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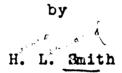


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THESIS

Design and Construction of a Small Single Phase Commutator Induction Motor.



Hichigan Agricultural College

Spring Term

THESIS

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INTRODUCTION

There is an increasing demand for small electric motors. Like large motor practice, there should be motors with characteristics, suited to the work they are to do.

The Shunt and Series Motors in D. C. will do about all that is required, but D. C. is not very extensively used on lighting circuits where the small motor is naturally connected.

Small A. C. motors are generally of the single phase induction type with squirrel cage motors and a split phase starting winding which is thrown out of service when full speed is reached, by a contrifugal device.

These motors run at only one speed and have a very small starting torque. Plain A. C. series motors are also used especially on vacuum cleaners. Such motors have a very bad power factor and small capacity for the iron used.

The writer made a number of tests on a small series motor and tried a compensating winding, but still the power factor was low and sparking bad.

Series characteristic is hardly what is wanted in a small motor, the shunt being greatly preferred. The writer's attention was next turned to the shunt induction motor for single phase.

These have a good starting torque and a wide speed variation, with a power factor near unity. The overload capacity is also higher than the plain induction motor. It is true that the efficiency is low, but this is not such an important item in a small motor for intermittant use.

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Therefore since the writer could find nothing concerning small motors of this type, it was thought worth while to experiment along this line.

THEORY

The theory of the single phase shunt commutator motor and the sommon single phase squirrel cage induction motor is exactly the same.

The shunt motor consists essentially of a status with a distributed single phase winding similar to the common induction motor and an armature and commutator similar to a D. C. machine. On the commutator are four brushes (speaking of a two pole machine for simplicity) one set parallel to the primary winding and the others at right angles. (See Fig. 1).

At stand still the motor is essentially a transfer under short circuit, stator winding primary and rotor winding secondary, shorted across y y.

Thus the stator current must supply flux enough to generate a counter E.M.F. equal to the impressed E.M.F. less the local stator impedance and balance the M.M.F. of the rotor current in the transformer axis.

The stator circuit is highly inductive thus the current I_0 the Magnitizing current will lag almost 90° behind the impressed E.M.F., E., I. causes the flux f_{e} which is nearly in phase with it.

 \oint_c generates an E.M.F. E_c in both the stator and rotor, laging 90°. The magnitude of these E.M.F.'s varies according to the ratio of transformation.

 E_{e} causes a current I_{e} to flow across axis y y, determined both in magnitude and phase by the local impedance of

x

the rotor. The primary current I, will then be the resultant of I, the magnetizing current, and I reversed, or the vectorial difference, (assuming 1 to 1 ratio of transformation). The impressed E. M. F. E, will be the resultant of a component equal and opposite to E_{z} and of a component i, z, to over come the local stator impedance and i, r, .

Now if the motor is brot up to speed, there will be in E.M.F. E'(Fig. 3) of line frequency along axis x x, due to the conductors cutting \oint_{e} . E_eis proportional to \oint_{e} and the speed and is either in time phase withor in time-phase opposition to flux $\oint_{\mathcal{L}}$ depending on the direction of rotation. Assuming it to be in time-phase with \langle . The rotor current I along the transformer axis sets up a leakage field gin phase with itself. A also generates an E.M.F. e'in the speed axis, it is in phase with Iz. Thus E is the vectorial sum of E and e. The conditions along the speed axis are those of a transformer on open circuit since the Counter E.M.F. allows only exciting current to flow. Thus E, causes a current I, laging heavily, this produces a flux ϕ_s nearly in quadrature with E_f. ϕ_s has line frequency and is along x x or right angles to ϕ mechanically. ϕ_s by it alternations induces an E.M.F., Esalong x x, 90° behind $\not d s$ in phase which brings it nearly in opposition to E. The vectorial difference between E, and E, is the E.M.F. required to drive I, thru the local impedance and resistance. The motion of the rotor conductors thru the speed field $\phi_{\rm g}$ generates an E.M.F. E'in the transformer axis, which is in time-phase opposition to $arphi_s$ and proportional to ϕ_s and the speed. Thus E's nearly in opposition to \mathcal{E}_{ϵ}

