



145  
339  
THS

LATERAL PRESSURE OF FLUID  
CONCRETE

Thesis for the Degree of M. S.  
MICHIGAN STATE COLLEGE

Robert Charles McLavy  
1950



3 1293 01067 1737

This is to certify that the  
thesis entitled  
LATERAL PRESSURE OF FLUID CONCRETE

presented by  
ROBERT CHARLES McLRAVY

has been accepted towards fulfillment  
of the requirements for  
M. S. degree in CIVIL ENGINEERING

A handwritten signature in cursive script, appearing to read "E. M. Gadsby".

Major professor

Date MAY 22, 1950

LATERAL PRESSURE OF FLUID CONCRETE

By

Robert Charles McLravy

A THESIS

Submitted to the School of Graduate Studies of Michigan

State College of Agriculture and Applied Science

in partial fulfillment of the requirements

for the degree of

MASTER OF SCIENCE

Department of Civil Engineering

1950

THESIS

#### ACKNOWLEDGEMENT

The author wishes to acknowledge the many helpful comments and suggestions which he has received from members of the faculty and also his appreciation for the materials and assistance furnished by the Michigan State Highway Research Laboratory at East Lansing.

## TABLE OF CONTENTS

Page	
1	Introduction
3	Proceedure
5	Sketch of Test Form
6	Computations for Test #1
11	Computations for Test #2
14	Graph Showing Results
15	Conclusion

## INTRODUCTION

During the summer of 1949, the occasion arose for the investigation and checking of the design of the formwork for a concrete bridge abutment. There was some doubt as to correct intervals for placing the walers and tie rods for holding the form together. In order to compute the pressure exerted by the fresh concrete against the form, some value for the unit lateral pressure of fresh concrete had to be selected.

Upon consulting the text books, it was found, as was to be expected, different authors recommended various values for this pressure. These values ranged from as low as 120 psf to 145 psf, the full weight of the concrete. The majority of authors made no differentiation between stiff or lean mixtures of concrete, although they stated that this factor would influence the correct value to be used. If the concrete were to be vibrated into place, instead of hand spaded, most recommended the use of the full equivalent fluid pressure of concrete, generally accepted as 145 psf.

The design of the formwork was then checked, using the 145 psf value. The results showed that the stresses in the tie rods would be almost at the failure point and no additional strength would be provided for impact, vibration and other factor of safety stresses.

When the abutment was poured a close watch was kept upon the formwork. No failure or yielding of the formwork was observed either during the pour or the stripping of the forms afterward. As a result, the impression was formed that the lateral pressure of fluid concrete against formwork was not as great as generally believed.

Thus, the idea of this thesis was born.



## PROCEDURE

At the start of this thesis, it was thought that the Goldbeck Pressure Cells would be used. It was soon discovered, however, that they were not available through the Civil Engineering department and that the cost of them would be greater than this experiment justified. Consequently, another method had to be devised.

After consulting with Dr. Harris, Professor Cade, and Dr. Pien, an arrangement was devised using electric strain gages. This arrangement was made in the form of a wooden box approximately two feet square and five and one half feet high. The lower side of the box was cut out and made into a sliding panel. This panel was held in place by two one-quarter inch circular steel tie rods acting upon 4" x 4" walers across the front of the panel and the back of the form. The box was made of three-quarter inch plywood fastened to 2" x 4"'s and held together with built up 4" x 4"'s and one-quarter inch steel rods. It was so constructed, that the component parts could be stripped, cleaned and easily reassembled.

The forms were erected in the concrete laboratory and the sliding panel shaped until it slid smoothly. Six inch electric strain gages were applied to the two tie rods holding the panel in place. (These gages and the potentiometer for reading them were supplied through the courtesy of the Michigan State Highway Research Laboratory.) Marks were established at distances of two, three, four and five feet above the bottom of the form. The forms were then oiled with mineral oil to prevent bonding between the concrete and the wood.

Concrete was then placed in the forms to the desired height and the deformation of the tie rods recorded by means of the electric strain gages. The concrete was vibrated before each reading using an electric powered, flexible cable type vibrator..

When the forms were filled to the five foot mark, a platform was placed on the concrete and a surcharge added. This was an attempt to determine the elapsed time required to produce enough set in the concrete so that any additional increment of concrete would not produce a corresponding increase in lateral pressure **at the** bottom of the form.

