2"	-5-5/16" x 6-3/4" L	5-5/16" x 6-3/4"	

Differences	
Mean	
of	
Table	

Rank	Size	Freq.	Mea	a .	P=2	P=3	P=4	P=5	P=6
1.	2-7/8" x 9"	Ŋ	306.0	psi	9.2	39.0	58.2	<b>*</b> 0 <b>*</b> 0	153.0**
2.	3-11/16" x 6-3/4"	Ŋ	296.8	psi	29.8	49.0	88.8*	143.8**	
3.	5-5/16" x 6-3/4"	ъ	267.0	psi	19.2	59.0	114.0**		
4.	5-5/16" x 4-1/2"	r T	247.8	psi	39.8	94.8*	*		
ъ.	3-11/16" x 4-1/2"	2	208.0	psi	55.0				
6.	5-5/16" x 6-3/4"	Н 4	153.0	psi					
* *	Denotes statistical Denotes statistical	significa significa	nce at nce at	0.05 0.01	level. level.				

	SUM OF SQUARED Deviations From the Means	189108.008880	1664.808883 7000 2000 2000 2000 2000 2000 2000 2000	4113,199997	362.75000			P=6	72.45**						
tte Sizes	STANDARD PEVLATION	68.875439	20.408980 42.42858	32.067117	10.996711 51.696865		fferences	P=5	116.2** 1	166.65**					
of Six Pla	DF SQUARES	3962.060080	3460.000000 2321.000000		6313.00000 8311.00000 8211.00000		of Mean Di	P=4	64.5**	110.4**	127.6**				
parison ad	N7 50H	194	0.4				Table	P=3	44.9	58.8*	71.3*	107.9**			.1.
Range Com timate Loi	MEAN INCREME		50.1	52.900	-113.7500			P=2	5.8	39.1	19.7	51.6	56.3*		0.05 leve 0.01 leve
Multiple at Ul	MEAN	276.5000800	335.20000800	329.400000000	200 33333333			Mean	335.2 psi	329.4 psi	290.3 psi	270.6 psi	219.0 psi	162.75 ps:	ficance at ficance at
incan's	REO	24		-	•			Freq.	ß	S	ю	Т Т	5	Т 4	signi signi
le 9(e). Du	L WUS	6636.0098CD	1676.00000					Size	"6 x	5" x 6-3/4"	' x 6-3/4".	' x 4-1/2"	5" x 4-1/2"	' x 6-3/4"	statistical statistical
Tab		(ERALL)	50RY 591 2 4-1 / 21	x 6-3/4"	x 6-3/4" L				2-7/8"	3-11/10	5-5/16'	5-5/16'	3-11/1(	5-5/16'	Denotes : Denotes :
		(0)	CATE( 2-7/8" x	3-11/16	5-5/16" 5-5/16" 5-5/16"			Rank	1.	2.	3.	4.	5.	.9	* *

Summary

The over-all conclusions from this series of tests and statistical comparisons of six plate sizes and orientations were that:

- a. At 0.015" deflection, any plate size may be used.
- b. At high levels of deflection (and high loads), plates ranging in width from 2-3/4" to about 4" and in length from two to three times their width are the most efficient, being about twice as strong as the nearly square plates applied in the weakest possible direction.
- c. The comparison of load-deflection curves is shown in Figure 47 for the average values of these six plate sizes, shapes, and orientations.

### Comparison of Matched Specimens

Description

Fifty-six specimens were tested to evaluate the effect of each of the following factors on contact area stress:

- a. Size of truss plate (3"x5", 3"x8", or 5"x5").
- b. Length of test specimens (8'-0" or 24'-0").
- c. Species of lumber (Douglas fir or white fir).
- d. Level of deflection (0.015", 0.040", 0.080", 0.150").
- e. Moisture content.
- f. Specific gravity.
- f. Location of 8'-0" tests (at home on small jig, or at M.S.U. on Forestry Dept.'s Riehle Testing Machine).

The plate size, specimen length, species, load-deflection curve, and other pertinent data for each group of specimens is given in Figures 48 through 59. The raw data is given in the Appendix, in Tables 33 through 46.

Comparison of 8'-0" vs. 24'-0" Specimen Length

The results of an initial comparison of 24 matched specimens was reported in "Test Results" of the chapter on "Experimental Analysis." Load-deflection curves comparing 8'-0" specimens with full-scale 24'-0" trusses are given in Figures 48 through 53.

The load-deflection curves for the 24'-0" trusses are shown with solid lines, while the 8'-0" specimens and curves are shown dashed. The 8'-0" specimens had higher values than the 24'-0" trusses for all cases except the 3"x5" plates in Douglas fir (Figure 48). However, by taking the average ultimate contact stress from the data Tables 33 through 38 in the Appendix, the comparison in Table 10 can be made:

Table 10. 8'-0" vs. 24'-0" Specimens at Ultimate Load.

Description		Average Ultimate Contact Stres			
Plate Size	Species	8'-0''	24'-0''	8'/24' Ratio	
3''x5'' 3''x8'' 5''x5''	D. fir """	301 317 287	322 422 290	93½% 75 99	
3''x5" 3''x8" 5''x5"	Wh. fir """ """	232 225 220	233 193 202	100 116½ 109	

8' average = 99% of 24'

This means the 8'-0" specimen average was almost identical to the 24'-0" average at ultimate load. Ultimate load data was not included in the statistical analysis.

A similar comparison at the other loads is given in Table 11.

Table 11. 8'-0" vs. 24'-0" Specimens at Four Deflection Levels.

Deflection	Comparison						
0.015" 0.040"	8'-0'' 8'-0''	specimen	is "	8½% 21 %	stronger "	than "	24'-0'' 24'-0''
0.080"	8'-0"	11	11	9 %	11	11	24'-0"
0.150"	8'-0."	11	11	4 %	11	11	24'-0"
Ultimate	8'-0"			1 %	weaker	**	24'-0"
Over-all	8'-0"	specimen	is	8 %	stronger	than	24'-0"

Comparison of Small 8'-0" Jig Results with Riehle Machine Results

As a result of concern over the data from the 8'-0" specimens tested on the small hand operated hydraulic test jig, an additional set of 24 specimens 8'-0" long was built, listed in Table 12.

Group	Quan.	Heel Plate	Species
1 2 3	4 4 4	3"x5" 3"x8" 5"x5"	D. fir """
4 5 6	4 4 4	3"x5" 3"x8" 5"x5"	Wh. fir """

Table 12. Riehle Machine 8'-0" Test Specimens

Two samples, the first two tested, were selected from each group and matched in a Preliminary Analysis of Variance to compare the effect of test location. The results are

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3"x8" - White Fir.



shown in Table 7 which showed there was no significant effect due to location. The tests performed on the small 8'-0" hand-operated jig were just as valid, and essentially the same, as the tests performed on the Riehle testing machine.

Comparison of Douglas Fir vs. White Fir

The same specimens were compared for the difference in species, and the load-deflection curves are shown in Figures 54 through 59. The Douglas fir trusses are shown with solid lines, while the white fir specimen curves are shown dashed. The Douglas fir specimens had higher values than the white fir in all cases. By making the comparison of average ultimate contact stress from the data Tables 33 through 38 in the Appendix, the species comparison in Table 13 can be made:

Table 13. White Fir vs. Douglas Fir at Ultimate Load.

Description		Average Ultimate Contact Stress			
Plate Size	Length	White Fir	Doug. Fir	White/Doug. Ratio	
3"x5" 3"x8" 5"x5"	8 ' 8 ' 8 '	232 225 220	301 317 287	77 % 71 76½	
3"x5" 3"x8" 5"x5"	24 ' 24 ' 24 '	233 193 202	322 422 290	725 455 695	
				6)412 \$ 69 \$	

White fir averaged 69% of the ultimate value of Douglas fir.





Figure 55. Load-Deflection Curves for Douglas vs. White Fir - 3"x8" - 8'.















Figure 59. Load-Deflection Curves for Douglas vs. White Fir - 5"x5" - 24'.

A similar comparison of the other loads is given in Table 14.

Deflection	Comparison						
0.015" 0.040"	White	fir "	averages	728	of "	Douglas	fir
0.080"	11	11	11	62%	11	11	11
0.150"	11 -	11	11	69%	11	11	11
<b>Ultimate</b>	11	11	11	69%	**	11	.11

Table 14. White Fir vs. Douglas Fir at Four Deflection Levels.

Comparison of 3"x5", 3"x8", and 5"x5" Plates

Using the same data, the average ultimate loads, based on plate sizes are shown in Table 15.

Table 15. 3"x5", 3"x8", and 5"x5" Plates Compared at Ultimate Loaa.

	Average U	ltimate Contac	ct Stress
Length Specie	3"x5"	3"x8"	5"x5"
8'-0" Doug. fir 8'-0" White fir 24'-0" Doug. fir 24'-0" White fir	301 232 322 233	317 225 422 193	287 220 290 202
	$\frac{4)1088}{272}$	4)1157 289	4 <u>) 999</u> 250

The 3"x5" plates fail at 94% of the ultimate stress of 3"x8".

The 5"x5" plates fail at 865% of the ultimate stress of 3"x8".

Similar comparisons were made and the results given in Table 16.

		Ave	rage Con	ntact Sti	ress	
	3"	3"x 5"		x8''	5"x5"	
	psi	8	psi	8	psi	8
0.015" 0.040" 0.080" 0.150"	82 163 223 256	124 110 104 100	66 148 215 257	100 100 100 100	67 130 187 229	101 88 87 89
Ultimate	272	94	289	100	250	86½
Ave. % of 3"	x8" value	= 106%		100%		90%

Table 16. 3"x5", 3"x8", and 5"x5" Plates Compared at Four Deflection Levels.

## Final (4-way) Comparison, including Moisture Content and Specific Gravity

Description

A final comparison of contact area stress, involving all fifty-six specimens, was made on a lest squares statistical routine on the M.S.U. CDC 3600 Computer using A.E.S. Stat Description 18, "Analysis of Covariance and Analysis of Variance with Unequal Frequencies Permitted in the Cells." This comparison was more complete than the preliminary comparison of 8'-0" vs. 24'-0" (Table 6), or the comparison of the 8'-0" jig vs. the Riehle testing machine (Table 7), since it included all the specimens, plus evaluating the effect of moisture content and specific gravity. It was not necessary to delete specimens just to keep all cells equal. It was possible to include moisture content and specific gravity as covariants, and even to include the square of moisture content and specific gravity.

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Data

The load-deflection data from Tables 33 through 46 in the Appendix was used, for 0.015", 0.040", 0.080", and 0.150" deflection. The actual data input for the computer program is given in Table 17. A part of that program is the transformation sub-deck described further under the sections on "Creation of Indicator Variables."

# Results

The computer output from this program, after slight abridgement, is included in Tables 18, 19, 20, 21, and 22. It should be noted in Table 19, that for the 224 observations,  $R^2 = .9104$ , which means that this set of variables accounted for 91% of the variance, a relatively high percentage for this type of research.

Summary of Final Analysis of Variance Comparison

By construction of an analysis of variance table from the data output, Table 22, the following conclusions could be drawn:

a. Species had a highly significant effect on strength with Douglas fir being about 59% stronger than white fir. This is a crucial factor since equivalent grades of the two species are often used interchangeably. That is a dangerous practice unless appropriately reduced tooth values (i.e., larger plates) are used.

Table 17. Data Input for Final Analysis of Variance.

I DEMAND + MT	77	87	21121 07206504
CLIDDOLITTHE TOANSILLY	20	<b>A</b> 7	21122106206504
COMMON/A/ND.NT.IS.IDD.JD . DIMENSION	×(21	201	
DOUBLE DECISION Y	20		21122202206504
1F(X(2)+FO+1+)X(9)=1+			
IF(X(2) * F(0 * 2 * ) X(0) = -1 *	40	e /	
IE(X(3) = E(-1 + X(1)) = 1	41	99	71121 77777
	42	88	31122160223474
	47	.88	112226722270
x(1/2) = x(11) = (-x(n))	10	29	21120250252424
IF (Y(1)) +NF +-1 +) Y(12)=1 +- Y(11)	ለፍ	80	41121 06202543
X(13)=X(14)=X(15)=0.0	16	80	1122186202543
[F(Y(5),FO,4)X(13)=X(14)=X(15)=-1.0	47	80	112222902542
K=X(F)	40	80	11120705202543
1F(X(5)+LT+4)X(12+K)=1+0	40	04	12121 72135771
X(16)=X(9)+X(1))	50	04	12122110125271
X(17) = X(0) + X(12)			
Y(18) = Y(0) + Y(12)	~1	. '24	121241201 1- 431
	52	<b>0</b> 4	12124237135371
	57	75	22121 71147306
x(20)=x(0)*x(15)	50	05	22122125147306
X(21)=X(11)+X(13)	55	35	22122172147306
X(22)=X(11)*X(14)	56	20	22120231107306
X(23)=X(11)#X(15)	67	06	22121 82150255
X(24) = X(12) + X(13)	50	06	22122162150255
X(25)=X(12)+X(14)			22122210 100000
			4212494KIEGHEE
ALCOJAALICJEALID) MIDDL-MIAALUMIAI	60	06	32124264150355
X(27)=X(10)+X(11)	- 61	07	42121 60154351
X(28)=X(10)+X(12)	62	<b>7</b> 0	42122112154751
X(29)=X(7)#X(7)	67	07	42123190154251
X(30)=X(R)#X(R)	64	97	42124226154351
PF TURN	65	00	11131 76108500
END	£ 6		11131 /819/360
	57	an	1113-100108500
PUN 1 030 0 2100 0 2	69	90	11134230108500
0*u*25t	60	10	21131 84106462
SSCP(X(6) X(30)0X(5))TRANS1.PES*	70	<b>0</b> 1	21132162196462
FOPMAT(8X+5F1+0+F3+0+F3+1+F3+3)	71	01	21137216196462
1 98 11111101278485	72	01	21130200106063
2 98 11112187278405	73		2112114180500
2 OP 1111212720405	7.	00	3113112140-00
	-4		411321 MIRG=00
4 99 11114 705278485	75	92	31133216180500
5 99 21111 98260485	76	92	31134229190500
6 00 21112173260485	77	50	41131 03213440
7 99 21113232260485	78	οj.	11132166213040
8 99 21114276260453	70	5	41137215213040
Q 100 31111 84201404	80	93	41134240213440
	81	126	12131 70147357
		• 0 ¢	13133130143353
11 100 11112248561000		106	
12 100 31119200201000		1.10	12133147147147
13 101 4111100303671	44	106	12134223147363
14 101 41112195397571	85	107	22131 57143308
15 101 41113232307571	86	107	22132110143308
16 111 41114296397572	97	107	22133173143308
17 102 12111 93169444	98	177	22134217143709
18 102 12112150160444	90	108	32131 66147364
	20	108	32132125147364
19 192 1211.0189169444	01	100	22122102107760
20 102 12114210160444		100	
UNERDISE 11155 103200		1114	121 30 2014 / 160
OBEEDIELSISS EUL SC	<b>ה</b> ט	100	42131 69130400
03 103 SSII3122103360	<b>04</b>	100	121 321 261 38000
24 103 22114221103380	<b>05</b>	100	12122122129400
25 104 32111 76132346	96	109	12134237138400
26 104 32112134132346	07	<b>e</b> 2	11211 03150404
	~ /	22	
CT 199 1011319713C180			1121210154464
2M 104 32114220132346	00	H2	11212241150454
29 105 42111 68160359	100	82	11210200150050
30 105 42112121160359	101	83	2121112173510
31 105 42113113160359	102	97	21212100173520
72 105 02114227160750	173	83	21212222173510
33 96 11121 66228587	100	AR	21214260177510
34 46 11133303330507	105	A۵	31211 86182400
	104	5.4	31313131183400
	107		31313241102400
30 80 11120386228587			121 220 11220 30