 E_{ϵ} . E_{s} is the counter E.M.F. of the motor. \oint_{J} also produces a leakage flux ϕ_{s} coarial with \oint_{S} and in phase e_{r}^{MTH} . This with the speed generates e'_{s} in the transformer axis in phase opposition to I_{s} . The vector sum of E_{ϵ} , E'_{s} and e'_{s} give E_{π} , which drives I_{ϵ} thru the local rotor impedance.

The limiting speed will be when the counter E.M.F. F'_{s} and E_{s} e'_{s} and E_{t} vectorily balance. E_{t} is constant while E'_{s} depends upon the speed. Now if an external E.M.F. in phase with E_{t} or opposition such as from line or taps from stator, is introduced across y y, E_{t} will be either increased or decreased and the speed will have to increase or decrease to keep up the balance. This method is used for speed variation and is used over wide ranges. See Fig. 4.

Again if the speed field can be increased or weakened, E'_s will be changed and the speed will have to change to again give equalibrium. This can be done by inserting a inductance or capacity along x x. A capacity increases I_s , thus \oint_s and E'_s and reduces speed; an inductance decreases I_s thus raises speed. (Fig. 5).

If I_s be made to pass thru stator coils along axis x which will either boost or buck \oint_3 , E'_s can be changed, thus the speed. (Fig. 6).

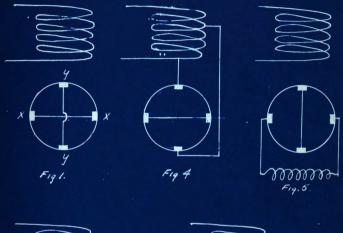
Power factor Compensation.

The power factor may be improved by introducing an E.M.F. from the line or stator in the speed axis. This E.M.F. E is in phase with I_s and ϕ_s approximately and at right angles with E_s and E_s . Thus we have three E.M.F's in speed axis. (Fog. 8) E_c causes I_c and ϕ_c nearly at right angles to it. ϕ_c generates E'_c

The Induction Motor--Bayley.

Laging 90° which is a counter E.M.F. to the E introduced. Thus along axis x x, we have two fluxes \oint_{a} and \oint_{c} 90° out of phase with each other, therefore they cannot react together to give torque and change the speed. The conductors cutting \oint_{c} generates another speed E.M.F. $E_{c}^{'}$ along the transformer axis in phase with the flux. $E_{c}^{''}$ being at right angles to the main speed E.M.F. $E_{s}^{'}$ in the y y axis, they combine to form a new resultant E.M.F. Taking the action of this E.M.F. $E_{c}^{''}$ causes $I_{c}^{'}$ in y y axis to flow laging heavily, thus causes flux $\oint_{c}^{'}$ on this exis 90° behind $E_{e}^{''}$. This flux generates $E_{c}^{'''}$ in both the rotor and the stator, which lags 90° behind $\oint_{c}^{'}$ or 90° behind the counter E.M.F. in the stator equal and opposite to E_{c} . Thus E, and $E_{c}^{'''}$ combined to give the stator resultant E.M.F. $\oint_{c}^{''}$, which can be made to either lead or lag behind the primary current I..

All of the theory connected with Fig. 3 holds for a squirrel cage rotor, the end rings at all times keep the rotor bars shorted across the respective axis, thus equavalent to commutator and shorted brushes.