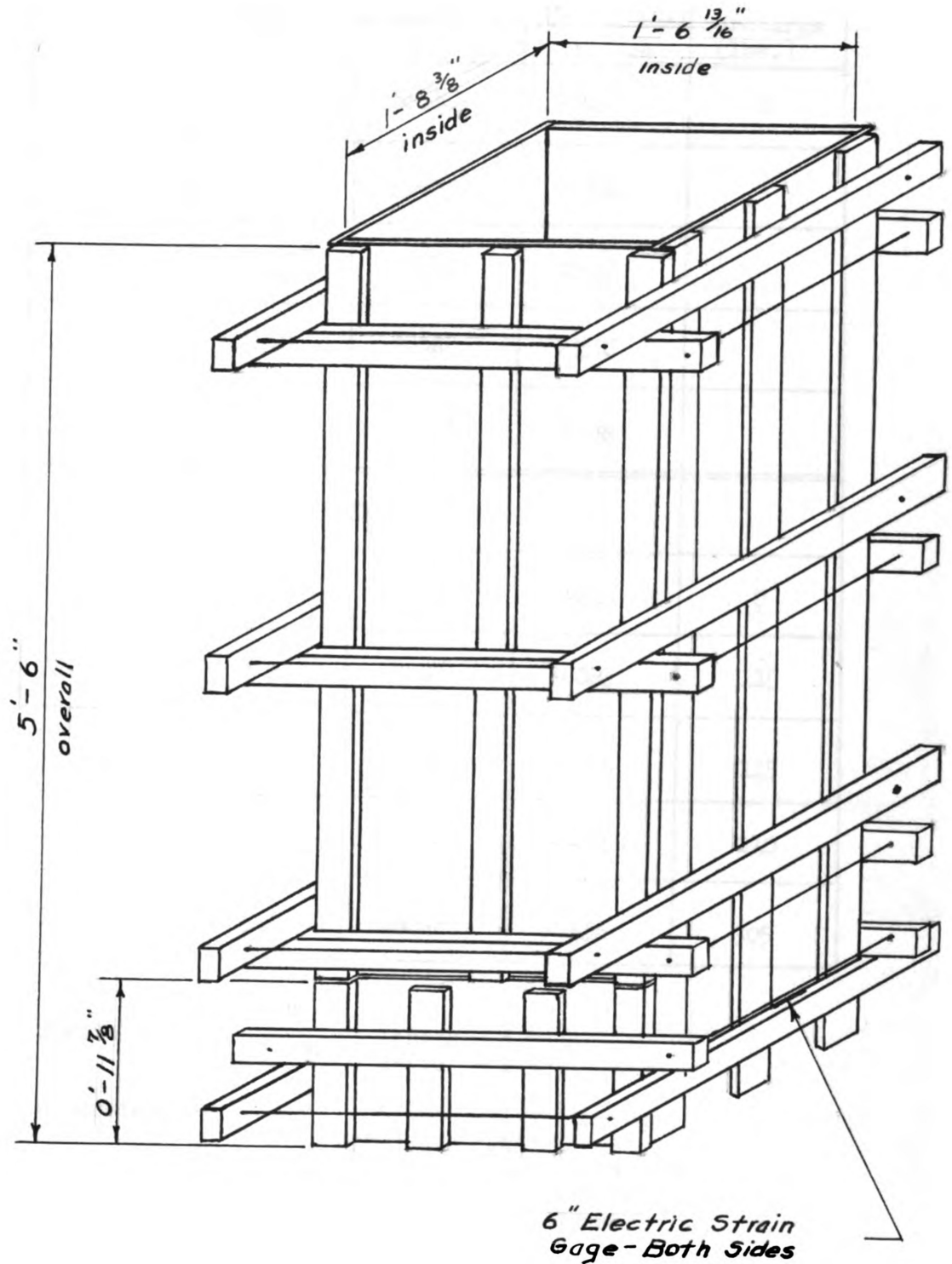
At the end of the experiment the electric strain gages and the tie rods were placed in a tension machine and calibrated. Knowing the area of the movable panel and the force exerted upon the tie rods, the lateral pressure was computed for each depth of concrete. This information was plotted in the form of graphs for comparison between the stiff and the lean mixtures of concrete on the theoretical fluid pressure of each mix.

\* The completion of this thesis was greatly facilitated by the help of Mr. Larry Childs of the Michigan State Highway Research Laboratory.