108	84 31214318182400
00	85 41211 83160470
	85 A1212170160470
:10	
111	R5 41217242160479
112	85 41214318160479
113	59 12211 60202347
114	59 12212100202347
	E0 13313175303347
11-	
1:16	SG 12214215202347
117	60 22211 74214380
118	60 22212110214780
110	61 22213161214380
120	60 22210206210380
100	A6 11221 72104605
120	40 11221 2194805
130	46 11222136194605
171	46 11223245194605
172	45 11224716194605
1 77	47 21221 77167458
	47 21222140167450
1	
1	4/ 2128 2.1410/454
136	47 21224725167458
145	62 12221 53202305
146	62 12222114202305
1 4 7	62 12222163202205
1 4 7	Be Tree Toseves
149	62 12224200202395
140	61 22221 37196406
1 = 0	61 22222 83196406
151	61 22223130196406
182	61 22224157196404
141	AQ 11931 7517454F
101	
107	49 1123214-174-48
163	49 11233213174548
164	49 11,234267174548
165	48 21231 72178515
166	48 21232142178515
167	48 21233211178515
168	48 21234259178515
181	63 22231 40196405
182	63 22232 87196435
107	67 22227126156405
10.5	03 22233128100403
1 44	03 222341071904 17
185	64 32231 70196393
186	64 32232112196393
187	64. 32233157196393
188	64 32234192196393
193	78 11111120198489
104	78 11112220108080
1	78 11112271108400
1.40	76.11113271196489
196	/H 11114205108440
197_	29 2111177215533
198	79 21112264215533
.199 .	.79.21113278215533
200	79 21114202215533
201	80 31111 95233498
202	80 31112187233498
203	80 31113246233498
204	80 3111637833408
2	
276	MI 41112250142502
277	B1.41113311142502
20 <b>8</b>	A1 41114734142502
209	51 12111113190417
210	51 12112144190417
211	51 12113169190417
212	51 12114197190417
212	52 22111 00140402
SL2 .	
214	76 27117163169402
215	52 22113207169402
216	52 22114241169432
225	40_11121 00185551
226	40 11122243185551
227	40 11123329185551

228	41 11120754195551
220	41 21121 771R4547
230	41 21122108184567
231.	41 21123248184567
222	41 21124272184567
241	54 12121 52162367
242	54 12122127162367
247	54 12127181162367
200	54 12124226162367
245	53 22121 63186405
246	53 2212213619640F
247	53 22123182186435
249	53 2212421018640F
257	58 11131 79206514
258	58 11132163206514
259	58 11133252206514
260	58 11134305206514
261	57 21131 501074R4
262	57 21132153197484
267	57 21137222107484
264	57 21134254107484
277	S5 12131 55182380
274	55 12132101182380
275	55 12133137182380
276	55 12134173182380
277	56 22131 86170392
279	56 22132138170392
270	56 22133177170392
280	56 22134217170302
293	38 11111 63202503
294	38 11112148202503
205	38 11113215202503
296	38,11114232202503
207	39 21111 40175442
208	39 21112164175442
299	39 21113246175442
300	09 211110316175442
101	• 44 11211102173483
302	44 11212236173483
303	44 11213208173483
304	44 11214710173483
305	45 21211127172511
306	45 21212228172511
3^7	45 21213313172511
POP	
X(6)	)=P(X(7)++X(3n))PF<+NR4
RZ()	((?))RL()*
9Z()	(10))PLO#
RZO	((11) •X(12))RLO#
RZO	((13)•••X(15))RLO#
R7()	((16)+X(17))RLO*
R7()	((18)+++X(20))RL0#
87()	((21)•••X(26))PLO*
R7()	((27)+X(28))RL0*
R7()	((7))PLO#
77()	<(A))RLO#
R7()	((7),X(A))RLO#
END	OF PUN

Table 17. (cont'd.)

- b. The length of test specimen (whether 8'-0" or 24'-0" long) also had a highly significant effect on strength with the 8'-0" specimens generally about 15% better test values than the 24'-0" trusses in the 0.015" to 0.150" range. Despite numerous retests, calibration of gauges, and careful reevaluation of the test procedure, this difference could not be explained. Strengths of 8' and 24' specimens were essentially identical at ultimate load. Ultimate load was not included in the statistical analysis to premit study of interactions with deflection.
- c. The heel plate size had a highly significant effect on strength with the 3"x5" and 3"x8" plates being approximately 45% and 39% respectively, stronger than the 5"x5" (based on axial contact area stress, psi).
- d. Level of deflection had a highly significant effect
  on stress level, as would certainly be expected.
  Higher levels of deflection result from higher loads,
  which certainly cause higher stresses.
- e. Plate size interacts significantly with species.
  The 3"x8" plates tested almost 90% better in Douglas fir, whereas the 3"x5" plates were 40% better and the 5"x5" plates only 25% better. This can be explained by the theory that it takes a wider "development width" in white fir to balance the

buckling strength of the steel plate; i.e., a 5" wide plate which almost always buckles in Douglas fir will come closer to that same strength in white fir where buckling distortion is not a problem, than will 3" wide plates which never buckle in Douglas fir.

- f. Plate size interacts with deflection. See Table 23 for values. The 3"x5" plates performed significantly better in the lower ranges, but the larger plates did better at the higher deflection levels.
- g. Moisture content had a significant effect on strength with the lower moisture content lumber giving better heel plate test results, as would be expected.
- h. Specific gravity did not have a significant effect on contact area strength, in the range included in the study.

## Stress Prediction Equation

## General

The use of M.S.U. A.E.S. Stat Description 18, Analysis of Covariance and Analysis of Variance with Unequal Frequencies Permitted in the Cells (Least Squares Routine), resulted in the computer developing a regression equation of best fit to accommodate the data from all the 56 specimens tested.
Statistics on Transformed Variables 1 Final (4-wav) Comnarison α ι Tahla

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1

			-		Ŭ																							
	SQUAREN DEVIATIONS FROM THE MEAN	1477922.55355835	5917.31928543	1.08783696	219.42857143	1A2.85714285	155. 42857143	126.00n000	<b>111.98214286</b>	110.99553571	118.99553571	155.4285743	128.0000000	<b>111.9</b> R214286	118.99553571	118.99553571	79.98214286	78.99553572	78.2955221	64.000000	64. 8 n n 0 0 0 0 0	64.000060	169-0080000	128.000000	21411632.24853516	0.92028176	0.0000000	279.95982143
	SUM OF SQUAPES	6688798.8800000	86878.4799954	47.46048700	224 .0500000	224.000000	160,000000	128.000000	112,000000	111.0000000	111.0000000	160.0000000	128.000000	112.0500000	<b>111.0</b> 000000	111.900000	60,000000	79.0000000	79.0500000	64.000000	64.000000	64.000000	160.000000	128.0000000	56044752.172A5156	10.95066644	224.000000	1665.000000
T2011 - 010 - 11001	S C I	40190.0001000	4289 90999988	101.0530000	32,0000000	96.0000000	32.00010000	0.00000000	2,0000000	1.0000000	1.00000000	32.0000000	0.0000000	2.0000000	1,000000C	1,0000000	2.0000000	1.00010000	<b>1</b> 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0°0000000	00000000	000000000000000000000000000000000000000	00000000	0.0000000	88078.4799954	47.40048700	224.000000	557.0000000
(4-Way) CUMPAI	STANDARD DEVIATION	A1.40918497	5.15121967	0.06984406	0,99195999	0.90553144	0.83485874	0.75762196	0,70863395	0.70550537	0.70550537	0.83485874	0.75762196	0,70863395	0,70550537	0,70550537	0.5988590	· 0,59518070	0,59518070	0.53571962	0.53571962	0.53571962	0.84204710	0.75762196	309.86495864	0.06424036	0000000000	1.12045759
TOUL LINAL	2 2 2 2	179 41964285	19 15178571	0.45470189	0_14285714	0 42857143	0.14295714	0,0000000	0_00992757	0.00446429	0.00446429	0.14285714	00000000000	0 C C B 9 2 8 5 7	0,00446429	0.00446429	0_0.0892457	0 01446429	0 00446429	0,6000000	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	000000000000000000000000000000000000000	0000000000	0,0000000	393,20750200	0,21160932	1,000,000	2.4A660714
1 80 16	LAREL VAR NO	ength 6	st. Cont. 7	c. Grav. 🔋	cie 9	gth 10	Plate 11	Plate 12	5" Defl. 13	0" Defl. 14	0 Defl. 15	Fir 16	Fir 17	5 Fir 18	0 Fir 19	0 Fir 20	P1015" 21	P1040" 22	P1080" 23	P1015" 24	P1040" 25	P1080" 26	x 3x5 Pl. 27	x 3x8 Pl. 2A	ist. Cont.)' 29	ecific Grav.) <sup>2</sup> 30	CONSTANT	
		Str	Moi	Spe	Spe	Len	3x5	3×8	.01	.04	80	3x5	3×8	.01	.04	.08	3 X 5	3x5	3×5	3x8	3×8	3×8	80	- ∞	W)	(Sp		

	•							R2 DELATES	0.91035	0.96640	0.89498	0.90415	0.90023	0.47072	0.00402	0.91035	0.0036A	0.91960	0.96616	0.94976	0.91057	0.98456	1.212.0		0.90916	0.05424	0.90945
ion		810	6 40 .00 B			OF ESTIMATE	67912	PARTIAL CORP. COEPS	0.07640	0.12769	ROQOE. 0	0.26492	0.13454	•0.0103E	40,46697 0.45534	ā0,07636	40.40210	50.84692	0.82410	0 1 1 1 1 0 0 1 0 1 1 0	87828.88	40.25684		4 5 1 1 2 1 5 1 4 4 0 5 4 0 2 9 2	0.20002	0.62334	-0.11621
Regress		•	84.742			DAPD ERBOR	25.727	816	0.279	0.071	50.000E		<pre><pre><pre><pre><pre><pre><pre><pre></pre></pre></pre></pre></pre></pre></pre></pre>	<0.0005	20 <b>00.</b> 07	0.81		0.508	100.0		0.487	\$0.00 · 0>	0 - 2 - 5		0,004	50.005 S	0.100
<b>r-all</b> ]	TART.)	<b>\$</b> DUARE	4852048	1347278		STAN		<b>F</b> B	1:1006	22222	35.6077	15 8209	- 16,5096	962.8665	55° 2943	1011	12 11 10 1 10 1 10 1 10 10 1 10 10 10 10 1	ñ. 1392	1025203		<u>ā</u> 1 k90 a	14,0549	29292	200000000000000000000000000000000000000	8. 2932	126:4576	2:7244
/ for Ove ents.	OVERALL CORS	D4 MEAN	56091.7	661.9		2	0 /9487	. 18	1,0066	19191	5.9572	3 8757	4 0035	631,0272	-7.4494	5080*1-		-0.6427	3=2450	1.5743	-0-9306	+3+7489	-1-5043	1,6345	2,9796	11:2453	-1,6506
son - AOV Coefficie	ROPRIATE IF NO	DEG OF FREED	24	199	223	RR COEFS R BAR 2	0.9001	STD. ERRORS OF BETAS	0.0000	0.37480	0.05250	0,02253	0.02850	0.02656	0.02645	0.02592	0.02591	0.02645	0.02645	0.0295	0.02977	0.02917	91620.1	0,02919 D.02864	0,02750	0.01133	0.35638
) Compari gression	S MAY BE INAPP	JF SQUARES	1.77249146	.78106308	2,5535635	MULTIPLE CO R	0.9544	BETA WEIGHTS	0.0000	0-46068	0.31277	0.08732	0.11500	• 0 • 62 4 0 B	-0.19763	•0.02802	0.09028	80.01752	0.08584	0.04218	e 0 . 0 2 4 7 3	=0.10936	-0.0408F	0.04778	0.07928	8 9 1 4 5 2	+0.54822
Final (4-way and Re	(LINES 1 AND 2	SUN	EAN) 1346201	13172(	EAN) 147792	R2	0.9109	STD, ERRORS Of COEFFIGIENTS	103.71101690	436.85750145	4.30887471	2.02955206	2.76005090 1.00043485	3.05096380	3.05205440 7.052440	2.52791222	2.78444304 3.05132620	3.05201929	3.05235545	4.06531815	4.07246919	4,43276288	4.43357516	4.43576789 9.75971738	2.95508831	0.02136613	451.62240716
Table 19. 1			EGRESSION (ABOUT M	ROA	TOTAL (ABOUT M	SNOI		REGRESSION COFFEICIENTS	112, 69-89422	793.39420706	25.66 63379	7.85-40559	11, 21429423 5 01477547	-94.66283142	-22,73411972	-2.73n93943	-18 0084008	-2,02269755	9,90407162	6.40459123 5.95007573	-3.38979295	-16, A1A15330	-6.569865n1	7,25440845 -8.84492820	8.51n04162	0.24126934	-745.43050633
			œ	il.		ORSERVAT	224	VAR	0	, <b>9</b>	• •	7	10	12	₩ U ₩ 4	2	1	0	20		23	2	2	<b>0</b> 2 0	28	62	·.) <sup>2</sup> 30
									CONSTANT	MOIST, LONT.	Specie	Length	3x5 Plate	.015" Defl.	.040" Defl.	3x5 Fir	3x8 Fir	.040 Fir	.080 Fir	3x5 P1. 015"	3x5 P1. 080"	3x8 P1015"	3x8 Pl040"	3x8 Pl080" 21 2 725 Pl	8' x 3x8 P1.	(Moist Cont.) <sup>2</sup>	(Specific Grav

Final (4-way) Comparison - Simple Correlation Coefficients. Table 20.