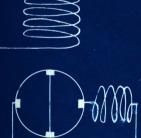
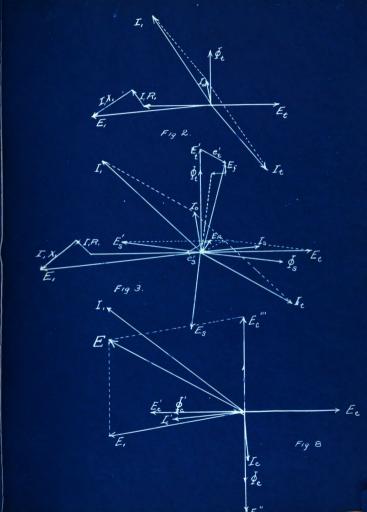




Fig 7.

Fig. 6



SPECIFICATIONS

Out put about <u>1</u> H. P. Voltage 110 60 cycles Single Phase Speed near 3600 R.P.M.

DESIGN

Armature

From small motor practice an armature about $2\frac{1}{4}$ " diam. and 2" long was selected. Standard punchings can be purchased 2 5/16" diam.12 round slots 3/8" diam.

Standard practice of motors of this size calls for a 5/16" shaft.

For mechanical detail, see drawing. Allowance was made for winding by examining armatures of similar size. Stator

The stator used is the same as that of any single phase induction motor of two poles.

The area of the air gap is the area of one-half the armature surface minus the slot area.

> $A = \frac{1}{2} (2x.5x12) = 6 \text{ sq. in.}$ Air gap density 22,500 lines per sq. in. (Standard Hand Book 13,000 lines to 26,000 lines) Thus 6 x 22500=135000 or total flux Number turnes wire

$$s = \frac{E \times 10^{\circ}}{2K, K, g_m} f$$

Where

E Line voltage

S number conductors in stator

K, Form factor

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A

K_z Distribution constant

 ϕ Maximum flux

f Frequency

K, for Sin wave 1.11

K_zfor 2/3 pole face distributors .9 (Fig. 52 Sheldon & Mason) $S = \frac{110 \times 100,000,000}{2 \times 1.11 \times .9 \times 135000 \times 60} = 630 \text{ turns}$

Considering 1/10 H.P. as 74 watts and 50% efficiency assumed, the imput should be 158 watts. Assuming Unity Power factor as this type of motor should give, the current would be 1.4 amps. With good ventilation, using 400 cir. mils. per amp. (Standard Hand Bock)

1.4 x 400 560 cir. mils. area
This is close toaa%22 wire, so use No. 22 wire.
With 8 slots, each slot must contain

 $\frac{630}{9} = 85 \text{ conductors}$ D.C.C. wire No. 22 will run 876 turns per sq. in. $\frac{85}{876} = .1 \text{ sq. in. approximately}$.1 sq. in corresponds to a 3/8" hole.

Allowing 1/16" for insulation of slot and extra room for winding, makes diameter of slot 7/16".

Round slots are used since they are easier to make and give greater air gap area thus greater capacity.

The inside diameter of stator is determined so as to give 1/32" air gap (Standard Hand Bock).

Outside diameter is determined by end room for coils and castings.

The punching are clamped by a 3/16" bolt. (See drawing for details.)

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Armature Winding

Designing the armature winding according to the transformer E.M.F. N_a actual number of conductors on the armature, the actual number turns is $\frac{N_s}{2}$. Since they are distributed around the armature, the E.M.F. in each cotl is equal to the Cos. of the angle of displacement from the position of Max. E.M.F. Thus the E.M.F. is the resultant as vectorial sum of E.M.F. around a circle.

 $\frac{N_e}{2}$ number turns in one-half the armature or from brush to brush, thus the effective turns would be $\frac{N}{2}$. Thus, $E_r = \frac{N_e}{\sqrt{2}} \frac{\phi}{10} e$

Assuming 40 volts for the transformer E.M.F. $N_{c} = \frac{E_{r} \sqrt{2} \ 10^{\circ}}{9} = \frac{40 \times 1.41 \times 100,000,000}{135,000 \times 60} = 700$ 700 Conductors on armature

 $\frac{700}{12} = 57.5$ conductors per slot use 60 conductors

3/8" round slots give an area of .ll sq. in. Allowing 1/32" for insulation gives a net area of about .l sq. in. Thus, 60 x .l 600 turns per sq. in. allowable

D.C.C. wire of this size is between No. 21 and No.22. Use No. 22 wire.