SKETCH OF TEST FORM

5



## Data Sheet

Trial #1

Time	Depth (ft.)	Strain Gage (micro in.)		Surcharge (lbs.)
		West Gage	East Gage	
11:02 AM	0	595R8	760R5	0
11:15	2.0	680R8	840R5	
11:20	3.0	755R8	910R5	
11:25	4.0	780R8	935R5	
11:31	5.0	800R8	950R5	
	Time of Set			
12:04 PM	5.0	790R8	920R5	0
12:07	5.0	790R8	960R5	115
12:32	5.0	795R8	960R5	115
12:45	5.0	800R8	968R5	210
1:00	5.0	800R8	965R5	305

Strain Gages:

Length - 6.0"

Ratio - 2.13

Concrete :

Slump - 1/2" to 3/4"

Aggregate - 6A

Cement - Air Entraining  
Penninsula

28 day strength - 2,085 psi

T<sub>o</sub> = 58° FT<sub>c</sub> = 62° F

## Computations

## Test #1

Head = <b>1.5'</b>	West Gage	East Gage
	680	840
	<u>595</u>	<u>760</u>
difference	85	80    micro-inches

$$100 \times 85 / 74.33 = 114.5 \text{ lbs}$$

$$100 \times 80 / 75.2 = \underline{106.2} \text{ lbs}$$

$$220.7 \text{ lbs}$$

$$\text{Panel area } 18.82 \times \underline{11.87} = 1.550 \text{ sq. ft.}$$

$$\text{Lateral pressure } \frac{220.7}{114} / 1.550 = 142.5 \text{ psf.}$$

Head = <b>2.5'</b>	755	910
	<u>595</u>	<u>760</u>
	160	150

$$100 \times 160 / 74.33 = 215 \text{ lbs.} ; 100 \times 150 / 75.2 = 199.8 \text{ lbs.}$$

$$215 + 199.8 = 414.8 \text{ lbs.}$$

$$414.8 / 1.55 = 267 \text{ psf.}$$

Head = <b>3.5'</b>	780	935
	<u>595</u>	<u>760</u>
	185	175

$$185 \times 100 / 74.33 = 249 \text{ lbs.} \quad 100 \times 175 / 75.2 = 233 \text{ lbs.}$$

$$249 + 233 = 482$$

$$482 / 1.55 = 311 \text{ psf.}$$

Head = 4.5'

West Gage

East Gage

800

950

595760

205

190

$$100 \times 205 / 74.33 = 276 \text{ lbs. ; } 100 \times 190 / 75.2 = 253 \text{ lbs.}$$

$$276 \quad 253 \quad 529 \text{ lbs.}$$

$$529 / 1.55 \quad 342 \text{ psf.}$$

## Weight per cubic foot

volume of container	0.1962 cu. ft.
---------------------	----------------

weight of container	0.50 lbs.
---------------------	-----------

full weight sample #1	29.19 lbs
-----------------------	-----------

#2	28.87
----	-------

#3	<u>28.63</u>
----	--------------

3	<u>86.69</u>
---	--------------

$$28.896 - 0.5 = 28.396 \text{ lbs.}$$

$$28.396 / 0.1962 = 144.5 \text{ lbs. per cu. ft.}$$

## Compressive strength

10 day average	2018 psi.
----------------	-----------

28 day	2085 psi.
--------	-----------

## Strain Gage Calibration for Trial #1

## East Gage

No	Load (pounds)	Gage Reading (micro inches)	Increment
1	1,000	729R6	
2	2,000	1491R6	762
3	2,000	846R7	
4	3,000	1587R7	741

$1503/20 = 75.15$  micro inches per 100 pounds

## West Gage

No	Load (pounds)	Gage Reading (micro inches)	Increment
1	100	530	
2	200	605	75
3	300	682	75
4	400	756	74
5	500	832	76
6	600	905	73
7	700	976	73

$446/6 = 74.33$  micro inches per 100 pounds



## Data Sheet

Trial #2

Time	Depth (ft)	Strain Gage (micro in.)		Surcharge (lbs.)
		West Gage	East Gage	
10:05 AM	0	530R8	680R8	
10:15	2.0	650R8	755R8	
10:20	3.0	730R8	860R8	
10:24	4.0	785R8	920R8	
10:30	5.0	860R8	1000R8	
	Time of Set			
11:20	5.0	850R8	1005R8	0
11:30	5.0	835R8	995R8	0
11:35	5.0	840R8	1000R8	205
11:45	5.0	840R8	1000R8	205
12:00 PM	5.0	840R8	1000R8	205

Strain Gages:

Length - 6.0"

Ratio - 2.13

Concrete:

Slump - 2 1/2" to 3"