SIMPLE CORRELATIONS

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										1.9800	0.45374	0.61299	0.0453	0.00453	0.01530	0.00724	0.0074	0000010	0.000.0	0.0000	0.0000	0.0000	0.15432	0110706	0.0000	-0.61233	16	3F
				1					1,00000	0.00653	0.000.0	0:06271	0:06303	0:13520	0102420	0.07421	0,16024	0 : 0 0 0 0 0	0.00000	0.00000	0:00750	0100010	- 101010-	-0.00269	00001	-0130989	15	80
									0.49548	0.00030		0.06271	01222.0	0.06403	9.17420	0.16814	0.07471	0.00000		0000010	0.00750	0.0000	-0.60155	•0.80819	0.00000	- 0. 62677	1	84
				1		!	t. 00000	6.49325	6.49325	0.01299	0.0000	0.14272	0.06271	0.66271	0.16987	0.07433	8.4733	0.0000	0.00000	0.0000.0	0.01494	000000	6 • Č 6 7 9 4	0.00460	0.00000	• 0 • • • • • • • • •	13	15
				•		1.0000	0.0000		0.0000.0	0000000	0.0000	0.0000	0.0000	0.0000	0000000	C . D 0 0 0 0	0.000	0.0000	0.0000.0	G . 0 0 0 0 0	0.22361	C.50000	0.02292	0.11092	0.0000.0	0.0000	12	88
				* +	1:00000	0.45374	0.01209	0.00693	0200653	0:17647	3.0000	0:01209	0.00653	0.00653	0:01530	0.00774	5.00774	010000	3 = 0 0 0 0 0 0	0000010	0.40584	0.22607	0;21152	0:09917	0.0000	-0:01233	11	35
				1. 1. 00000	-0.08135	000000	0.00799	0.00401	0,00401	-0.08135	0000000	8.00799	0.00401	8.00401	0.00945	8.00475	0.00475	0.00000	0.0000	0.0000.0	0.18706	0.00000	8.11601	-0.07602	00000000	-0.00758	10	
			1.00000	-0.06847	0,14852	0.00000	0.01094	0.00549	0.00549	0.14852	0,0000	0.01094	0,00549	0.00549	0.01294	0.00651	0.00651	0.0000	0.000.0	0.0000.0	0.000.0	0.0000	0.27528	0.84929	0.000.0	-0.01037	•	SP
		1.00000	0.84877	-0.09901	0,10187	0,09034	0.00431	-0.00015	-0.00248	0.11817	0.12457	0.01518	0.00531	0.00622	0.01154	-0.00018	-0.01018	0.00360	0.0000.0	0.01719	0.11271	0.09847	0.33566	0.99730	0.0000.0	-0.00495	•	SG
	1,0000	0.41914	n. 36152	0.10914	0,23184	0,03516	n.05024	.0.154	-0.00574	D. 13383	0,00804	0.05024	-0.00154	n. 30166	n. 25945	-0,20183	0.0197	00000	0.0000	0.00487	n.29064	n. U1448	n.95937	0.41924	n.900n	- n , 14898	7	HC
1.00010	0,20616	0.35311	0.36975	0.04780	0.17033	0,11746	-0.74497	-0.44078	-0.17539	0.11464	0,0A171	-0,20318	-0.10364	-0.01971	-0.11404	-0.05936	-0.01627	-0.0.277	-0.05244	-0.02098	0.03043	0.09474	0.22140	0.34979	0.000.0	0.79029	•	s T P
æ	•	•	o	5	11	12	13	-	5	16	17	67	19	20	21	22	23	24	52	2¥	27	29	50	2Ú	c	ŝ		
Strength	Moist. Cont.	Spec. Grav.	Specie	Cength	5x5 Plate	<b>5x8</b> Plate	.015" Defl.	.040" Defl.	.080" Defl.	Sx5 Fir	5x8 Fir	015 Fir	040 Fir	080 Fir	x5 Pl015"	XS P1040"	XS P1080"	X8 Pl015"	x8 P1040"	X8 P1080"	TX 3x5 PL.	x 3x8 Pl.	Moist. Cont.) <sup>2</sup>	Specific Grav.)	CONSTANT			

Table 20. (cont'd.)

													T	4	T	
								,	1.0000	0.44721	0.25739	0.11474	0.000.0	-0.01417.	27	95
								1.0000	00000.0	0.00000	n.n0293	n.n0657	U 0 U 0 U 0 U	0.000.C	26	8
							1.0000	0.916.0	0.000.0	0.00000	0.000.0	0.0000.0	0.000.0	0.0000.0	25	4
						1.00000	n . 50/00	0.50000	0.0000.0	0.0000	0.00600	0.00528	0.0000.0	0.0000	24	<b>10</b> .
					1.00000	6.22502	5.27502	0.45005	0.00889	C.00000	0.00053	-0.00023	0.0000.0	►C.84362	24	58
				1.0000	3,49364	0:22502	9:45005	0.22502	0.00989	000000	-0.0182	-0.00022	0,0000	-0.09741	22	24
			1.00000	8.49053	8.49053	D.44726	0.22363	0.22363	0.01768	0.0000	0.08039	0.01132	0000000	-0.16021	21	51
		1.00000	0.07420	0.07471	0.16014	0.00000	0.0000	0,0000	0.00750	0.0000.0	0.00044	0.00519	0.0000	-0.03680	20	<b>8</b> 0F
	1.0000	0.49548	U.07420	0.16014	0.37471	0.0000	0.0000.0	0.0000	0.01750	0.0000	-0.0A153	0.00476	0.0000	-0.08218	19	40F
0000.1	A.49325	n. 49325	n.16887	n_07433	D.97433	0.0000	a.000n	0.0000	0.01494	0.0000	n.36794	0.11450	0.0000.0	-0.13540	18	15F
1.00000 0.00000	0.000.0	0.0000	0.000.0	0.000.0	0.000.0	0.0000	0.000.0	0.0000	0.000.0	0.000.0	0.00758	0.13887	0,000.0	0.000.0	17	<b>L</b> E
17	19	20	21	22	23	24	25	26	27	28	50	30	0	<b>r</b> i		
3x8 Fir .015 Fir	.040 Fir	.080 Fir	3x5 P1015"	3x5 Pl040"	3x5 Pl080"	3x8 Pl015"	3x8 P1040"	3x8 P1080"	8' x 3x5 Pl.	8' x 3x8 Pl.	(Moist. Cont.) <sup>2</sup>	(Specific Grav.) <sup>2</sup>	CONSTANT			

ONT.) 29 0.00968 1.00006 Grav.) <sup>2</sup> 30 0.11048 0.33919 1.00006 STANY 0 0.00000 0.30060 0.00000 5 0.00000 0.26 29 0.00523 0.00000 28 28 29 CONSTANT 88±	8 P1.	53	1.00000				
av.) <sup>2</sup> 30 0.110A8 0.33910 1.00006   v 0 0.00000 0.33910 0.00000   v 0 0.00000 0.00000 0.00000   v 0 0.00000 0.00000 0.00000   z 0 0.00000 3.0 0.0000   z 0 0.00000 3.0 0.0000   z 29 3.0 0 0.0000   B8# CONSTANT 0.0 0.0 0.0		53	0.00968	1.90000			
0 0	av.) <sup>2</sup>	50	0.110A8	0.33919	1.00000		
5 0,00000 -0,06523 -0,00515 0,00000 28 29 30 30 0 88# constant		0	0.0000	0.00000	0.0000	0.0000.0	
28 29 30 0 88≠ Constant		r	0.000.0	-0.06523	-0.0n515	0.00000	1.00000
BB# CONSTANT			2.A	29	gn S	•	ŝ
			88×			CONSTANT	

# Table 21. Final (4-way) Comparison

# - Measured Stress vs. Predicted Stress.

(224 Data Points)

RESIDUALS

·			etD		
		ñ P		FRIIMATED V	Y - ESTIMATED Y
1 08	1	1	101.0000000	88.91892031	12-08107969
2 08	2	2	187,0000000	174.58586897	48.41413103
3 98	3	3	223,0000000	239.95038510	-16,95038510
4 98	4	4	305.0000000	278.88726760	26.11273240
5 00	1	5	98,0000000	88,03487169	9,96512831
6 00	2	6	173.0000000	175,70182034	-2,70182034
7 00	3	7	232,10000000	239.06633647	-7,06633647
R OG	4	88	276,0000000	274.98944642	1.01055357
a too	1	9	84.ñ0000000	91.09824499	-7,09824499
12 100	2	10	169,0000000	178.76519364	=9,76519365
11 100	3	11	238,0000000	242.12970978	-4,12970978
12 100	4	12	299.0000000	281,06659228	17.93340772
13 101	1	13	109,0000000	134.46945952	-25,40945952
14 101	~ 2		185,000000	222.1364081/	
15 101	3	17		203.30092930	
16 101		- 10	296, 1000000		-2 20288102
17 102	. 1	1/		77.2V200178	Ā 00467490
<u>18 172</u>	<u>ç</u>	10			Ă. 10280401
10 1/12	3	17		200+00/40309 998.30207783	#5.30207783
31 1 12		21		74.76643042	=2.76643042
24-412-	2	22	133 0000000	128.66187420	4.33812580
23 103	3	23	177.00080000	165.33543894	15.66456105
24 103	4	24	221,0000000	204.86562633	16,13437367
25 104	1	25	76.000000	94.41348681	-18,41348681
26 104	ž	26	134.0000000	148.30893059	-24.30893059
27_104	3	27	195,0000000	187.81800799	7.18199201
28 104	4	28	220,00000000	224.51268272	<b>P4.51268273</b>
29 105	1	29	68,0000000	82.72117551	• £4,72117551
30 105	2		121,0000000	136,61661929	-15,61661929
31 105	3	31	113,0000000	178.12569668	-63+12569668
32 175		32	552' 40004000	212.8203/142	
3786	1	33			48 61114490
<u>34 HN</u>		- 34		278.00334408	34.90665592
10 DO		32	384.0000000	327.71550905	88.28449095
37 87	1	37	97.0000000	98.47204144	0.52795855
38 A7	2	38	196.0000000	195.23279388	0.76720612
30 87	3	39	303.0000000	281.15945216	21.84054784
40 87	4	40	363,0000000	333.78161713	29.21838287
41 BB	1	41	73.0000000	90.92389023	-17192389023
42 RA	2	42	160.0000000	189,68464267	-29,68464267
<b>4</b> 3 AA	3	43	263.0000000	275.61130094	-\$2,61130094
41 AA	. 4	44	350,0000000	328,23346591	21.76653408
44 . HU	1	45	96.0000000	98.02919697	•2,02919698
A6	2	46	186,0000000	198.78994941	• 80 . 78994941
47 89	3	47	278,0000000	202+/1660768	<b>PR</b> 71660769
40 00		48		74.04770404	<u> </u>
47 74	1	47		/9471332071 438.00987448	
		<u> </u>		201.07170409	
-1 ''4 53 04	J 4	91 <b>42</b>	237.00000000	252.35375122	-15+35375123
53 05		53	71,0000000	78.66284375	•2,66284375
54?	2	54	125,0000000	138,65209131	-13,65209131
	_	-			

Table 21. (cont'd.)

	<b>77 05</b>	-				
		3	55	172,0000000	200.72331085	-28,72331085
	<u>56 05</u>	• 4	50	231,1000000	251.10326806	-20,10326806
	57 06	1	57	83,0000000	57,98649930	25.01350070
	<u>58 06</u>	2	58	163,0000000	122,97574686	40,02425314
	50 06	3	59	236,0000000	185,04696640	50,95303360
	60	4	60	264,0000000	235,42692361	<u>88,57307,639</u>
	61 07	1	61	60,00000000	59,37547923	0,62452077
	62 97	2	62	118,00000000	124,36472680	-6,36472680
	63 07	3	63	180,0000000	186,43594634	+6+43594634
	64 97	Å	64	226,0000000	236.81590354	-10.81590355
	55 00	1	65	76,0000000	76.96205353	-0.96205353
	66 90	2	Å6	143,00000000	154.97174487	-15.97174487
	67 90	3	67	199,00000000	223, 69972491	- 24. 69972491
	60 97	Ă	68	230 0000000	263.64556812	-33.64556812
	60 91	Ť		84,000000	74.28548589	9,71451411
	70 91	;	70	162 0000000	154.29517723	7.70482276
	71 91	Ť	71	216 0000000	221 02315727	-5.02315727
	72 91	Ă	72		260.9600048	
	73 02		- 73		82 62646846	14.17361163
	74 92	-	74		449 41446094	
	75 02			214 0000000	220 36413084	
	76 02		7.5	228 0000000	248 100010904	-10100410909
						66 41447652
	77 43	1		. 93 . "UUUUUUU	0/,10070440	
	70 0.		70	100,0000000		10,0013441/
	78 01	3	/ 4	215,10000000	213,92003500	1,0/336414
	An at		<u> </u>	240.000000	223.8/24/908	
	<u>A1 106</u>	1	81	71,10000000	/8.03/08/19	-0.03/02/19
	42 104	<u></u>		128,0000000	122,2/52/300	
	A1 176	3	83	189,0000000	105,14781490	23,85218504
•	84 176	4	84	553°000000	202,85145041	20,14854959
	85 107	1	85	57,0000000	87,67846496	-30,67846496
	<u>A6 107</u>	2	86	110,0000000	133,91665143	-23,91665143
	<u>87 107</u>	3	87	173,nç000000	176,78919273	-3,78919273
	AA 107		88	217,0000000	214.49282818	2,50717182
	90 109	1	89	66,00000000	77,82865887	-11,82865887
	90 10A	2	90	125.0000000	124.06684534	0.93315465
	01 10B	3.	91	182.0000000	166.93938664	15,06061336
	72 108	4	92	224,0000000	204.64302209	<u>\$9,35697791</u>
	02.100	1	93	64,0000000	90.91743824	-22.91743824
	04 100	?	94	126.0000000	137.15562472	-11.15562472
	05 100	3	95	177.00000000	183.02816601	-3.02816602
	96 109	4	96	237. 10000000	217.73180147	19,26819853
	97 82	1	97	83,0000000	113.95883684	-30.95883684
	0A 42	2	98	169,00000000	199.57331971	-30,57331972
	99	3	99	241,0000000	264.99030162	-25,99030162
	28 00	4	100	298.0000000	303.92718412	<b>•5.92718413</b>
	21 83	1	101	112,0000000	107.63300673	4,36699326
	02 83	- Ž	102	149.00000000	195,42178575	-46,42178575
	03 83	3	103	232.0000000	258.66447151	-26.66447152
	04 83	4	104	269,00000000	297.60135402	-28.60135402
		1	105	86.0000000	103.42687598	-17.42687598
	26 84	2	106	171.0000000	191.09382464	-21.09382464
	<u></u>	3	107	261,0000000	254.45834076	6.54165923
		4	108	318,0000000	295.39522327	24,60477673
	00 9E	Ì	109	83.00080000	111.41952262	-28,41952262
		3	110	170.0000000	199.08447127	-29,08647128
			-111	242,0000000	267.4509A740	-20.45098741
		Ă	112	318 0000000	301.38784001	14. A1213000
		$\overline{}$	113		64.21 nA4An1	.4.210A4A01
		2	114	100.0000000	118.10420170	-1A,10A20170
	114 50	- <del>-</del> -	148		189. 6183601A	17. TRAATA92
	15-52	3	115	1/7, "Vuunuuu	131101330170	414304004CE

### 'Table 21. (cont'd.)

116	50	4	116	215,0000000	194.31004392	20,68995608
117	67	1	117	74.00000000	69.58105617	4.41894383
118	52	2	118	119,0000000	123.47649995	=4,47649995
110	62	3	119	161.00000000	162.98557734	=1.98557735
120	60	4	120	206,0000000	199.68025208	6.31974791
120	46	1	121	72.0000000	63.77853090	8.22146910
130	46	2	122	136,0000000	162.53928333	-26.53928333
131	46	3	123	245	248.46594161	-3.46594161
132	46	4	124	316.00000000	301.08810658	14.91189342
1 33	47	1	125	77,00000000	73.78769764	3.21230236
134	47	2	126	148.00000000	172.54845008	-24.54845008
1 75	47	3	127	238,00000000	258.47510836	-20.47510836
1 76	07	4	128	325.00000000	311.09727333	\$3.00272667
105	62	1	129	53.0000000	18.46345244	14.53654756
106	62	2	130	114.00000000	85.45270000	30.54730000
147	62	7	171	163 0000000	145.53301055	47.47408045
147	62		172	200 0000000	108 00787475	1 00(10705
140	61		177	37 0000000	20 74479011	44 45744080
150	61	-	130	37, 10001000	22.34030011	14.05301969
1.40			134	03, 10000000	67.33562767	4.33562767
151	61		1.35	130,0000000	149.40684/21	-19,40684/21
152	-61_	4	130	157,0000000	199.78680442	•42,78680442
161	40	1	137	75.0000000	70.79456051	4.20543949
162	47	5	138	145,0000000	150.80425185	-5.80425185
163	40	3	139	213,0000000	217.53223189	-4,53223189
164	40	4	140	267.00000000	257.47807510	9.52192490
165	40	1	141	72.0000000	69.17035976	2.82964023
166	49	2	142	142,0000000	149.18005111	·7+18005111
167	40	3	143	211,0000000	215.90803114	-4.90803115
168	48	4	144	259,0000000	255.85387436	3,14612564
181	67	1	145	47,0000000	51,52939993	-11,52939993
182	63	2	146	87,0000000	102,78456386	-15,78456386
187	63	3	147	126,00000000	151.85293449	-25.85293449
184	63	4	148	167,0000000	183.36074061	-16,36074061
185	64	1	149	70,0000000	49.14691198	20.85308802
186	64	2	150	112,0000000	95.38509845	16,61490155
107	60	3	151	157,00000000	138,25763975	18,74236025
100	64	4	152	192,00000000	175,96127520	16.03872480
102	70	1	153	120,0000000	97.17655415	22.82344584
100	70	2	154	224,00000000	184,84350281	39,15649719
105	78	3	155	271,0000000	248,20801894	22,79198106
106	78	4	156	295.0000000	287.14490144	7.85509856
107	70	1	157	177,00000000	94,29459159	82.70540841
100	70	2	158	264,00000000	181.96154024	82,03845975
100	70	3	159	278,00000000	245.32605637	32.67394362
200	70	4	160	202.00000000	284.26293887	-82.26293888
201	00	1	161	95,00000000	90.41633948	4.58366052
200	-	. 2	162	187 00000000	178.08328813	8.91671187
		3	143	246 0000000	241.44780426	4.55219574
	-	4	164	278 0000000	280. 38468677	-2.38468677
2.14	10	1	145	147 0000000	121 77798858	95.22201142
344	м	2	166	250 0000000	208 44493723	40.5550%277
ane	41		167	311: 0000000	272.80945336	38.19054663
207	81		168	374 00000000	311 74433584	22. 25366413
208			140	113 0000000	88.10002687	20.89007343
200	-51	2	170	144 00000000	139 00537045	6.00462075
210	51		171	149,0000000	174 51444805	- * E14440AE
211	51	3	172	107 0000000	218 20012278	-** 20012270
212	51		177	197,	88.34404103	43303047
213	52	1	1/3	90.0000000	140 04040575	1.03303803
214	52	- 5	175	103,0000000	192+202402/2	85.2285148E
215	52	3	. 1/3	207,0000000	101.//140319	27122021082
216	52	4	1/0	241.00000000	223.01/31283	1/+30208/1/

Table 21, (cont'd.)