With 12 slots and 24 commutator segments, makes 4 coil per slot of 15 turns each.

(See winding diagram and drawings for details.)

This motor was built as designed, but did not operate at all satisfactorily. Sparking at the commutator was at all times very bad, in fact, the commutator was nearly destroyed. The

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exciting current was very large, being 2.4 amps. the imput on no load, 100 watts.

The synchroneous speed was 3600 R.P.M., but the speed was only 2400 R.P.M. The motor would carry a heavy load of about 1/10 H.P., but the current was excessive, running up to five amperes. Standard Squirrel Cage Induction Motor.

Using the same stator with four more slots to make 12 slots and with the same flux per pole 135000 lines. With 6 slots per pole with winding distributed over five slots.

$$E = 2.32 \times k_{1} \otimes \oint f 10^{-9}$$
where E line E. M. F.

$$S = \text{number conductors}$$

$$\oint = \text{flux per pole}$$

$$f = \text{freguency}$$

$$S = \frac{10^{9}}{2.22 \text{ M/f}} = \frac{110 \times 10000000}{3.22 \times .74 \times 130000 \times 30} = 330 \text{ turns}$$
Minimum tooth area of stator.
7idth of slot $\frac{1}{4}$ ", 6 slots per pole face
 $6 \times \frac{1}{4}$ " $\times 2 1/16 = 3.1 \text{ sq. in. area}$
Core area of stator depth $\frac{1}{2}$ " $\times 2.1/16$ "=1 eq. in.
Apparent gap area per pole of stator tooth $\frac{1}{2}$ "
 $6 \times \frac{1}{2} \times 2 1/16 = 6.2 \text{ sq. in area}$
Waximum core density. The stator flux divides half going
around each way.
 $\frac{135000}{2 \times 1} = 67,500 \text{ lines}$
Minimum tooth area per pole of rotor
11 conductors or $5\frac{1}{2}$ per pole face
 $5\frac{1}{2} \times \frac{1}{4}$ " $\times 2 1/16 = 2.35 \text{ sq. in.}$
Maximum tooth density of stator
 $\frac{17}{2} \times \frac{9}{10000} = 74,500$
Stator density $= \frac{135000}{3.1 \times 3} = 74,500$
Rotor density $= \frac{135000}{2.85 - 3} = 74,000$

830 turns in 12 slots gives

 $\frac{830}{10} = 83$ Condustors per slot or 83 turns per coil The slots will easily hold this amount of No. 82 wire. (See first Calulation)

Squirrel Cage Rotor.

Air gap clearance 1/64" External Diameter 2 9/32" Length 2 1/16" Number slots 11

In order for the rotor not to lock on starting the rotor slots must be prime to the stator slots.

Rotor current I per condutor at full load.

I for full load will be 1.6 amps. No. 22 wire has an area of 642 cir. mils at 400 cir. mils per amp.

 $\frac{643}{400} = 1.6 \text{ mps.} \text{ carrying capacity with good ventilation.}$ Rotor mps.=.35 I x total stator conductors I = .85 x 1.6 x $\frac{830}{11} = 103$ mps. Ampere conductors per inch $\frac{11 \times 103}{x 3.33} = 160$ X in mils per amp. allowable 500 (Standard Hand Book)

103 x 500 = 51500 Cir. Nils.

This area is close to No. 3 B&S wire .229" diameter or Drill slots 15/64" diameter.

Magnetizing current.