Aggregate - 6A

Cement - Air Entraining  
Penninsula

28 day strength - 3350 psi

T<sub>o</sub> = 65° FT<sub>r</sub> = 58° F

## Computations

## Test #2

Head = <b>1.5'</b>	West Gage	East Gage
	650	755
	<u>530</u>	<u>680</u>
	difference 120	75 micro-inches

$$100 \times 120 / 74.33 = 161.5 \text{ lbs.} ; 100 \times 75 / 75.6 = 99.2 \text{ lbs.}$$

$$161.5 + 99.2 = 260.7 \text{ lbs.}$$

$$\text{Lateral pressure} \quad 260.7 / 1.55 = 172 \text{ psf}$$

Head = <b>2.5'</b>	730	860
	<u>530</u>	<u>680</u>
	200	180

$$100 \times 200 / 74.33 = 269 \text{ lbs.} ; 100 \times 180 / 75.6 = 238 \text{ lbs.}$$

$$269 + 238 = 507 \text{ lbs.}$$

$$\text{Lateral pressure} \quad 507 / 1.55 = 327 \text{ psf.}$$

Head = <b>3.5'</b>	785	920
	<u>530</u>	<u>680</u>
	255	240

$$100 \times 255 / 74.33 = 344 \text{ lbs.} ; 100 \times 240 / 75.6 = 318 \text{ lbs.}$$

$$344 + 318 = 662 \text{ lbs.}$$

$$\text{Lateral pressure} \quad 662 / 1.55 = 427 \text{ psf.}$$

Head = <b>4.5'</b>	West Gage	East Gage
	860	1000
	<u>530</u>	<u>690</u>
	330	320

$$100 \times 330 / 74.33 = 443 \text{ lbs. ; } 100 \times 320 / 75.6 = 423 \text{ lbs.}$$

$$443 + 423 = 866 \text{ lbs.}$$

$$\text{Lateral pressure } 866 / 1.55 = 560 \text{ psf.}$$

#### Weight per cubic foot

volume of container	0.1962 cu. ft.
weight " "	0.50 lb.
full weight sample #1	30.25 lbs.
#2	30.19
#3	<u>30.22</u>
	3  <u>90.66</u>
	$30.25 - 0.5 = 29.72 \text{ lbs.}$
	$29.72 / 0.1962 = 150.6 \text{ lbs. per cu. ft.}$

#### Compressive strength

14 day average	2,598 psi.
28 day "	3,350 psi.

## Strain Gage Calibration for Trial #2

## East Gage

No	Load (pounds)	Gage Reading (micro inches)	Increment
1	200	885	
2	300	945	60 omit
3	400	1020	75
4	500	1096	76
5	600	1170	74
6	700	1245	75
7	800	1323	78

$$378/5 = 75.6 \text{ micro inches per 100 pounds}$$

## West Gage

No	Load (pounds)	Gage Reading (micro inches)	Increment
1	100	530	
2	200	605	75
3	300	680	75
4	400	756	76
5	500	832	76
6	600	905	73
7	700	976	73