225 4° 1 177	0(:00000.99	183.18512199	-4-18512199
226 41 2 178	243.00000000	201.94587443	41.05412557
227 40 3 179	329,00000000	287.87253270	41.12746729
222 40 4 180	354.0000000	340.40460764	(T. BASTA212
	108 0000000		-29,9021,970
	120*0000000	201.00200221	-3,00200222
271 41 3 143	247,0000000	287.58952049	•39.58952049
232 41 184	272,00000000	340.21168546	-68,21108540
241 54 1 182	52,0000000	59.63200791	•7,6320r791
242 54 2 180	127.00000000	124.62125547	2+37874453
203 54 3 157	181.0000000	186.69247501	<b>*5</b> +69247501
244 54 <b>4 188</b>	226,0000000	237.07243222	<b>*</b> £1+07243222
245 57 1 189	63,00000000	58.13548803	4.86451197
246 53 2 190	136,00000000	123.12473559	\$2,87526441
207 53 3 191	182.0000000	190.21293258	-8,21293258
248 57 4 192	210.0000000	235.57591234	-25.57591234
257 58 1 193	79.0000000	74.93337070	4.06662939
259 59 2 194	163.00000000	154.94306204	8.05693796
250 5P 3 105	252,00000000	221.67104208	31.32805702
	305 0000000	264 61488520	AT 1814474
		78 02408202	
		458 07447174	-2 03447374
	202 0000000		•2,9300/330
263 57 3 199	227 1000000	222,00407339	• 0 .00 40 7 3 4 0
264 57 4 200	254,10000000	201,01049001	-5,01049001
273 55 1 201	55,0000000	07,79204264	-\$0,79264264
. 274 55 2 202	101,0000000	112,03082911	-11.03082911
275 55 3 203	137,0000000	154,90337041	-\$7,90337041
276 55 4 204	173,00000000	192,60700586	-19,60709586
277 56 1 205	86,0000000	73,18115083	12,81884917
278 55 2 20 <b>6</b>	138,0000000	119,41933731	18,58066269
270 56 3 207	177,00000000	162.29187860	£4.70812139
290 56 4 208	217,00000000	199,99551405	17.00448594
203 38 1 209	63,00000000	96.80170267	-33,80170267
294 38 2 210	148,00000000	184.46865133	-36.46865133
205 38 3 211	215,00000000	247.83316746	-32.83316746
206 38 4 212	232,00000000	286.77004996	-\$4.77004996
207 20 1 213	40,00000000	100.49343286	-40.49343286
208 20 2 214	164,00000000	184.16038151	-84.16038152
200 30 3 215	246.00000000	251.52489765	-5.52489745
200 00 1 216	431.00000000	397.00409330	33.09590470
301 44 1 217	102.0000000	1 NR_ 0500RAR1	- % . 0R0084E4
202 AA 2 21A	236.0000000	A+FF0404 . 901	40, 1710474
		254 00144020	44 0.0855071
			41,00000071
3-14 44 7 220		<b>277.928331/9</b>	
11'5 45 1 671	127, 10000000		17,13/19373
			32,49024470
107 45 3 223	313,00000000	228.8/42/124	24,127/28/2
309 45 4 224	335 <b>,</b> r00000'0	247.411103/5	3/+18884025
	<b>B</b> , <b>M</b> , <b>M</b>		
			307 RE3
	AATAA'UCABUGAD		0.00000000
	PEV	COLV _ MEANINA	SC DEC
	~37 8/0708 20000	33(1 - MEAN 1) 4477000 FEEEDOFF	
	9048\A4°40000000	147/922,55355835	131/20 <b>0</b> 78106308

p2 0,91087437 .

SS(R - PREV R) 141279,17008209

D.W. STAT 1.07256554

Analysis of Variance Interactions.	
way) Comparison - , 2 Cofactors and	•
[able 22. Final (4-w for 4 Factors,	•

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DEPENDENT VARIARLE--X4 5) STR

			-			
1.	Species	SUM OF SQUARES 23489,79259087	DFG OF FRFEROM 1	MEAN SQUARE 23459,782597 <b>8</b> 7	55,4877	516 <0.0705
2.	Length	9942.56848645	4	9942.56848644	15.8209	<0.0105
3.	Plate Size	23735,13164091	~	11867.565A2C4K	17.9292	<0.0005
4	Deflection	919086.46629333	۰. ۱	304342,15543365	462,8432	<0.00.0×
ς.	Plate & Spècies Interaction	8476.01282763	~	4238.00641382	4.4027	0.002
و. و	Defl. & Species Interaction	30956.88358499	ñ	10318:96119499	15.5894	<80085
7.	Plate Size & Defl. Interaction	16224.21447253	×	2704,03574538	4.0452	Tu0'0
.8	Length & Plate Size	7737.47006333	~	3868,73503166	5.8446	\$00.0
6	Moisture Content	57738.15421009	1	57738,15421080	A7.2292	<0.0105
10.	Specific Gravity	2183.23093355	1	2163.23893355	3,2984	6.071
11.	Moist. Cont. & Spec. Gravity	57998.76101494	¢	24999.3885074 <b>7</b>	43.8114	<8.0n85

			Deflec	tion	
		0.015"	0.040"	0.080"	0.150"
Sizė	3''x5''	101.5	172.3	223.7	261.5
te	3"x8"	73.2	155.1	229.1	280.6
Pla	5"x5"	76.9	140.1	194.9	233.7

Table 23. Interaction of Plate Size and Deflection.

All other variables and covariates are held constant at their means.

τ,

Categories Studied

In order to describe the regression equation more detail, the data used in the analysis must be more completely explained. In punching the original cards for the Stat Description 14, Analysis of Variance, preliminary analysis for Tables 6 and 7, the following categories were used:

Category	Description	Value
A (X <sub>2</sub> )	Species	Doug. fir = 1 White fir = 2
B (X <sub>3</sub> )	Length	8'-0" = 1 24'-0" = 2
C (X <sub>4</sub> )	Plate Size	3"x5" = 1 3"x8" = 2 5"x5" = 3
D (X <sub>5</sub> )	Level of Defl.	0.015" = 1 0.040" = 2 0.080" = 3 0.150" = 4
E (X <sub>1</sub> )	Repetitions	Spec. #1 = 1 Spec. #2 = 2 Spec. #3 = 3 Spec. #4 = 4

By using equal number in the cells, that is, the same number of repetitions and all factors matched, the following number of data points must be used:

Species (2) x Length (2) x Plate Size (3) x

Deflection (4) x Repetitions (2) = 96 So 96 separate data cards must be used so that each point may be unique.

Creation of Indicator Variables for Categories

To use the Unequal Frequencies (Least Squares Routine) to perform an Analysis of Variance, the distinct category variables described above must be converted to <u>Indicator</u> <u>Variables</u>, denoted I.V., by use of a matrix, where each I.V. may have a value of 1, o, or -1.

For example, if the category has just two possibilities, (such as either Douglas fir or white fir), then just one I.V. is required, as follows:

Value of	x <sub>9</sub>	(I.V.	for	Species)
Douglas fir	. 1			
White fir	-1			

Similarly,  $X_{10}$  (I.V. for test specimen length) = 1 for 8'-0" specimens and -1 for 24'-0" specimens. If the category contains three possibilities, such as 3"x5", 3"x8", or 5"x5" plate sizes, two I.V.s are required in a matrix as follows:

Plat <b>e</b> Size	x <sub>11</sub>	X <sub>12</sub>
3"x5"	1	0
3"x8"	0	1
5112511	- 1	- 1

This same type matrix may be used for the levels of deflection (4 choices in the category) by using three I.V.s;

Level	of Deflection	x <sub>13</sub>	x <sub>14</sub>	x <sub>15</sub>
	0.015"	1	0	0
	0.040"	0	1	0
	0.080"	0	0	1
	0.150"	-1	-1	-1

Creation of Indicator Variables for Interactions

To accommodate interactions, such as plate size (2 I.V.s) with level of deflection (which has 3 I.V.s),  $2 \times 3 = 6$  new I.V.s must be created as follows: I.V. for Level of Deflection X<sub>11</sub>  $X_{12}$  $X_{13}$  $X_{21}$ X<sub>24</sub> X<sub>14</sub> X<sub>22</sub> X<sub>25</sub>  $X_{15}$ X<sub>23</sub>  $X_{26}$ 

Each of these Level of Deflection - Plate Size interaction indicator variables will have values as shown in the matrix following: ion

x<sub>22</sub> x<sub>24</sub> X 26 Description x<sub>21</sub> X<sub>23</sub> X<sub>25</sub> 3"x5" @ 0.015" def1. 1 0 0 0 0 0 3"x5" @ 0.040" def1. 0 1 0 0 0 0 3"x5" @ 0.080" def1. 1 0 0 0 0 0 3"x8" @ 0.015" defl. 0 0 1 0 0 0 3"x8" @ 0.040" def1. 1 0 0 0 0 0 3"x8" @ 0.080" def1. 0 0 0 0 0 1

It is not necessary to include the third plate size (5"x5") or the fourth level of deflection (0.150") since these are handled with the -1 values.

The Indicator Variables described in this section were created by the computer by use of a transformation sub-deck.

Regression Equation

After creation of the appropriate indicator variables, (indicator variables must be used not only for all the main categories to be studied, but also for all the interactions which are of interest), the Least Squares Prediction Equation for stress can be written in terms of these indicator

I.V. for Plate Size

Plate	Deflectio	n Interact
	Indicator	Variables

variables (along with the continuous variables used as covariants), by using the regression coefficients given in Table 19.

Y(stress) = 112.69 - 12.43 x Moist. Cont. + 793.29 x Spec. Grav. + 25.67 x Species (Indicator Variable) + 7.85 x Length (I.V.) + 11.21 x 3"x5" Plate (I.V.) + 5.94 x 3"x8" Plate (I.V.) - 94.66 x 0.015" Def1. (I.V.) -22.74 x 0.040" Def1. (I.V.) + 37.34 x 0.080" Def1. (I.V.) - 2.73 x 3"x5" - Fir Interaction Indicator Variable (1.I.V.) + 9.69 x 3"x8" - Fir (I.I.V.) - 18.90 x 0.015" - Fir (I.I.V.) - 2.02 x 0.040" Fir (I.I.V.) + 9.90 x 0.080" - Fir (I.I.V.) + 6.40 x 3"x5" - 0.015" (I.I.V.) + 5.26 x 3"x5" - 0.040" (I.I.V.) - 3.38 x 3"x5" -0.080" (I.I.V.) - 16.62 x 3"x8" - 0.015"  $(I.I.V.) - 6.67 \times 3'' \times 8'' - 0.040'' (I.I.V.) +$ 7.25 x 3"x8" - 0.080" (I.I.V.) - 8.05 x 8' - 3"x5" (I.I.V.) + 8.51 x 8' x 3"x8"  $(I.I.V.) - 0.24 \times (Moist. Cont.)^2 -$ 745.43 (Spec. Grav.)<sup>2</sup>.

The predicted stress of the particular sample can be computed by just putting in the appropriate values for moisture content, specific gravity, and a +1, 0, or -1 as required for each of the Indicator Variable (I.V.) and Interaction Indicator Variable (I.I.V.) terms. The computer has already done this for all the data used in the analysis and compares the measured stress ( $Y = X_6$ ) with the estimated stress, plus giving the differences (residuals, which equal measured stress minus predicted stress). See Table 21.

# 152 Theoretical vs. Experimental Analysis

General

The contact area stresses derived in the theoretical section were based, in the main, on a standard engineering analysis of eccentricity, with just two modifications; (a) teeth closest to the crack were not counted due to edge or end distance, and (b) the vertical component of top chord axial force was neglected in the eccentricity calculations since it is believed to act directly on the support through crushing of the feather end of the bottom chord, without being transferred by the heel plate.

The theoretical contact area stress, for each of the three sizes studied most closely in the experimental phase is given in Table 24.

Table 24. Theoretical Contact Stress for 3"x5", 3"x8", and 5"x5" Plates

Plate Size	Axial Stress	+ <sup>€</sup>	centr Stress	ic =	Total	Proportion
3''x5''	200	+→	138	2 2	323	130.2%
3''x8''	200	+→	66		248	100 %
5''x5''	200	+→	188		378	152.5%

Theoretical vs. Experimental Results at 0.150" Deflection

Comparing these results with those contained in Table 23 (using stress at 0.150" deflection as the reference level), and assuming that the 3"x8" plates are equal experimentally and theoretically, the percentage comparison values are in Table 25.

Plate Size	Experimental	Theoretical	Difference
3"x 5"	107.3%	130.2%	21.3%
3"x8" 5"x5"	100.0% 121.0%	100.0%	26 %

Table 25. Comparison of Theoretical vs. Experimental Results @ 0.150" Deflection.

If the theoretical results are exactly right for the 3"x8" size, then they are 21.3% and 26% too conservative for the 3"x5" and 5"x5" plates, respectively. The experimental stresses for both the 3"x5" and 5"x5" plates were much closer to the simple axial stress computation (no eccentricity considered) than either the proposed method of heel plate analysis or the FHA method.

When comparing experimental results at 0.150" deflection, the simple axial stress method is more accurate, especially for plates of the same width, than the more elaborate methods.

Theoretical vs. Experimental Results at 0.015" Deflection.

If the experimental results at 0.015" deflection (which is the design deflection) from Table 23, are compared with the theoretical values, Table 26 results:

Plate Size	Experimental	Theoretical	Difference
3''x5''、	72.0%	130.2%	80.7%
5"x8" 5"x5"	100.0%	100.0%	- 60.5%

Table 26. Comparison of Theoretical vs. Experimental Results @ 0.015" Deflection.

Summary

This means that at the lower deflection levels, due to the considerably better performance of the 3"x5" and 5"x5" plates, the more elaborate theoretical methods are even worse predictors than at the higher deflection levels. The simple P/A contact stress calculation method was more accurate for the plate sizes tested than the proposed method of analysis.