C,=the stator Carter coefficient $\frac{s}{\delta} = \frac{.125}{.02} = 5.1$ s = slot width = .125 $\delta = clearance = .02$

f = from Curve of Carter fringing constand page 44 Gray's Electrical Machine Design

$$f = .5$$

$$C_{r} = \frac{\lambda}{t + f_{S}}$$
slot pitch = .606

$$C_{r} = \frac{\lambda}{t + f_{S}}$$
slot pitch = .606

$$C_{r} = \frac{.606}{.437 \cdot .5 \times .125} = 1.21$$

$$C_{r} = for rotor = \frac{s}{6} = \frac{.062}{.02} = 3.1$$

$$f = .05$$

$$C_{r} = \frac{.64}{.625 \cdot .65 \times .06} = 1.02$$

Pole pitch = $2.64 = 7$ $L_{g} = Axel length of dirgap$
Magnetizing current $I_{0} = \frac{1}{.37 (Cond. per pole) T_{y}}$

$$L_{g} = \frac{1}{.37(6x80) - 3.64 \times 2}$$

Allow 20% for iron 1.2 x 1.1=1.3 amps. mag. current Constant Losses

> Weight of stator teeth in pounds Volume of stator teeth 5.4 sq. in. 1 cu. in. steel .274 # 5.4 x .274 = 1.47#

Loss in watts per 10. 7 watts (Fig. 31 pg.102 Gray's Machine Design)

1.47 x 7 = 10.3 watts loss in teeth

Volume of core 13 cu. in. 13 x .274 = 3.56# Watts per 1b. 7 3.56 x 7 = 25 watts loss in core Disregard rotor iron loss since the frequency is very low. Total doss 35 watts which remains constant on all loads Bearing loss = .81 x dl $\left(\frac{v}{100}\right)^{\frac{3}{2}}$ watts d = bearing diam. Where 1 = length of rubbing surface v = velocity of rubbing in feet per min. .81 x .31 x 1.25 $(3600 \times x .31)^{\frac{3}{2}} = 1.7$ watts For 2 bearings 3.4 was Assume 1 watt windage Total loss 40 watts. Maximum Current Slot Leakage(Page 330 Sheldon & Mason) Stator $\mathbf{I}_{,=}$ 2 f $\mathbf{I}_{,Nn}^{2}(.62 \underline{d})$ 10^{-7} (For round slots) $l_s = length of slot in inches$ Where

n = number conductors in series per slot

N = number slots per phase

d, = depth of saw cut

W. = width of saw cut in tooth

$$\mathbf{X}_{,=} \ 2 \ \mathbf{x} \ 60 \ \mathbf{x}^2 \ \mathbf{x} 12 \ \mathbf{x} 6400 (.625 .5) \ 10 = 2.7 \ \text{ohm} \mathbf{s}$$

Rotor

 $I = 2x10x2x11x1(.625 2) 10^{-7} =$

Comes out very small so disregard

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Zig Zag Leakage

Stator and Rotor

 $X_{z}=3.35 \text{ f } 1_{s} \text{ Nr}, \frac{\lambda}{4} \left(\frac{t}{\lambda}, \frac{t}{\lambda_{z}}, -1\right)^{2} 10^{-8}$ Where t, and t_{z} are stator and rotor tooth tip widths respectively λ , and λ_{z} are stator and rotor tooth pitches λ average or common tooth pitch 4 radial length of air gap in inches $X_{z}=3.35 \times 60 \times 2 \times 12 \times 6400 \cdot \frac{687(.5}{2(.68} + \frac{.68}{5} - 1)^{10} = 15 \text{ ohms}$

Resistance Primary

Length of conductors on stator

$$\frac{2(2.5 \quad 3.64) \times 833}{12} = 85 \text{ ft.}$$

$$\frac{2(2.5 \quad 3) \times 83}{12} = 76 \text{ ft.}$$

$$\frac{2(2.3 \quad 1.5) \times 83}{12} = 52 \text{ ft.}$$

$$\frac{2(2.3 \quad 1.5) \times 83}{12} = 52 \text{ ft.}$$

$$\text{Total} = 213 \text{ ft.}$$

$$\text{Resistance per foot of No. 22 wire is .0184 ohms}$$

$$213 \times .0184 = 3.9 \text{ ohms stator resistance}$$

$$\sqrt{3.9 + 2.85}^{2} = 4.9 \text{ ohms apparent resistance}$$

$$\text{Maximum current} = \frac{110}{4.9} = 32.4 \text{ anps.}$$

$$\frac{110}{295} = 28.6 \text{ amps.}$$
This value is used for diameter of the circle diagram.