$$446/6 = 74.33 \text{ micro inches per 100 pounds}$$



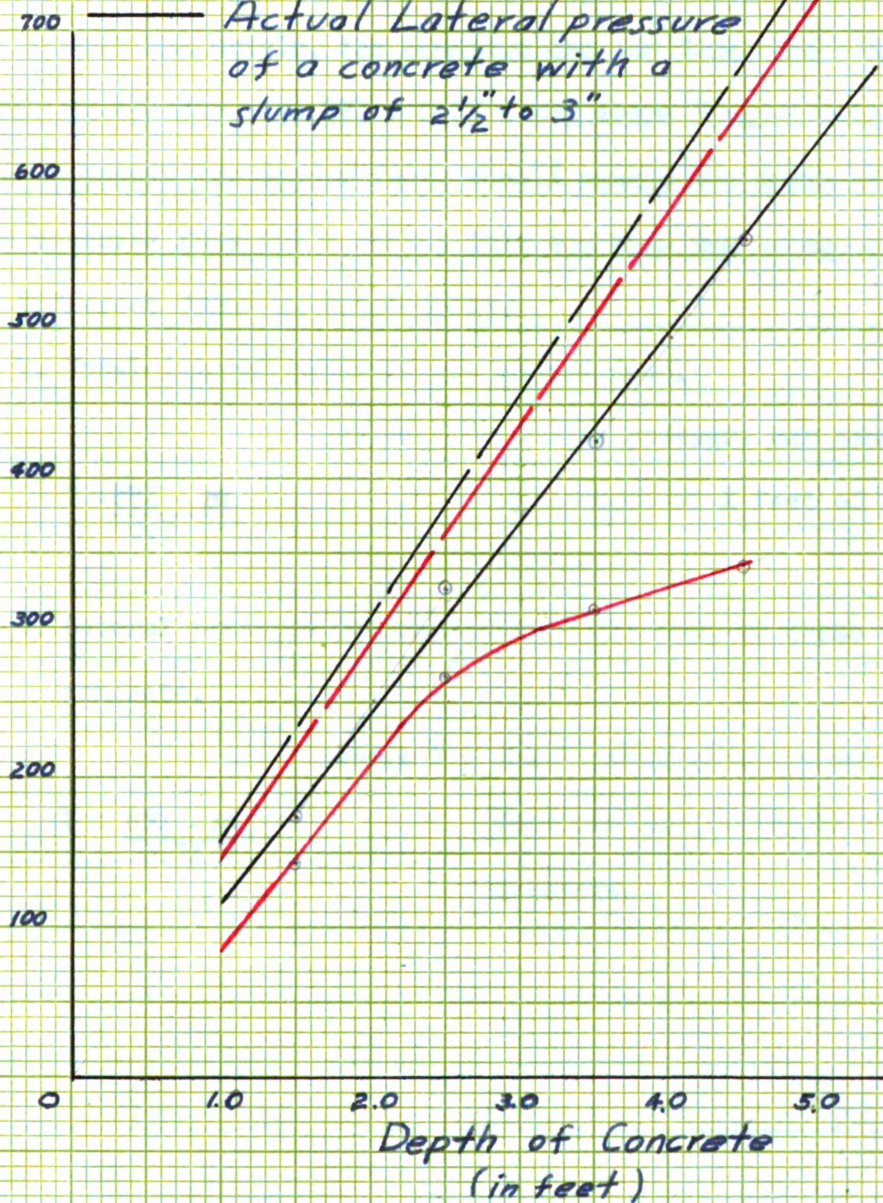
### Test 1

- Theoretical lateral pressure of a liquid weighing 144.5 lbs. per cu. ft.
- Actual lateral pressure of a concrete with a slump of  $\frac{3}{4}$ "

### Test 2

- Theoretical lateral pressure of a liquid weighing 150.6 lbs. per cu. ft.
- Actual Lateral pressure of a concrete with a slump of  $2\frac{1}{2}$ " to 3"

Lateral Pressure  
(pounds per square foot)





## CONCLUSION

The following formulae for lateral pressure may be developed using the results of Test #2, which was performed with a 3,000 psi. concrete having a slump of 2 1/2" to 3", a common mix in construction work.

Since the graph of this test resulted in a straight line not passing through the origin, the equation has the form of  $AX + BY = K$ , or in this particular case  $89X - 0.7Y = 10$ , where Y equals the lateral pressure in pounds per square foot, when X equals the depth of fluid concrete measured from the surface. This equation can be arranged into the two different forms as shown below.

1. Total lateral pressure per square foot.

where Y = lateral pressure per square foot

$$Y = \frac{89X - 10}{0.7}$$

at a depth of X feet of fluid  
concrete.

2. Lateral pressure per square foot per foot of depth of fluid concrete.

where Y = the lateral pressure per square

$$Y = \frac{89X - 10}{0.7X}$$

foot per foot of depth X of fluid  
concrete.



Substituting values for X and Y in equation (2) gives the following results.

X = 1.0'	Y = 113.0 psf
X = 2.0'	Y = 120.0 psf
X = 3.0'	Y = 122.0 psf
X = 4.0'	Y = 123.8 psf
X = 5.0'	Y = 124.3 psf

As  $X \rightarrow \infty$  the value of Y approaches a limit, thus:

$$\lim_{X \rightarrow \infty} \frac{89X - 10}{0.7X} = \lim_{X \rightarrow \infty} \frac{89}{0.7} = 127.3 \text{ psf}$$

Consequently, the results of these tests indicate that for forms whose dimensions compare with those of the test forms and where the rate of filling is not over five feet per thirty minutes at a minimum temperature of 60° F., the formwork should be designed to resist a lateral pressure of 125 psf per foot of depth of fluid concrete. This value of 125 is believed to be preferable to the actual computed value of 124.3 psf for a five foot depth because it will include all the above stated depths and the designer has only one value to remember instead of several.

It was originally thought that as a collary of this thesis the determination of time of set of concrete in forms could be measured. The data gathered from this part of the work, however, was not conclusive. A different apparatus should be used for that determination. It can be seen from the data sheets that as the time interval increased after the last increment of concrete had been added, the strain gage readings started to decline although a surcharge was



placed upon the fresh concrete. This was caused probably by the shrinkage of the concrete as it began to set. This does, however, indicate that as concrete takes its initial set, more concrete can be poured into the forms without an increase in the lateral pressure at the bottom of the form.

ROOM USE ONLY

NO. 100-100000

MAR 02 1958



MICHIGAN STATE UNIV. LIBRARIES



31293010671737