**-7** 

### CHAPTER VI

### **CONCLUSIONS**

A statistical comparison of average stress at ultimate load for repetitive tests of six different heel plate sizes yielded the following conclusions:

- Plates proportioned three times as long as their breadth are stronger by about 2%, but this is not significantly stronger, than those two times their breadth.
- 2. Plate lengths ranging from two to three times their breadth are from 13½% to 50% stronger (statistically significant) than those nearly square (one and onequarter times their width).
- 3. All plates applied with their long dimension parallel to the bottom chord are significantly stronger than those applied perpendicular to the bottom chord.

A check of the Stress-Coat crack patterns on several plates indicated the following:

 The shear stress in the steel plate is highest near the crack between the members.

٠.

- 5. The contact area remote from the crack is still flat and is not stressed to the buckling point even when the plate is destroyed at the shear crack if the plate width exceeds the "development width" for shear.
- 6. Shear stresses in the steel, as well as buckling stresses, are lower in plates applied with the teeth oriented parallel to the bottom chord than in those with teeth oriented perpendicular to the bottom chord.

Inspection of the photographs (confirmed by visual inspection of numerous specimens during failure) reveals:

- 7. The nearly square plates undergo rotation or sideways distortion during deflection of the heel joint, showing the effect of torsional forces.
- 8. Buckling resistance is higher when the entire plate area is backed up by wood than when a portion of the truss plate is over the triangular air space between members.

Comparison of matched 8'-0" and 24'-0" specimens showed the following factors to be statistically significant.

9. Douglas fir had about 42% stronger heel joints than white fir. This emphasizes the need to specify the species.

10. The length of heel plate had no effect on joint strength, for plates 3" wide. The 3"x5" plates had 3% more strength per square inch than 3"x8" heel plates.

- 11. Narrower heel plates are stronger than wider heel plates. The 5"x5" plates were only 82% as strong, on a per square inch basis, as the 3"x5" plates, which was a significant reduction.
- 12. Small plates are significantly better at the lower levels of deflection (0.015" to 0.040") whereas the larger plates were better at higher levels (0.080" to 0.150"), an inter-action effect of plate size with level of deflection.
- 13. Moisture content had a highly significant effect on results. The lower moisture content specimens gave better test values.
- 14. There was no significant effect of specific gravity on stress values. This was an unusual finding since all connector values for mechanical fasteners are based on species groupings by specific gravity.
- 15. The 8'-0" specimens tested better than the 24'-0" trusses by a significant amount which cannot be explained. The 24'-0" truss heel plates are about 92% as strong as the same plates on the 8'-0" specimen based on the statistical correlation.
- 16. The small 8'-0" hand-operated test jig provides an accurate heel test not significantly different from results obtained on the Riehle test machine.
- 17. Wider truss plates are weaker, due to their buckling in the steel, but provide a much more uniform,

**...** 

predictable load-deflection pattern and greater total deflection than narrower plates. This may be of benefit where a known safety factor is essential.

- 18. Where two plates are used on each side of the heel joint, both should be oriented the same direction, or their design strengths adjusted in accordance with load-deflection data relating their stiffness.
- 19. Average ultimate contact area stresses, figured on the straight P/A basis of gross area, were:

Plate Size		Doug. Fir	White Fir
3x5 3x8		315 374	226
5x5		264	227
2-7/8x9 3-11/16x6-3/4 3-11/16x4-1/2 5-5/16x6-3/4 5-5/16x4-1/2⊥ 5-5/16x6-3/4⊥	(Hem.)	335 330 309 290 (Unequal 271 163	areassee text)

- 20. Twenty gauge plates with all teeth parallel to bottom chord buckled at loads of about 575 lbs. shear per inch of plate (1150 pli on joint), and 500 pli shear if teeth were perpendicular to crack.
- 21. Twenty gauge plates with teeth in four directions did not buckle at loads of 675 pli shear (1350 pli on joint), but failed by tooth withdrawal.

### CHAPTER VII

### **RECOMMENDATIONS FOR HEEL JOINT DESIGN**

The following recommendations are based on this research:

1. Provide sufficient truss plate contact area to accommodate the top and bottom chord axial forces, using the TPI reduction factors for slope effect. An additional reduction factor of 20% is recommended for plates over 4" wide, to account for eccentricity.

2. Twenty gauge heel plates placed parallel to the bottom chord should be kept short enough (probably not exceeding 9" in most cases) to prevent tensile failures in the steel.

3. Twenty gauge heel plates should be kept narrow enough (probably not over -1/2" in most cases) to prevent buckling failure in the steel. If wide plates are used, they should be designed on the basis of their buckling resistance rather than their contact area.

4. Heel plates should be proportional from two to three times as long as their breadth, whenever possible, to increase their rotational resistance to eccentric forces.

5. Tooth values and plate sizes are highly dependent on species of lumber. Care in specifying the species on the

drawings must be followed in the actual production of the trusses, or larger plates used if a less desirable species is substituted in the design.

6. Heel plates should be positioned with the longest possible amount of plate over the crack to resist rotation, with equal contact areas on both members.

7. Heel plates should not be positioned perpendicular to the crack if avoidable, or, if this positioning is unavoidable, appropriately reduced tooth values should be used in the design, plus checking the buckling resistance of the reduced steel shear line.

8. Large sized heel plates, when used for girder trusses, widely spaced trusses, or other trusses with high axial forces, should be checked for buckling strength and tensile strength to prevent a misplaced feeling of confidence based on contact area size.

### CHAPTER VIII

### RECOMMENDATIONS FOR FURTHER RESEARCH

- Bracing (Bridging) Methods and Requirements for Flat Trusses.
- Load-Sharing (and Its Stress Increases) as It Applies to Trussed Rafters.
- Top Chord Column Buckling Resistance Provided by 2"x4" Roof Boards 24" O.C., or 3/8" Plywood Sheathing.
- Study Methods of Improving Stiffness of Long Span -Shallow Depth Flat Trusses.
- 5. Long Term Deflection Characteristics of Flat Trusses.
- Suitability of Metal Plates in Making Joints in Continuous Floor Joists.

# APPENDIX

# APPENDIX

## LOAD DEFLECTION DATA

This appendix contains the tabular test data obtained experimentally. The tables are grouped as follows:

	Tables		Purpose	Pages
27	through	<b>3</b> 2	Comparison of Six Plate Sizes.	163-168
33	through	38	Initial Comparison of Plate Size Specimen Length, Species, and Level of Deflection.	169-174
39	and	40	Substantiating Tests for Table 33.	175-176
41	through	46	Tests of 8' Specimens on Riehle Testing Machine to Verify Suitability of Small Hand Hydraulic Jig.	177-182

Load Deflection Data for 2-7/8" x 9" Plates. Table 27.

	Τò	p Cho 1b	rd Fo s.	rce		с С	ontac	t Ar ps	ea S i	tres	S		Shear	Lin pl	i St	ress	
#15		#20	#30	#34	Ave.	6#	#15	#20	#30	#34	Ave	6#	#15	# 20	#30	#34	Ave.
		0	0	0	0	0	0	0.	0	0	0	0	0	0	0	0	0
20	0	660	285	315	899	40	85	25	11	12	35	162	232	69	30	33	105
500	0	1230	570	630	1500	80	115	50	22	24	58	324	315	130	60	66	179
379	0	1860	920	1260	2152	112	146	75	35	48	83	458	400	196	97	132	257
4	0	2480	1380	1660	2724	139	172	96	53	64	105	562	472	260	145	174	323
22	00	3480	2440	2610	3793	182	219	134	94	100	146	740	600	366	255	275	447
33	80	4080	3160	3465	4555	218	245	156	122	134	175	890	670	430	333	365	537
6	40	4740	3625	4030	5139	245	267	182	139	155	198	990	730	496	381	425	604
13	50	5350	4130	4490	5614	258	282	206	158	172	215	1060	775	562	435	472	661
-	00	5840	4740	5060	6078	270	296	225	182	194	233	1100	810	615	498	503	705
0000	30	6280	4970	5430	6398	279	308	240	191	209	246	1140	845	660	522	572	748
23	60	6530	5300	5780	6594	286	321	251	204	221	253	1160	880	688	558	608	779
36	90	6760	5430	6060	6908	291	333	260	209	233	265	1190	910	710	572	638	804
8	06	7350		6600	7613**		341	282		254	292		935	171		695	800
00	90	7900		7015	8002**		349	303		270	308		955	830		740	842
32	85			7330	8308***	4 Phy. 5644 (1971)	355			282	320		975			770	872
948	80						364						1000			• •	
4	80	9000	*	8210	8740	317	364	345	*	315	335	1290	1000	950	*	865	1034

<sup>\*</sup> Opposite top chord broke prior to test joint; therefore ultimate load could not be determined. \*\* Average based on three specimens. \*\*\* Average based on two specimens.

6-3/4" Plate × 3-11/16" for Load Deflection Data 28 Table

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\*Estimated data; gauge removed to prevent damage.

Load Deflection Data for 5-5/16" x 6-3/4" Table 29.

6-3/4"
×
5/16"
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Deflection
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le 29.
Tab

	Top	Choi	d For	ce Cc	ontac	t Ar	ea.	tres	s She	ear Li	ine Si	tress
Heel			S.			Sd					011	
Def1.	#75	#76	#77	Ave.	#75	#76	#77	Ave	#75	#76	#77	Ave.
0.000	0	0	0	0	0	0	0	0	0	0	0	0
0.005	1900	1320	1190	1470	73	51	38	54	281	195	176	217
0.010	2550	2100	1780	2143	97	81	57	78	367	310	263	313
0.015	2990	2630	2270	2630	114	101	72	96	441	388	336	388
0.020	3370	3070	2690	3043	129	118	85	111	500	454	396	450
0.030	4110	3950	3360	3807	158	152	107	139	610	585	499	564
0.040	4820	4740	3850	4470	185	182	122	165	712	700	570	660
0.050	5240	5400	4280	4973	201	207	136	181	774	800	632	735
0.060	5660	6060	4740	5487	217	232	151	200	840	006	700	813
0.070	5980	6440	5200	5873	229	247	166	214	882	981	770	878
0.080	6320	6640	5580	6180	243	255	177	225	940	980	822	914
060.0	6620	6850	5750	6407	254	263	183	233	980	1010	850	947
0.100	6780	7050	5910	6580	259	270	189	239	1000	1040	880	973
0.125	7130	7440	6320	6963	274	286	201	254	1055	1100	940	1031
0.150	7470	7900	6620	7330	286	304	211	267	1100	1165	980	1081
0.175	7780	8100	7110	7663	298	310	226	278	1145	1195	1050	1130
0.200	8000	8300	7260	7853	306	317	230	284	1180	1225	1070	1158
Ult.	8200	8500	7260	7987	315	325	230	290	1210	1255	1070	1178

Since these truss plates were not all positioned equally on the members, the contact area was computed on the basis of the minimum area provided (26.1 in.<sup>2</sup> for 75 and 76) (31.5 in<sup>2</sup> for 77).

# Table 30. Load Deflection Data for 5-5/16" x 4-1/2" L to Bottom Chord.

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Table 30. Load Deflection Data for 5-5/16" x 4-1/2" L to Bottom Chord.

Heel		Top	Chor 1bs	d For	e		ő	ntac	t Ar	i S	tres	s		Shea	r Lin	i Str	ess	
Def1.	#17	#65	#69	#70	#71	Ave.	#17	#65	<del>6</del> 9#	#70	#71	Ave	#17	#65	#69	# 70	#71	Ave.
0.00.0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0.005	1900	300	560	650	1740	1030	79	13	23	27	73	45	338	56	66	116	310	184
0.010	2600	610	1020	1190	2480	1580	108	26	43	50	104	66	463	108	182	212	441	281
0.015	3160	920	1840	1690	3050	2132	132	39	77	71	128	89	562	164	327	300	542	379
0.020	3560	1250	2670	2260	3600	2668	148	52	112	95	152	112	635	222	475	402	640	475
0.030	4250	1910	3420	3220	4300	3420	177	80	131	135	180	141	758	340	610	572	765	609
0.040	4870	2480	3950	3830	4780	3982	203	104	166	161	200	167	865	440	703	680	850	708
0.050	5140	2860	4175	4440	5150	4353	214	120	175	186	216	182	915	510	742	790	915	774
0.060	5400	3180	4400	4880	5520	4676	225	134	185.	205	232	196	960	567	782	870	985	833
0.070	5600	3300	4630	5150	5750	4886	233	138	194	216	241	204	1000	587	825	918	1020	870
0.080	5745	3420	4800	5420	5860	5049	240	144	202	228	246	212	1020	610.	855	965	1040	898
0.090	5900	3540	4910	5640	6080	5214	245	148	206	237	254	218	1050	630	875	1000	1075	926
0.100	6030	3660	5010	5830	6350	5376	252	154	211	245	266	226	1070	652	892	1040	1125	956
0.125	6320	3950	5270	6320	6530	5678	264	166	221	266	275	238	1120	705	930	1120	1160	1007
0.150	6580	4210	5420	6645	6700	5911	274	177	228	279	281	248	1165	750	965	1180	1190	1050
0.175	6800	4470	5560	6970	6870	6134	284	188	234	292	288	257	1205	795	985	1235	1215	1087
0.200	7000	4740	5700	7000	7040	6296	291	199	239	294	296	264	1240	842	1010	1240	1250	1116
Ult.	7000	5060	5700	7290	7290	6468	291	213	239	305	305	271	1240	006	1010	1290	1290	1146

Table 31. Load Deflection Data for 3-11/16" x 4-1/2" Plates.

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Table 31. Load Deflection Data for 3-11/16" x 4-1/2" Plates.

	4	To	p Cho	rd For	e		Str	ess I	C n	ntac	t Ar	ea		tres	s In	Shea	r Lin	0
			<b>-</b>	.bs.					psi						٩	<u>li</u>		
Heel ]	4/1	12 Pit	:ch	6/1	2 Pitc	h:	4/1	2 Pit	ch	6/12	Pit	ch	4/12	Pit:	ch	6/1	2 Pit	ch
Def.	#67	#68	Ave.	1 #	8#	Ave.	<b>#67</b>	#68	Ave	# 7	# 8	Ave	#67	#68	Ave	#7	# 8	Ave .
0.000	0	0	0	0	0	ò	0	0	0	0	0	0	0	0	0	0	0	0
0.005	440	350	395	800	450	625	26	21	24	48	27	38	93	73	83	168	100	134
0.010	870	720	795	1820	1010	1415	52	44	48	110	61	85	182	150	166	383	224	304
0.015	1270	1020	1145	2350	1675	2015	77	62	70	142	100	121	266	214	240	495	372	434
0.020	1620	1300	1460	2650	2235	2445	98	79	88	158	134	146	340	272	306	554	497	577
0.030	2040	1680	1860	3350	2900	3125	123	102	112	201	174	188	424	351	390	705	644	674
0.040	2440	2070	2255	3730	3535	3435	147	125	136	224	213	219	510	435	474	785	786	786
0.050	2800	2370	2585	4070.	3920	3995	169	143	156	245	236	240	589	495	540	857	871	864
0.060	3160	2440	2800	4360	4030	4195	191	147	169	262	242	252	665	511	576	918	896	206
0.070	3230	2510	2870	4520	4140	4330	195	152	174	272	249	260	675	528	600	952	920	936
0.080	3300	2580	2940	4600	4250	4425	199	156	178	277	256	266	690	540	615	968	944	926
060.0	3370	2650	3010	4680	4360	4520	204	160	182	281	262	271	708	555	632	985	969	977
0.100	3440	2720	3080	4810	4470	4640	208	164	186	289	269	279	720	570	650	1012	993	1003
0.125	3620	2910	3270	5020	4700	4800	218	176	196	302	283	293	760	610	685	1057	1044	1050
0.150	3800	3100	3450	5140	4885	5010	229	187	208	309	294	301	796	650	723	1082	1086	1084
0.175	3800	3210	3505	5200*	4890*	5040	229	194	212	313	294	304	796	675	735	1095	1087	1091
0.200	3800	3310	3555	5250*	4900*	5075	229	200	215	316	295	306	796	695	745	1105	1089	1097
		- 		1			(		1				1	1	   			(
Ult.	3800	3470	36351	15360	4920	5140	229	209	219	323	296	309	796	730	763	1110	1093	1102

\*Estimated values; gage removed to prevent damage.