22.4 is used to determine the locked position of the rotor in the circle diagram.

Exciting Current

 $\frac{40}{110} = .363 \text{ amps. in phase with E.M.F. or a power component}$ Copper loss I²R=1.3²x 3.9=4.9 watts $\frac{4.9}{110} = .406 \text{ amps. in phase with E.M.F. or OG in circle diagrag$

Total amps. in phase with E.M.F. =.769 Exciting current $\sqrt{.76^2+1.3^2}=/.5$ amps. or OI in Circle diagram Rated Load

> Maximum capacity of wire =1.6 amps. Magnetizing current =1.3 1.6 = $\sqrt{1.3^2 + x^2}$ x = .93 amps. .93 x 110 =103 watts power component 103 - 50 watts = 50 watts net power 50 = .067 H.P. or 1/15 H.P. 746 Efficiency 50 = 48.5%

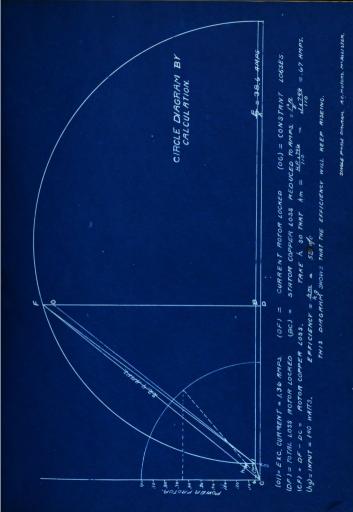
TABULATED DATA

	Stator	Botor
External Diameter	4. 5/16*	2 9/32*
Internal Diameter	2 5/16*	
Frame Length	2 1/16*	2 1/16"
Air ducts	none	none
Net iron	2 1/16*	2 1/16*
Slots number	12	11
Size	7/16• D	15/64"
Conductors for slot	8 3	1
Size	#32 D.C.C.	∄ 3
Winding type	two coil	squirrel cage
Kinimum slot pitch	.60 6 *	.64*
Kinimum tooth width	1. u	14 #
Core depth	.]. n 2	1
Pole ritch	3 .64	
Minimum tooth area per pole	3.1 sq. in.	2.35sq. in.
Core area	l sq. in.	2 sq. in.
Apparent gap area per pole	6.2	6 .2
Flux per pole	135000	135000
Maximum tooth density	69000	74300
Kaximum core density	67,500	67,500
Ampere conductors per inch	230	160
Circular mills per ampere	500	500
Apparent gap density	22500	
Air gap clearance	.03	.02
Carter Coefficient	• 5	.65
Magnetizing current air gap	1.1	
Total	1.3	
Reactance per phase	2.85 ohns	
Maximum line ourrent	22.4	

Rating	Stator 75 watts	Rotor
Horse Power	1/10	
Terninal voltage	110	
Amperes full load	1,9	
Phases	1	
Frequency	60	
Synchroneous R.P.N.	3600	
Poles	2	

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METHOD OF STARTING.

factor is needed

The Single Phase Motor will not start alone as there is no torque at standstill. For starting purposes a second winding was put on at right angles to the main winding, as in a two phase motor. This winding was of fine wire therefore of high resistance, thus the current was slightly in advance of the main current. This gives the polyphase effect. DESIGN. The coil is completely in one slot thus no distribution

> Conductors in main winding 830. Distribution factor .74 .74 x 830 = 615 conductors. or 307 turns. $\frac{77}{4}$ x $(7/16)^2$ = .15 sq. in. area of slot. $\frac{307}{.15}$ = 2050 turns per sq. in. This corresponds to a No. 26 S. C. C. wire.