#7 - parallel to bottom chord in 6/12 - 8'0" specimen. #67 - #68 parallel to bottom chord in 4/12 - 8'0" specimen. #8 - parallel to bottom crack in 6/12 - 8'0" specimen.

		L to Crack
		5-5/16" x 6-3/4" .
		ection Data for '
		le 32. Load Defi
		Table

Load Deflection Data for 5-5/16" x 6-3/4" L to Crack Table 32.

| Ave.  | 0  | 195   | 315   | 416   | 497  | 610  
  | 690  | 744   
  | 194   | 835  
  | 864   | 882   | 906  | 946   
  | 965   | 985  | 1001  
  | 1076  |
|-------|--|---|---|---|--
--
---|--|--|---
---
---	---	--
--	---	
#74	0	239
  | 759  | 800   
  | 840   | 880  
  | 898   | 905   | 910  | 930   
  | 950   | 970  | 066   
  |   |
| #73   | 0  | 173   | 296   | 389   | 471  | 604  
  | 695  | 768   
  | 820   | 872  
  | 910   | 935   | 965  | 1025  
  | 1040  | 1055   | 1060  
  | 1065  |
| #72   | 0  | 238   | 380   | 480   | ·560   | 673  
  | 758  | 810   
  | 865   | 910  
  | 950   | 980   | 1020   | 1060  
  | 1080  | 1115   | 1135  
  | 0011  |
| #24   | 0  | 148   | 240   | 334   | 412  | 492  
  | 550  | 600   
  | 650   | 680  
  | 700   | 710.  | 730  | 780   
  | 790   | 800  | 820   
  |   |
| Ave   | 0  | 31  | 50  | 69  | 79   | 97   
  | 109  | 118   
  | 126   | 132  
  | 137   | 140   | 143  | 150   
  | 153   | 156  | 159   
  | 271   |
| #74   | 0  | 35  | 53  | 69  | 81   | 100  
  | 112  | 118   
  | 125   | 130  
  | 133   | 134   | 135  | 138   
  | 141   | 144  | 146   
  |   |
| #73   | 0  | 26  | 44  | 58  | 70   | 89   
  | 103  | 114   
  | 122   | 130  
  | 135   | 138   | 142  | 152   
  | 155   | 157  | 158   
  | 1 50  |
| #72   | 0  | 35  | 56  | 71  | 83   | 100  
  | 112  | 120   
  | 128   | 134  
  | 140   | 146   | 152  | 157   
  | 161   | 166  | 169   
  | 176   |
| #24   | 0  | 29  | 47  | 66  | 81   | 97   
  | 108  | 118   
  | 128   | 134  
  | 138   | 140   | 144  | 153   
  | 155   | 158  | 161   
  | 166   |
| Ave.  | 0  | 1125  | 1805  | 2362  | 2832   | 3467   
  | 3915   | 4234  
  | 4515  | 4750   
  | 4900  | 5025  | 5150   | 5397  
  | 5502  | 5602   | 5700  
  | EOAE  |
| #74   | 0  | 1270  | 1910  | 2460  | 2900   | 3580   
  | 4030   | 4250  
  | 4460  | 4680   
  | 4770  | 4810  | 4850   | 4950  
  | 5050  | 5150   | 5250  
  | 200   |
| #73   | 0  | 920   | 1580  | 2070  | 2510   | 3210   
  | 3700   | 4090  
  | 4370  | 4650   
  | 4840  | 4980  | 5120   | 5470  
  | 5570  | 5620   | 5670  
  | E 700   |
| #72   | 0  | 1260  | 2020  | 2550  | 2990   | 3580   
  | 4030   | 4320  
  | 4600  | 4840   
  | 5040  | 5230  | 5430   | 5650  
  | 5790  | 5940   | 6080  
  | 6270  |
| #24   | 0  | 1050  | 1710  | 2370  | 2930   | 3500   
  | 3900   | 4275  
  | 4630  | 4830   
  | 4950  | 5080  | 5200   | 5520  
  | 5600  | 5700   | 5800  
  | 000   |
| Defl. | 0.000  | 0.005   | 0.010   | 0.015   | 0.020  | 0.030  
  | 0.040  | 0.050   
  | 0.060   | 0.070  
  | 0.080   | 0.090   | 0.100  | 0.125   
  | 0.150   | 0.175  | 0.200   
  | + [ 1]  |
|       | Def1. #24 #72 #73 #74 Ave. #24 #72 #73 #74 Ave #24 #76 #74 Ave #24 #72 #73 #74 Ave | Def1.       #24       #72       #74       Ave.       #24       #72       #73       #74       Ave.         0.000       0 | Defl.       #24       #72       #74       Ave.       #72       #73       #72       #73       #72       #73       #74       Ave.         0.000       0 | Defl.       #24       #72       #72       #73       #74       Ave.       #72       #73       #72       #73       #74       Ave.         0.000       0 | Def1.       #24       #72       #74       Ave.       #72       #74       Ave.       #72       #74       Ave.         0.000       0 | Def1.       #24       #72       #74       Ave.       #72       #73       #74       Ave.         0.000       0 <t< td=""><td>Def1.         #24         #72         #74         Ave.         #72         #73         #74         Ave.           0.000         0&lt;</td><td>Def1.         #24         #72         #74         Ave.         #72         #73         #74         Ave.           0.000         0&lt;</td><td>Def1.         #24         #72         #73         #74         Ave.         #72         #73         #74         Ave.           0.000         0</td><td>Def1.         #24         #72         #73         #74         Ave.         #24         #72         #73         #74         Ave.           0.000         <t< td=""><td>Defl.         #72         #73         #74         Ave.         #24         #72         #73         #74         Ave.           0.000         0        
0         0</td><td>Def1.         #24         #72         #73         #74         Ave.         #24         #72         #73         #74         Ave.           0.000         &lt;</td><td>Def1.         #72         #72         #73         #74         Ave         #24         #72         #73         #74         Ave           0.000         <td< td=""><td>Def1.         #24         #72         #73         #74         Ave         #24         #72         #73         #74         Ave           0.000         <td< td=""><td>Def1.         #24         #72         #73         #74         Ave         #24         #72         #73         #74         Ave           0.000         0</td><td>Def1.         #24         #72         #74         Ave.         #24         #72         #73         #74         Ave.         #74         Ave.         #74         Ave.         #74         Ave.         #74         #72         #73         #74         F         <th< td=""><td>Def1.         #24         #72         #73         #74         Ave.         #24         #72         #73         #74         Ave.           0.0000         &lt;</td><td>Def1.         # 72         # 72         # 72         # 72         # 72         # 73         # 74         Ave.         # 72         # 73         # 74         Ave.         0</td></th<></td></td<></td></td<></td></t<></td></t<> | Def1.         #24         #72         #74         Ave.         #72         #73         #74         Ave.           0.000         0< | Def1.         #24         #72         #74         Ave.         #72         #73         #74         Ave.           0.000         0       
 0         0         0         0         0         0         0         0< | Def1.         #24         #72         #73         #74         Ave.         #72         #73         #74         Ave.           0.000         0 | Def1.         #24         #72         #73         #74         Ave.         #24         #72         #73         #74         Ave.           0.000         0 <t< td=""><td>Defl.         #72         #73         #74         Ave.         #24         #72         #73         #74         Ave.           0.000         0</td><td>Def1.         #24         #72         #73         #74         Ave.         #24         #72         #73         #74         Ave.           0.000         &lt;</td><td>Def1.         #72         #72         #73         #74         Ave         #24         #72         #73         #74         Ave           0.000         <td< td=""><td>Def1.         #24         #72         #73         #74         Ave         #24         #72         #73         #74         Ave           0.000         <td< td=""><td>Def1.         #24         #72         #73         #74         Ave         #24         #72         #73         #74         Ave           0.000         0</td><td>Def1.         #24         #72         #74         Ave.         #24         #72         #73         #74         Ave.         #74         Ave.         #74         Ave.         #74         Ave.         #74         #72         #73         #74         F         <th< td=""><td>Def1.         #24         #72         #73         #74         Ave.         #24         #72         #73         #74         Ave.           0.0000         &lt;</td><td>Def1.         # 72         # 72         # 72         # 72         # 72         # 73         # 74         Ave.         # 72         # 73         # 74         Ave.         0         0         0       
 0         0</td></th<></td></td<></td></td<></td></t<> | Defl.         #72         #73         #74         Ave.         #24         #72         #73         #74         Ave.           0.000         0 | Def1.         #24         #72         #73         #74         Ave.         #24         #72         #73         #74         Ave.           0.000         < | Def1.         #72         #72         #73         #74         Ave         #24         #72         #73         #74         Ave           0.000         0 <td< td=""><td>Def1.         #24         #72         #73         #74         Ave         #24         #72         #73         #74         Ave           0.000         <td< td=""><td>Def1.         #24         #72         #73         #74         Ave         #24         #72         #73         #74         Ave           0.000         0</td><td>Def1.         #24         #72         #74         Ave.         #24         #72         #73         #74         Ave.         #74         Ave.         #74         Ave.         #74         Ave.         #74         #72         #73         #74         F         <th< td=""><td>Def1.         #24         #72         #73         #74         Ave.         #24         #72         #73         #74         Ave.           0.0000         &lt;</td><td>Def1.         # 72         # 72         # 72         # 72         # 72         # 73         # 74         Ave.         # 72         # 73         # 74         Ave.         0</td></th<></td></td<></td></td<> | Def1.         #24         #72         #73         #74         Ave         #24         #72         #73         #74         Ave           0.000         0   
     0         0 <td< td=""><td>Def1.         #24         #72         #73         #74         Ave         #24         #72         #73         #74         Ave           0.000         0</td><td>Def1.         #24         #72         #74         Ave.         #24         #72         #73         #74         Ave.         #74         Ave.         #74         Ave.         #74         Ave.         #74         #72         #73         #74         F         <th< td=""><td>Def1.         #24         #72         #73         #74         Ave.         #24         #72         #73         #74         Ave.           0.0000         &lt;</td><td>Def1.         # 72         # 72         # 72         # 72         # 72         # 73         # 74         Ave.         # 72         # 73         # 74         Ave.         0</td></th<></td></td<> | Def1.         #24         #72         #73         #74         Ave         #24         #72         #73         #74         Ave           0.000         0 | Def1.         #24         #72         #74         Ave.         #24         #72         #73         #74         Ave.         #74         Ave.         #74         Ave.         #74         Ave.         #74         #72         #73         #74         F <th< td=""><td>Def1.         #24         #72         #73         #74         Ave.         #24         #72         #73         #74         Ave.           0.0000         &lt;</td><td>Def1.         # 72         # 72         # 72         # 72         # 72         # 73         # 74         Ave.         # 72         # 73         # 74         Ave.         0</td></th<> | Def1.         #24         #72         #73         #74         Ave.         #24         #72         #73         #74         Ave.           0.0000         0
        0         < | Def1.         # 72         # 72         # 72         # 72         # 72         # 73         # 74         Ave.         # 72         # 73         # 74         Ave.         0 |

Ting Stress Tahle 33. Load Deflection Data tor 8' vs. 24' - 3"x5" - Doug. Fir.

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Table

		Tol	cho:	rd For	eo.		ŭ	ontac	t Ar	ea S ;	tres	s		Shea	ir Li	ne S	tres	s
Heel	- 0	Specin	nen	24	Tru	ss	- 00	beci	men	241	Tru	SS	- 8	Speci	men	241	Tru	ss
Def1.	#38	#39	Ave.	#44	#45	Ave.	#38	#39	Ave	#44	#45	Ave	#38	#39	Ave	#44	#45	Ave
0.000	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0.005	330	200	265	420	465	440	22	13	18	28	31	29	63	38	50	80	83	84
0.010	660	400	530	835	1370	1100	44	27	35	56	16	73	125	76	100	158	260	207
0.015	940	600	770	1530	1910	1720	63	40	51	102	127	115	178	114	146	290	362	326
0.020	1230	1062	1010	2230	2340	2285	82	53	67	148	156	152	233	150	192	423	444	434
0.030	1820	1855	1840	2890	3020	2955	118	120	119	193	201	197	336	531	339	549	573	560
0.040	2230	2460	2345	3550	3420	3485	148	164	156	236	228	232	423	410	445	673	649	661
0.050	2550	2930	2740	4200	3820	4010	170	195	183	280	254	267	484	556	520	800	725	760
0.060	2790	3270	3030	4290	4230	4260	186	218	202	286	282	284	529	620	575	815	804	810
0.070	3040	3480	3260	4380	4510	4445	203	232	217	292	301	296	577	660	619	831	855	840
0.080	3220	3690	3455	4470	4700	4585	215	246	230	298	313	305	611	700	656	846	881	860
0.090	3340	3930	3635	4560	4860	4710	222	262	242	304	324	314	634	746	690	865	922	885
0.100	3480	4160	3820	4660	5030	4845	232	278	255	310	335	322	660	789	725	884	955	919
0.125	3480*	4520	4000	-	:			302	267	:		11	11	858	759	11		:
0.150	3480*	4740	4110	-	:	-	-	316	274	Ξ			-	899	780	11	:	=
0.175				-	:	:				:		••				11	-	=
														Ē				
Ult.	3480	5530	4505	4660	5030	4845	232	368	301	310	335	322	660	1049	855	884	955	919

Gauge removed to prevent damage. \*Deflection estimated.

## Table 34.

Load Deflection Data for 8' vs. 24' - 3"x8" - Doug. Fir.

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- 3"x8" - Doug. Fir. Load Deflection Data for 8' vs. 24' Table 34.

			9	Б	0	8	ഹ	2	9	4	4	0	-1	0	0	S	S	0	0	] a
	1S S	Ave	Ñ	14	21	24	34	40	49	5	63	68	73	77	85	06	95	101	117	, du
SSS	' Tru	#46	41	154	216	250	245	420	476	550	626	671	722	765	846	918	980	1040	1250	ding
Stre	24	#46	70	132	205	246	344	393	515	558	640	690	739	776	853	892	930	970	060	n rea
Line pli	en	ve	58	37	42	48	91	22	16	45	83	15	43	66	75	83			96	ctio
ear	ecim	41 A	52	12 1	0512	94 3	24 4	58 6	09 60	557	787	00 8	22 8	43 8	55 8	67 8			878	efle
Sh	' Sp	40#	65	62 1	7912	02 2	58 4	86 5	73 6	35 6	89 6	29 7	65 7	88 7	94 7	00 7			05 7	hed
	8	#			12	4	S	0	7	80	<b>∞</b>	6	6	6	6	10			<b>D</b>	t t
SS	uss	Аvе	20	<b>S1</b>	75	88	129	142	176	197	224	241	259	279	301	320	338	356	422	ease
stre	Tri	#47	14	54	77	88	129	148	169	196	222	238	256	277	300	325	347	370	451	incr
rea S Si	24	#46	25	47	72	87	128	136	183	198	227	245	262	281	302	316	330	344	394	l ch
t Al ps	men	Ave	21	49	86	123	174	220	245	264	278	289	299	307	310	313			317	wh.
ntac	peci	#41	18	40	73	104	147	198	216	232	240	248	256	258	268	272			273	rely
CC	5 1 8	#40	23	57	99	143	194	243	274	296	315	329	342	343	352	354			349	seve
		Ave.	475	1215	1790	2150	3080	3410	4220	4735	5380	5790	6210	6690	7225	7695	8125	8555	0125	Very
	russ	6	46	10	40	20	06	60	50	20	20	10	40	40	00	00	30	60	100	lays
e	4 t T	# #	M	13	18	21	30	35	40	47	53	57	61	66	72	78	83	80	108	idew
Forc.	2	#46	600	1120	1740	2090	3070	3260	4390	4750	5440	5870	6280	6740	7250	7590	7920	8250*	9450*	ing s
Chord 1bs	en	Ave.	495	11.65	2055	2960	4090	5285	5875	6335	6660	6925	7170	7360	7435	7510			7615	buck1
Top	ecim	#41.	440	950	740	:500	5530	1740	5180	5570	5760	5950	5140	5320	5420	5520			5640	was
r.	s Sp		0	0	0 1	0 2	50 3	50 4	0 5	5 00	00	00	00* 6	0 * 0	20 <b>*</b> 6	0 <b>*</b> [ €			01	lord
	30	#	55	138	237	342	465	583	657	110	756	790	820	840	845	850			854	p ch
	eel	efl.	.005	.010	.015	.020	.030	.040	.050	.060	.070	.080	.090	.100	.125	.150	.175	.200	lt.	To
	H	Â	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	D	*

Ultimate The test joint did not fail despite this lateral buckling. 

Table 35. Load Deflection Data for 8' vs. 24' - 5"x5" - Doug. Fir.

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5"x5" - Doug. Fir. ı Table 35. Load Deflection Data for 8' vs. 24'

Heel         24'         Truss         8'         Test           Defl         #48         #49         Ave.         #57         #58         Ave.           000         0         0         0         0         0         0         0           005         712         635         675         396         1030         715           015         1785         1860         1825         1470         1980         1725           015         1785         1860         1825         792         1395         1093           015         1785         1860         1825         1470         1980         1725           010         1240         1070         1255         792         1395         1093           015         1785         1860         1825         1470         1980         1725           020         22870         2380         3820         4670         4560           030         2870         2870         3720         3540         3557           050         2880         3820         4670         4560         35670           070         49510         4450         4450			Tol	Cho1	rd Foi	rce		Stre	SS I	n Co	ntac	t Ar	ea		stres	s In	Shear	Line	
Def1         #48         #49         Ave.         #57         #58         Ave.           000         0	Heel	24	I Tri	155		8' Tes	t	241	Tru	SS	8	Tes	÷	5	I' Tri	ISS	8	' Tes	t
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	Defl	#48	#49	Ave.	#57	#58	Ave.	#48	#49	Ave	#57	#58	Ave	#48	#49	Ave.	#57	#58	Ave.
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	.000	0	0	0	0	,0	0	0	0	0	0	0	0	0	0	0	0	0	0
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	.005	712	635	675	396	1030	715	28	26	27	15	41	28	135	120	128	75	194	135
.015       1785       1860       1825       1470       1980       1725         .020       2280       2240       2070       2610       2340         .030       2870       2928       3160       3320       3240         .040       3540       3620       3820       4070       3950         .050       4020       4210       4115       4450       4670       3550         .050       4020       4210       4115       4450       4670       3550         .070       4960       4990       5420       5155       570         .070       4960       4990       4850       5420       5950         .070       4960       4990       5740       6510       6125         .070       4950       5790       5735       5580       6290       59235         .090       5590       5790       5690       5740       6510       6125         .125       6510       6430       6556       5850       6700       6290         .125       6510       6570       5850       6700       6690         .125       6510       6570       5920       5935 <td>.010</td> <td>1240</td> <td>1070</td> <td>1255</td> <td>792</td> <td>1395</td> <td>1093</td> <td>50</td> <td>43</td> <td>47</td> <td>32</td> <td>56</td> <td>44</td> <td>236</td> <td>198</td> <td>217</td> <td>150</td> <td>264</td> <td>207</td>	.010	1240	1070	1255	792	1395	1093	50	43	47	32	56	44	236	198	217	150	264	207
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	.015	1785	1860	1825	1470	1980	1725	72	75	74	59	79	69	338	352	345	279	376	326
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	.020	2200	2280	2240	2070	2610	2340	88	16	06	83	104	94	418	432	425	392	495	443
.040       3540       3620       3580       3820       4070       3950         .050       4020       4210       4115       4450       4560       4560         .050       4510       4640       4575       4990       5420       5155         .070       4960       4990       4850       5420       5155         .070       4960       4990       5420       5155         .080       5280       5315       5380       5920       5670         .090       5590       5790       5690       5740       6510       6125         .100       5850       6070       5960       5850       6700       6275         .125       6310       6430       6565       6350       7180       6690         .150       6460       6670       6565       6350       7160       6980         .175       6650       6990       6580       7750       7165	.030	2870	2920	2895	3160	3320	3240	115	117	116	126	134	130	544	555	550	600	630	615
.050       4020       4210       4115       4450       4575       4990       5420       5155         .060       4510       4640       4575       4990       5420       5155         .070       4960       4990       4850       5420       5920       5670         .080       5280       5315       5580       5920       5670       5935         .090       5590       5790       5690       5740       6510       6125         .125       6310       6430       6565       6350       7180       6690         .150       6460       6670       6565       6350       7750       7165         .175       6650       6910       6780       6500       7750       7165	.040	3540	3620	3580	3820	4070	3950	142	145	143	153	163	158	672	688	680	724	770	750
.060       4510       4640       4575       4990       5420       5155         .070       4960       4990       5420       5670       5670         .080       5280       5350       5315       5580       5920       5670         .090       5590       5790       5690       5740       6510       6125         .125       6310       6430       5365       6370       6200       7180       6690         .125       6310       6430       6565       6350       7180       6690         .150       6460       6670       6565       6350       7750       7165         .175       6650       6910       6780       6500       7750       7165	.050	4020	4210	4115	4450	4670	4560	161	169	165	178	186	182	762	798	780	842	886	864
.070       4960       4990       4850       5420       5920       5670         .080       5280       5350       5315       5580       6290       5935         .090       5590       5790       5690       5740       6510       6125         .100       5850       6070       5960       5850       6700       6275         .125       6310       6430       6565       6370       6200       7180       6690         .150       6460       6670       6565       6350       7100       5960       7180       6690         .155       6650       6910       6780       6550       71165       7165	.060	4510	4640	4575	4990	5420	5155	180	186	183	200	218	209	855	878	867	940	1030	386
.080       5280       5355       5315       5580       6290       5935         .090       5590       5790       5690       5740       6510       6125         .100       5850       6070       5960       5850       6700       6275         .125       6310       6430       6370       6200       7180       6690         .150       6460       6670       6565       6350       7160       6980         .175       6650       6910       6780       6500       7160       6980	.070	4960	4990	4850	5420	5920	5670	198	199	198	218	236	227	940	948	944	1030	1120	1075
.090 5590 5790 5690 5740 6510 6125 .100 5850 6070 5960 5850 6700 6275 .125 6310 6430 6370 6200 7180 6690 .150 6460 6670 6565 6350 7610 6980 .175 6650 6910 6780 6500 7750 7125 .200 6820 7160 6990 6580 7750 7165	.080	5280	5350	5315	5580	6290	5935	211	213	212	222	252	237	1000	1015	1008	1060	1190	1125
.100         5850         6070         5960         5850         6700         6275           .125         6310         6430         6370         6200         7180         6690           .150         64460         6670         6565         6350         7610         6980           .175         6650         6910         6780         6500         7750         7155           .200         6820         7160         6990         6580         7750         7165	060.	5590	5790	5690	5740	6510	6125	223	232	228	229	261	244	1060	1095	1080	1090	1240	1165
.125 6310 6430 6370 6200 7180 6690 .150 6460 6670 6565 6350 7610 6980 .175 6650 6910 6780 6500 7750 7125 .200 6820 7160 6990 6580 7750 7165	.100	5850	6070	5960	5850	6700	6275	235	243	239	234	268	251	1110	1150	1130	1108	1270	1190
.150 6460 6670 6565 6350 7610 6980 .175 6650 6910 6780 6500 7750 7125 .200 6820 7160 6990 6580 7750 7165	.125	6310	6430	6370	6200	7180	6690	252	257	255	247	287	267	1195	1215	1205	1175	1360	1268
.175 6650 6910 6780 6500 7750 7125 200 6820 7160 6990 6580 7750 7165	.150	6460	6670	6565	6350	7610	6980	259	267	263	254	305	279	1228	1268	1248	1205	1440	1322
	.175	6650	6910	6780	6500	7750	7125	266	276	271	261	310	286	1265	1305	1285	1235	1470	1350
	.200	6820	7160	0669	6580	7750	7165	272	287	280	264	310	287	1295	1345	1320	1243	1470	1358
111 + 6820 7700 7260 6580 7750 7165	+ [1]	6870	7700	7260	6580	7750	7165	626	308	200	264	1015	787	1 205	1460	1 7 7 5	1243	1470	1358

Load Deflection Data for 8' vs. 24' - 3"x5" - White Fir. Table 36.

	ISS	Ave	0	119	160	189	166	271	314	353	408	455	478	500	531	565	598	629	660		660
res	Tru	<b>09</b> #	0	138	173	208	242	300	337	372	405	435	456	474	502	546	585	622	660	1	660
le St	74	6S #	0	66	146	169	161	243	286	337	410	475	500	526	560	584	611	635	660		660
r Lir	men	Ave	0	151	236	288	324	381	436	466	494	512	532	545	555	600	622	650	660		660
hear	peci	#52	0	165	210	256	310	390	464	492	525	555	586	605	618	670	685	720	720		7 20
0)	- 80	#51	0	138	262	319	339	372	408	443	461	470	478	483	493	530	560	580	600 <sup>.</sup>		600
ss	ISS	Ave	0	42	56	67	76	97	110	125	144	161	168	177	187	199	210	222	233	1	233
Stre	Tri	<b>#</b> 60	0	48	61	74	85	107	119	131	143	154	161	168	177	192	206	220	233		233
rea	24	<b>65</b> #	0	35	51	60	67	86	100	118	145	168	175	186	198	206	215	224	233	1	233
t Al	men	Ave	0	53	84	96	114	135	153	164	173	180	188	192	196	212	219	229	232	0	232
ontac	peci	#52	0	58	74	90	108	138	163	173	184	195	207	213	218	236	241	253	254	1	254
ŭ	- 8	#51	0	48	93	113	119	131	144	156	162	165	169	170	174	187	197	204	211	1	211
	S	Ave.	0	625	842	995	1140	1430	1640	1865	2150	2400	2525	2640	2800	2980	3155	3320	3475	1	3475
ce	Trus	#60	0	730	915	1100	1280	1580	1780	1960	2130	2295	2410	2500	2640	2880	3090	3280	3475	1	3475
d For s	241	# 29	0	520	770	890	1005	1280	1500	1770	2165	2510	2640	2780	2960	3080	3220	3360	3480		3480
Chor 1b	len	Ave.	0	800	1245	1520	1710	2010	2300	2470	2605	2695	2810	2870	2930	3165	3280	3425	3480	( ( , ,	3480
Top	pecim	#52	0	870	1100	1350	1630	2060	2450	2600	2770	2920	3090	3190	3260	3530	3610	3790	3800		3800
	815	#51	0	725	1390	1685	1790	1960	2150	2340	2440	2470	2525	2550	2600	2800	2950	3060	3160	1	3160
	Hee1	Def1.	0.000	0.005	0.010	0.015	0.020	0.030	0.040	0.050	0.060	0.070	0.0.80	060.0	0.100	0.125	0.150	0.175	0.200		Ult.

Immediately backed off, but affected \*Overload from 560 lbs. to about 250 lbs. readings.

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Load Deflection Data for 8' vs. 24' - 3"x8" - White Fir. Table 37.

T					5	0	2	-	-	~	7	8	2	10	-	00		5	5	-	
	10	1 <b>S</b> S	Å٧٤		96	6	127	59T	230	282	31;	348	38,	415	440	458	48,	500	528	554	
	ress	Tru	#62	0	84	120	148	202	270	325	374	394	430	462	492	505	546	566	591	623	202
	i i	24'	#61	0	48	75	106	135	191	238	260	302	344	368	387	409	428	446	465	485	105
	Lin pl	men	Ave	0	62	115	163	216	310	374	416	464	488	519	549	570	597	620	631	639	0 4 7
	hear	peci	#54	0	52	103	149	203	296	361	412	460	485	519	549	566	608	642	650	656	212
	S	8 I S	#53	0	72	128	178	229	324	387	421	467	490	519	549	573	586	599	612	623 ·	203
	S	SS	Ave	0	22	34	45	59	82	66	112	122	136	146	153	161	172	178	185	193	201
	tres	Tru	#62	0	29	42	53	11	97	114	131	138	151	163	171	178	192	200	208	216	216
	ea S i	241	#61	0	16	27	37	- 47	68	83	92	106	121	130	136	144	151	157	163	170	-021
·	t Ar ps	men	Ave	0	22	41	58	76	109	132	147	163	171	182	189	201	210	218	222	225	) ) L
	ntac	peci	#54	0	18	36	52	111	104	127	145	162	171	181	189	200	214	226	228	230	120
	ပိ	81 S	#53	0	25	45	63	81	114	136	148	164	172	182	189	202	206	210	215	219	010
			•	0	7	8	5	0	0	0	Ś	5	0	S	S	5	5	2	0	Ň	U
		ISS	Ave		5.5	82	107	142	195	237	264	293	326	350	371	385	410	423	446	464	
	e	' Tri	#62	0	712	1020	1250	1700	2240	2740	3100	3320	3620	3900	4160	4260	4600	4800	4990	5190	
	For.	24	#61	0	402	635	900	140	610	000	190	550	006	110	270	450	610	770	920	100	
	b'rd b's		_		~		_	5 11	<u>–</u>	0	0 2	0 12	2	3	3	) 3	)   3	3	5 3	4	
	Cho	Imen	Ave.		52;	97	1380	182	261	316(	352(	392(	411	438(	465(	5010	504(	524	532	540(	E 1 2 1
	Tol	Speci	#54	0	440	870	1260	1715	2500	3050	3480	3880	4100	4380	4650	4790	5140	5430	5490	5540	001
		• 8	#53	0	605	080	500	935	730	270	560	950	130	380	650	840	950	090	160	260	760
			Ļ		10		1		0 2	) 3	)   3	)   3	)   4	0 4	) 4	0 4	5 4	5	5	5	L
			•	<u>ں</u>		<u> </u>		L S	5	2	20	5	2	2	S	2	5	3	2	ž	
		<b>fee1</b>	Def1		0.00	0.01	10.01	20.02	0.03	0.04	0.0	0.00	0.01	0.0	0.00	0.1(	1.1	0.1	0.17	0.2(	+

Fir White ı. 21 5"X ı . 4 N ۷S ø for Deflection Data Load 38 Table

1115 1192 1192 2559 2559 578 578 578 670 731 804 850 904 942 954 Ð Av Truss #64 137 137 282 3283 3283 5594 652 7755 7755 800 800 877 911 950 985 S S 00 Stres - $\begin{array}{c} & 0 \\$ 80 24 #63 Φ  $\infty$ Lin 1040 p . Ave en Specime # 56 Av Shear E H 212 326 326 405 477 576 556 656 7796 881 881 905 881 905 11070 11070 ഗ 111 8000 S S 96 സത \* Ave 69 79 91 99 202 S Truss S Stres 20 29 29 20 20 20 200 200 200 200 200 213 #64 06 24 63 Area \* H ď 20 #56 Ave 220 Contact 45 45 69 69 69 101 122 101 122 101 1222 204 2217 2204 2217 2204 2226 236 Ś ഗ 204 പ ∞ \* 0 605 1005 1365 2490 2490 35300 35300 35300 35300 35300 35300 4480 4480 S S 96 502 Ð Truss AV 4 724 724 1280 1725 2020 2440 3440 3440 3680 3680 4090 4210 #64 4620 4800 5000 5190 5310 Ð Force 24 **484 730 730 1005 1280 1280 2180 2180 23140 33500 33500 33500 35500 4520 4520 4520** 40 63 47. \* Chord 1bs 780 1340 1750 2100 2585 2585 3565 3565 3740 3520 4115 4115 4580 4835 5085 5300 90 . Ave. men 540 Top Speci #56 1120 1720 2140 2520 3460 3460 3460 44200 44200 4450 4450 5100 5420 5650 5880 5880 0 440 955 1560 1675 2130 22520 22520 22520 3670 3270 3570 3570 3570 3570 4060 4250 4520 4720 00 S 5.5 51 \* 010 015 020 020 050 060 080 080 080 080 080 080 090 125 125 200 000 Heel Defl Ult. . ٠ . ٠ . <u>o o o o o o o o</u> 0000000000

Table 39. Load Deflection Data for 8' Small Jig - 3"x5" - Doug. Fir.