It was found that the motor would not start with the full voltage on the main winding, so an inductance coil was put in series with it, to reduce the starting current and the locking effect. This also caused the main current to lag still more, giveing a greater difference in phase.

A 40% reduction in voltage was found to be satisfactory the motor would then run up to speed with only 2 amps starting current.

TEST DATA.

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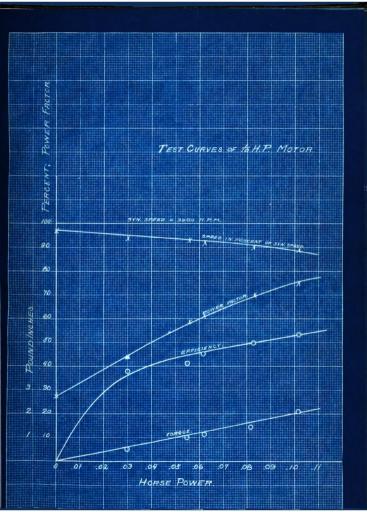
Xa//s	EI	Watts	Power Factor	Speed	Amps.	Load oz.	НР
114 113 107 110 107.5 104	154 168 161 170 183 203	44 69 95 103 12 6 153	.286 .438 .59 .605 .69 .75	3500 3400 3350 3350 3300 3200	1.35 1.4 1.5 1.55 1.7 1.95	0 12 22 25 34 46	0 .0303 .0555 .0625 .0835 .109
Eff.		Torque. In. 1ba		Speed. % Syn.	Speed		
0 30.8 41.5 45 49.5 53.2		0 .562 1.03 1.17 1.6 3.16		97.2 94.5 94.5 93.2 91.6 89			

Comparison of calculated data, and test data.

	By Calculation	Ву	Test.
Capacity	1/16 H P	1/10	ΗP
Exc. Current	1.5 amps.	1.35	amps.
Watts input no load	40 5 <i>2%</i>	44	
Efficiency at 1/10 H P		5 3%	
Power Factor at 1/10 H P	.65	.75 7,5 ch	,
Resistance of primary	3.9 ohma	7,5 ch	1/72 5
Reactance	2.85 ohms.		

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APPENDIX.

Shunt Motor Drawings.

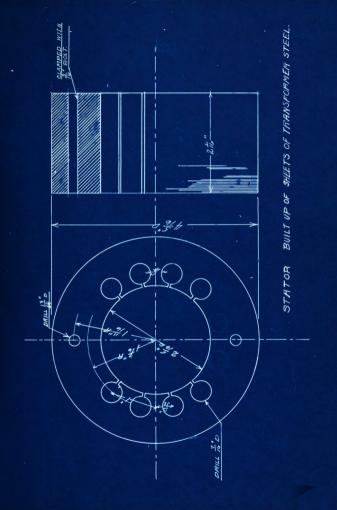
- 1 Stator.
- 2 Armature.
- 3 End Castings.
- 4 Commutator and Brushes.
- 5 Wireing Diagram.

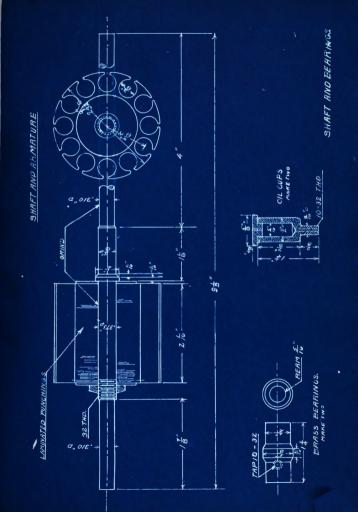
Squirrel Cage Induction Motor Drawings.

L Stator as above with four more slots, so as to make twelve slots equally spaced.