									į	ſ	į				ſ
	-	op cı	lbs.	orce		ront	act	Area psi		ess	She	ear l	ulne bli	Stre	ss
#78		6/#	#80	#81	Ave.	#78	#79	#80	#81	Ave	#78	#79	# 80	#81	Ave
		0	0	0	0	0	0	0	0	0	0	0	0	0	0
72	ഗ	1630	620	1120	1024	48	109	41	75	68	137	310	118	212	194
130	ഗ	2180	1070	1730	1571	87	145	71	115	105	248	414	203	328	298
180	0	2650	1420	2210	2020	120	177	95	147	135	342	503	270	420	383
223	20	3075	1740	2630	2419	149	205	116	175	161	423	584	330	500	458
29	20	3630	2290	3290	3040	197	242	153	219	203	560	690	435	625	578
33	60	3960	2720	3760	3450	224	264	181	250	230	637	751	516	714	655
36	50	4010	3120	4080	3715	244	268	208	272	248	693	761	592	774	705
39	40	4065	3320	4350	3919	263	271	222	290	261	748	771	630	825	743
40	00	4120	3500	4620	4060	266	274	234	308	271	760	781	664	876	770
40	60	4170	3685	4670	4146	271	278	246	311	276	770	791	700	886	785
41	20	4220	3870	4720	4232	274	282	258	314	282	781	800	735	895	804
41	60	4270	4020	4770	4300	278	286	268	317	287	790	810	763	905	816
42	90	4405	4095	4890	4420	286	294	273	326	295	814	836	775	929	840
44	20	4535	4170	5015	4535	295	302	278	334	302	840	860	161	951	860
45	50	4650	4255	5140	4649	304	310	284	342	310	862	882	809	975	880
46	20	4960	4340	5260	4800	310	331	289	350	320	881	941	824	998	910
				-				_							
46	50	4960	4340.	5260	4800	310	331	289	350	320	881	941	824	998	910

Table 40. Load Deflection Data for 24' Full Scale - 3"x5" - Doug. Fir.

Heel		rop Ch	lord F 1bs.	orce		Cont	act.	Area psi	str	ess	She	ar L	ine pli	Stre	SS
Def1.	#82	#83	#84	#85	Ave.	#82	#83	#84	#85	Ave	#82	#83	#84	#85	Ave
0.000	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0.005	525	400	560	400	470	35	27	37	27	32	95	72	101	72	84
0.010	880	1230	920	815	960	59	82	61	54	64	158	221	166	147	173
0.015	1235	1675	1285	1230	1360	83	112	86	83	90	222	301	231	220	244
0.020	1550	1875	1730	1530	1670	103	125	115	104	111	279	337	310	275	301
0.030	2050	2055	2240	2050	2000	137	137	149	137	140	370	371	404	370	378
0.040	2540	2235	2570	2550	2470	169	149	171	170	165	458	403	464	458	446
0.050	2900	2790	2790	2930	2855	194	186	186	196	190	521	502	502	528	512
0.060	3250	3160	3190	3170	3190	217	211	213	212	214	585	569	573	570	576
0.070	3460	3370	3630	3475	3485	231	225	242	232	233	624	609	654	627	629
0.080	3610	3470	3910	3620	3655	241	232	261	242	244	651·	625	705	652	659
0.090	3760	3570	4170	3910	3855	251	238	277	261	258	678	642	752	704	695
0.100	3910	3630	4430	4190	4050	261	242	296	279	272	704	654	798	753	729
0.125	4320	3830	4690	4450	4330	288	256	313	297	289	780	690	844	802	779
0.150	4470	4030	4760	4760	4505	298	269	318	318	301	805	725	860	860	815
0.175	4750	4230	4830	4935	4685	316	282	322	329	313	860	762	870	890	845
0.200	5030	4460	4910	5190	4900	335	298	328	346	326	910	805	888	932	881
+ [1]	E 0 2 0	U Y K D	0101	100		7 7 C	000	270	246	205		L C 0	000	620	100
• 1 T N	2020	00++		D T T C	「うつんす」	000	ר מ 7	070	040	270	מדר		0000	2 O V	1100

Fir Doug 3"x5" I Riehle ø for Data Deflection Load Table

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Table 42. Load Deflection Data for 8' Riehle - 3"x8" - Doug. Fir.

SS	Ave.	0	113	173	246	309	430	532	614	969	760	817	865	906	975	1023	1050	1065	1072
Stre	68 #	0	131	199	273	337	439	532	616	686	742	792	831	866	936	978	980	1000	1000
Line pli	#88	0	103	158	206	2.53	354	456	531	613	686	747	804	847	935	066	1029	1067	1089
shear	#87	0	125	187	261	324	461	560	644	737	804	860	006	935	066	1028	1055	1058	1060
[0]	<b>98</b> 6	0	94	149	244	324	462	580	664	747	809	869	925	974	1045	1095	1120	1140	1140
ress	Ave	0	40	61	87	109	150	186	214	245	268	288	304	320	345	362	367	376	378
a St	#89	0	46	70	96	118	154	186	216	242	262	278	292	306	331	345	346	353	5.5.5
Are	#88	0	36	56	73	89	124	160	186	216	245	263	283	298	330	350	360	376	384
act	#87	0	44	66	92	115	161	196	225	260	284	303	316	329	350	363	369	372	373
Cont	#86	0	33	53	66	115	161	203	232	263	285	306	326	342	370	386	392	401	401
	Ave.	0	957	1465	2080	2615	3631	4500	5190	5885	6427	6910	7316	7655	8265	8655	8870	9015	9067
orce	<b>68</b> #	0	1110	1680	2310	2840	3720	4500	5210	5800	6270	6700	7040	7330	7920	8270	8370	8470	8470
lord I lbs.	#88	0	870	1340	1740	2140	3000	3860	4490	5180	5800	6320	6800	7160	2000	8390	8700	9010	0200
rop Ch	#87	0	1060	1580	2210	2740	3900	4740	5450	6240	6800	7270	7600	7900	8390	8700	8930	8940	8960
L	#86	0	790	1260	2060	2740	3905	4900	5610	6320	6840	7350	7825	8232	8850	9260	9480	9640	0640
Heel	Def1.	0.000	0.005	0.010	0.015	0.020	0.030	0.040	0.050	090.0	0.070	0.080	060.0	0.100	0.125	0.150	0.175	0.200	111 +

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Load Deflection Data for 8' Riehle - 5"x5" - Doug. Fir. Table 43.

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Heel		Ch Ch	lps.	orce		Cont	act	Area psi	Sti	ress		shear	Line	Stres	S
Def1.	06#	16#	#92	#93	Ave.	06#	#91	#92	#93	Ave	06#	<b>16</b> #	#92	#93	Ave.
0.000	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0.005	950	840	1740	1110	1160	38	34	70	44	46	180	160	330	210	220
0.010	1420	1580	2,530	1740	1817	57	63	101	70	73	270	300	480	330	345
0.015	1900	2110	2840	2320	2292	76	84	114	93	92	360	400	540	440	435
0.020	2290	2610	3260	2770	2732	92	105	130	111	109	435	495	620	525	520
0.030	2980	3470	4010	3540	3500	119	139	161	142	140	565	660	765	670	665
0.040	3580	4060	4460	4160	4065	143	162	178	166	162	680	770	850	790	770
0.050	4080	4460	4760	4530	4457	163	178	190	181	178	775	850	905	860	845
0.060	4460	4830	5000	4855	4786	179	193	200	194	191	850	915	950	925	910
0.070	4740	5110	5170	5120	5035	190	204	207	205	201	006	970	980	970	960
0.080	4980	5350	5340	5330	5250	199	216	216	215	211	945	1010	1010	1040	1025
0.090	5200	5520	5420	5470	5402	208	221	217	219	216	966	1050	1030	1035	1025
0.100	5380	5690	5500	5590	5540	215	228	220	224	222	1020	1080	1045	1060	1050
0.125	5670	5885	5590	5850	5749	227	235	224	234	230	1075	1115	1060	1110	1090
0.150	5750	6080	5680	6000	5877	230	244	228	240	235	1090	1150	1080	1140	1115
0.175	5810	6110	5770	6015	5926	232	245	231	241	237	1110	1165	1090	1145	1125
0.200	5920	6140	5770	6030	5965	237	246	231	242	239	1125	11.70	1095	1150	1130
Ult.	5980	6140	5770	6030	5980	239	245	231	241	239	1135	1170	1095	1150	1135

Table 44. Load Deflection Data for 8' Riehle - 3"x5" - White Fir.

eel		Top Cł	lbs.	orce		Cont	tact	Area	Str	ess	She	ar I	ine pli	Stre	ss
f1.	#102	#103	#104	#105	Ave.	102	103	104	105	Ave	102	103	104	105	Ave
000	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
005	780	520	680	570	637	52	35	45	38	42	148	66	129	108	121
010	1140	830	950	820	935	76	55	63	55	62	216	157	180	156	178
.015	1390	1085	1150	1030	1164	93	72	76	68	77	264	206	218	196	221
020	1580	1300	1330	1220	1357	105	86	88	81	06	300	247	252	232	258
.030	1990	1680	1770	1550	1730	132	111	113	103	115	378	319	323	294	328
040	2260	2010	2020	1820	2022	150	133	134	121	134	430	382	384	346	384
050	2480	2270	2290	2050	2247	164	151	152	136	150	470	430	436	388	426
060	2620	2470	2530	2250	2467	174	164	168	150	164	498	469	480	427	468
070	2740	2560	2720	2440	2615	183	170	181	162	174	521	486	516	464	496
080	2840	2660	2930	2590	2755	189	177	195	173	184	540	505	556	492	523
060	2950	2840	3000	2640	2857	197	189	200	176	191	-560	540	570	502	542
100	3020	3040	3060	2680	2950	202	203	204	179	197	574	577	581	509	560
125	3160	3190	3300	3160	3202	210	212	220	210	214	600	605	626	600	610
150	3160*	3310	3300*	3340	3277	210	221	220	223	218	600	628	626	634	621
175	3160*	3310*	3300*	3420	3297	210	221	220	223	219	600	628	626	649	626
200	3160*	3310*	3300*	3420*	3297	210	221	220	223	219	600	628	626	649	626
t	3160	3310	3300	3420	3297	212	221	220	228	220	600	628	626	649	626

\*Plate did not deflect this far. Estimated readings.

Fir.
White
I
3"x8"
I
Riehle
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for
Data
Deflection
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Table

e l		Top C	hord F 1hs.	orce		Cont	act	Area nsi	l Str	ess.	She	arl	,ine nli	Stre	SS
1.	#94	#95	96#	#97	Ave.	#94	#95	#96	#97	Ave	#94	#95	#96	#97	Ave
000	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
05	842	1028	948	062	902	35	43	40	33	38	100	122	102	93	106
10	1344	1430	1474	1140	1347	43	60	61	48	56	159	169	174	135	159
15	1740	1706	2000	1450	1724	72	71	83	60	72	206	202	236	172	204
0.2.0	2086 <sup>.</sup>	2012	2452	1740	2072	87	84	102	72	86	247	238	290	206	245
030	2581	2573	3220	2320	2673	108	107	134	97	111	306	304	381	274	316
040	2844	3004	3918	2840	3151	118	125	163	118	131	336	360	463	336	373
020	3430	3400	4487	3280	3649	143	142	187	136	152	406	402	531	388	432
090	3850	3736	4980	3630	4049	160	155	208	151	168	455	442	590	429	478
010	4213	3952	5372	4000	4384	176	164	224	167	183	498	467	636	463	519
80	4550	4140	5658	4310	4664	189	172	236	180	195	538	490	670	510	553
060	4864	4424	5920	4590	4949	202	184	246	191	206	576	523	700	543	585
100	5124	4664	6180	4840	5202	214	194	258	202	217	606	553	731	572	616
125	5538	5167	6250*	5370	5581	222	215	260	224	232	655	612	740	635	999
L50	5690	5540	6325*	5430	5746	237	231	264	226	240	673	655	749	643	680
175	5730	5930	6400*	5490	5887	239	247	266	229	245	679	702	757	650	696
200	5760	6160	6490*	5540	5987	240	257	270	231	250	682	730	768	655	709
دى	5768	6500	6490	5540	6075	240	271	270	230	253	684	770	768	655	719

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\*Top chord of #96 buckled. These are estimated.

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Load Deflection Data for 8' Riehle - 5"x5" - White Fir. Table 46.

	Ton CF	1 proc			Lon t	+ 10	Ares	t s	220.	Ū	1	i no	+ + 0 0 0	
	n do t	lbs.	2010		11100	מרר	Alea psi	וזכו	622	ō	lear	ulne v pli	CLESS	
90	#107	#108	#109	Ave.	106	107	108	109	Ave	#106	#107	#108	#109	Ave.
0	0	0	0	0	0	0	0	0	0	0	0	0	0	
40	710	740	950	810	34	28	30	38	32	159	135	140	180	154
40	1110	1190	1340	1245	54	44	47	54	50	254	211	226	254	236
40	1420	1640	1710	1627	70	57	65	68	65	330	270	312	324	309
90	1740	1950	2030	1952	83	69	78	81	78	396	330	370	386	371
90	2310	2590	2650	2560	107	92	103	106	106	511	439	492	503	486
10	2760	3115	3160	3061	128	110	125	126	122	610	525	591	600	581
30	3125	3510	3630	3474	145	125	140	145	140	690	594	666	690	660
25	3480	3820	4000	3841	161	139	153	160	154	765	661	725	760	730
20	3950	4190	4240	4200	177	158	168	169	168	840	750	795	805	797
40	4320	4550	4420	4507	189	173	182	177	181	006	820	865	840	856
80	4580	4830	4740	4782	199	183	193	190	191	946	870	917	006	910
30	4840	5050	5060	5020	205	194	202	202	201	975	920	960	962	955
30	5220	5440	5530	5380	213	209	217	221	215	1012	166	1031	1050	1021
70	5420	5600	5920	5627	223	217	224	237	225	1058	1027	1062	1123	1069
30	5520	5830	6160	5810	227	218	229	244	230	1087	1049	1108	1170	1103
50	5610	5830	6400	5897	226	221	229	252	231	1001	1066	1108	1215	1118
			•						4 %ba					
750	5610	5850	6550	5940	230	225	234	262	243	1091	1066	1112	1243	1128

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Figure 60. Full-Scale Tooth Layout for 3"x5", 3"x8", and 5"x5" Plates.

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