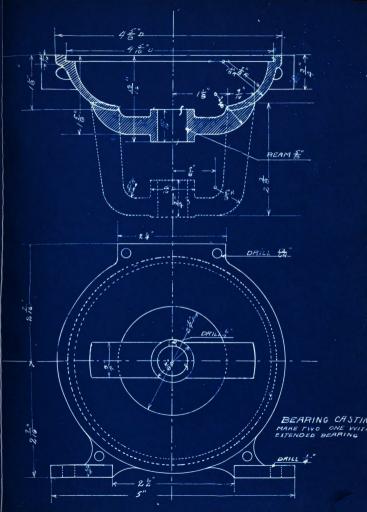
- 2 Squirrel Cage Rotor.
- 3 Bearings and Oil Cups as above.
- 4 End Castings as above, both with the short bearing.
- 5 Base.
- 6 Wireing Diagram.
- 7 Photograph of Finished Machine.

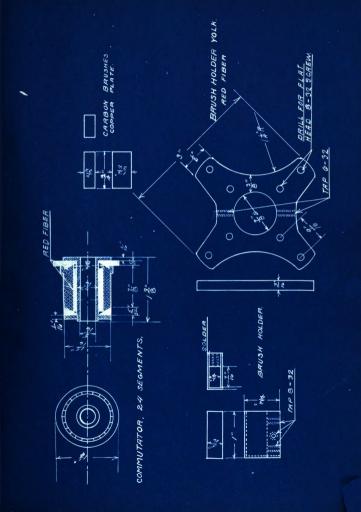
References



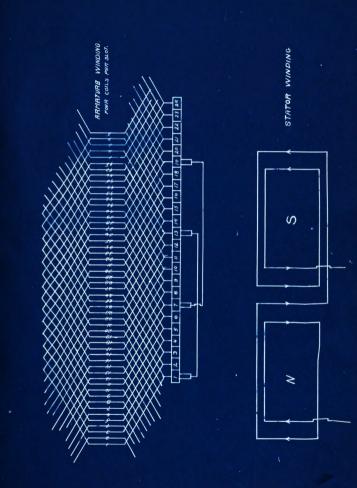


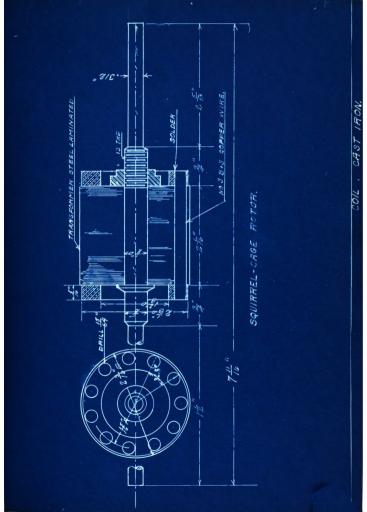
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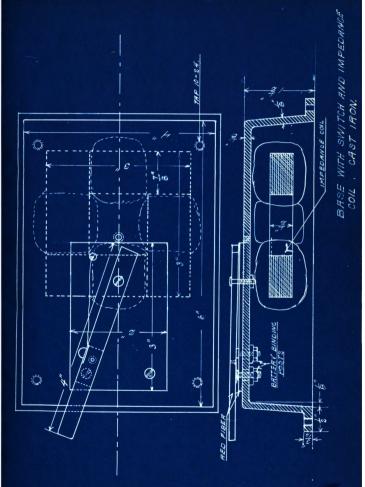




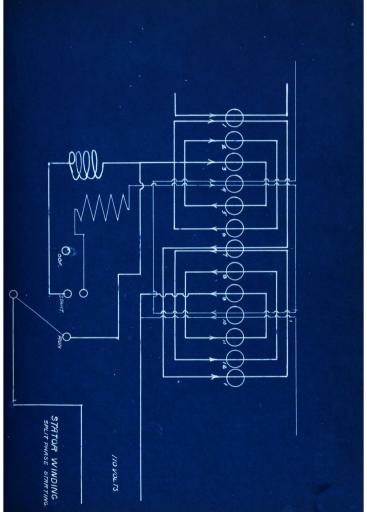
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